

## Introduction

- A two dimensional multifluid code which treats the electrons, reacting ions and the generated alphas as separate fluids which interact with the electric and the magnetic fields has been developed.
- The system of equations which the code solves are the fluid equations for each of the plasma species supplemented by Maxwell's equations.

## Model description

### Fluid Equations for each of the species

Continuity: 
$$\frac{\partial \rho_s}{\partial t} + \nabla \cdot (n_s \mathbf{v}_s) = 0$$

Momentum: 
$$\frac{\partial \rho_s \mathbf{v}_s}{\partial t} + \nabla \cdot (n_s \mathbf{v}_s \mathbf{v}_s + pI) = q_s n_s (\mathbf{E} + \mathbf{v}_s \times \mathbf{B})$$

Energy: 
$$\frac{\partial \varepsilon_s}{\partial t} + \nabla \cdot (\mathbf{v}_s) (\varepsilon_s + p_s) = q_s n_s \mathbf{v}_s \cdot \mathbf{E}$$

and Maxwell's equations

### Production of alpha particles

- The reacting ions are 50% Tritium – 50% Deuterium and are treated as a single fluid with particle mass  $2.5m_p$
- The reaction rate is (Bosch Halle 1992):  $R = \frac{1}{4} n_i^2 \langle \sigma(u) \rangle$
- Appropriate sink and source terms are introduced in the fluid equations

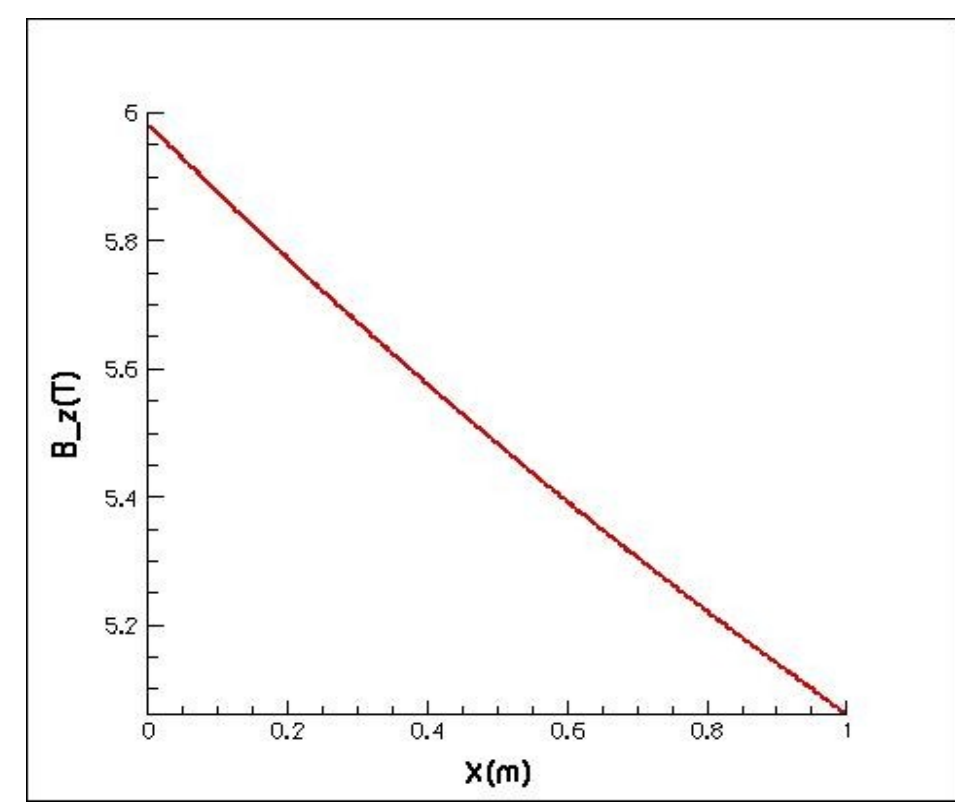
### System of equations in Cartesian geometry

Is of the form: 
$$\frac{\partial \mathbf{q}}{\partial t} + \frac{\partial \mathbf{F}(\mathbf{q})}{\partial x} + \frac{\partial \mathbf{G}(\mathbf{q})}{\partial y} = \mathbf{S}(\mathbf{q})$$

where:

$$\mathbf{q} = \left( \rho_e, \rho_i, \rho_\alpha, \right. \\ \left. \rho_e u_x^e, \rho_e u_y^e, \rho_e u_z^e, \right. \\ \left. \rho_i u_x^i, \rho_i u_y^i, \rho_i u_z^i, \right. \\ \left. \rho_\alpha u_x^\alpha, \rho_\alpha u_y^\alpha, \rho_\alpha u_z^\alpha, \right. \\ \left. \varepsilon_e, \varepsilon_i, \varepsilon_\alpha, \right. \\ \left. E_x, E_z, E_z, B_x, B_y, B_z \right)$$

ITER-like Magnetic Field (f/r)



The above system of equations is solved using a Total Variation Diminishing method in space and Runge-Kutta in time.

## 2D Scenario: Early stage of burning process

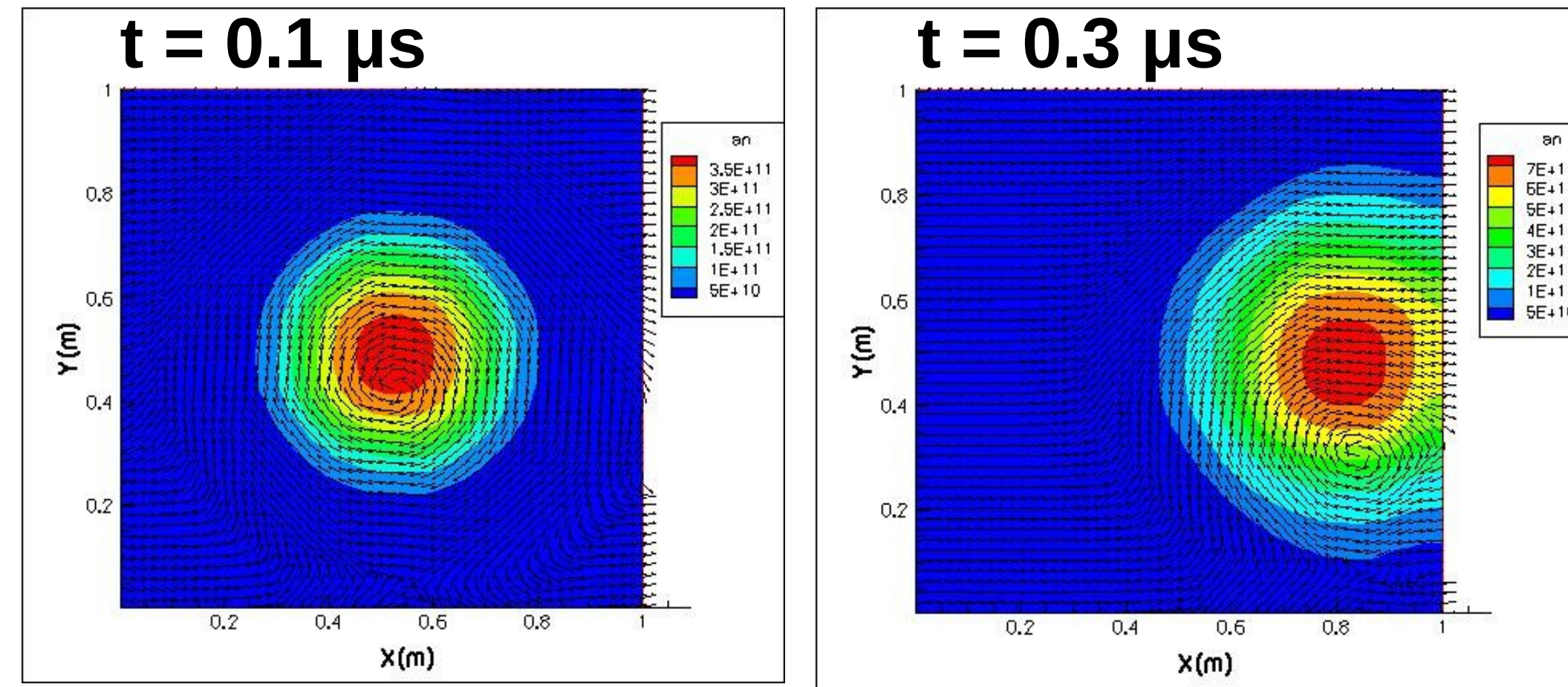
A high pressure circular plasma blob is placed in the center of the two-dimensional computational domain.

Parameters of the blob  
Plasma temperature = 22.5 keV  
Plasma density =  $2 \times 10^{20} \text{ m}^{-3}$   
Blob radius = 0.2 m

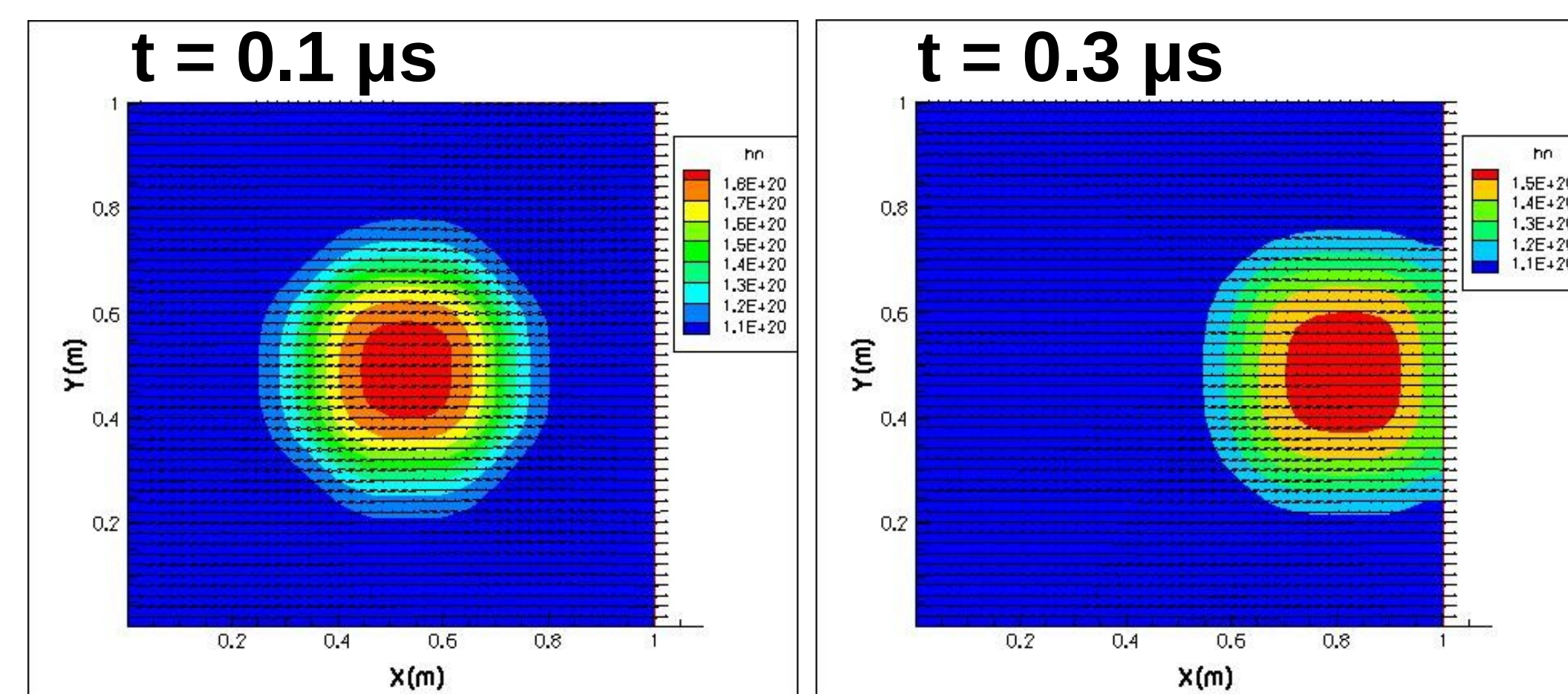
Background plasma  
Plasma temperature = 5 keV  
Plasma density =  $10^{20} \text{ m}^{-3}$

### Positive magnetic field

Alpha particles densities and velocities

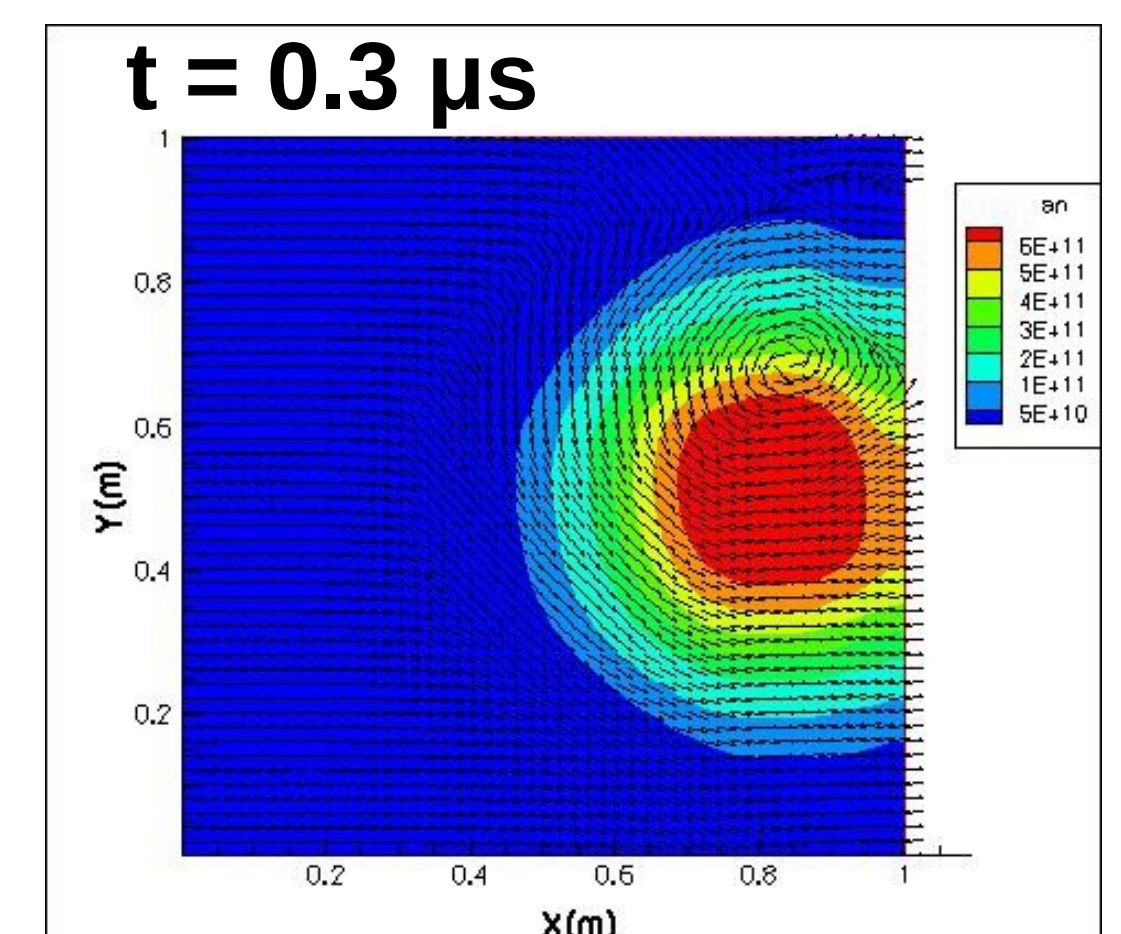
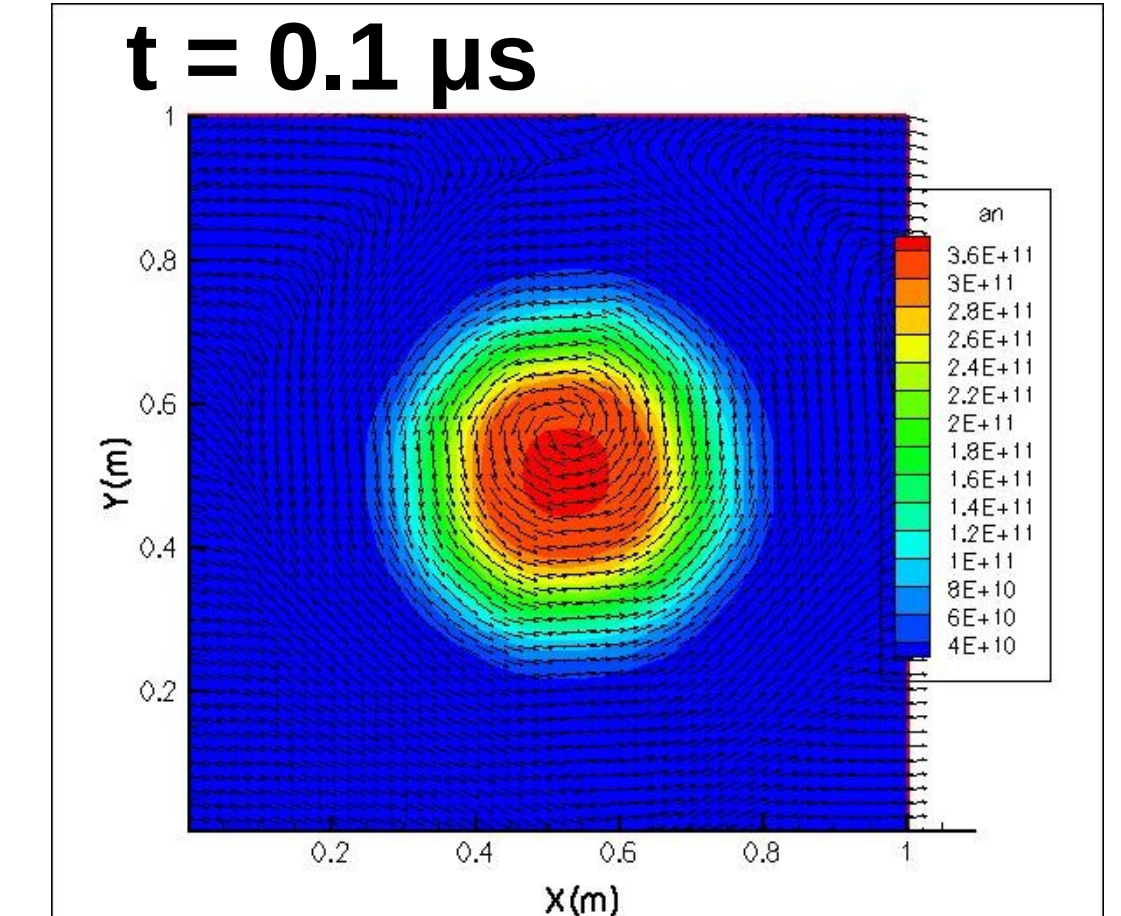


Reacting ions densities and velocities



### Negative magnetic field

Alpha particles densities and velocities



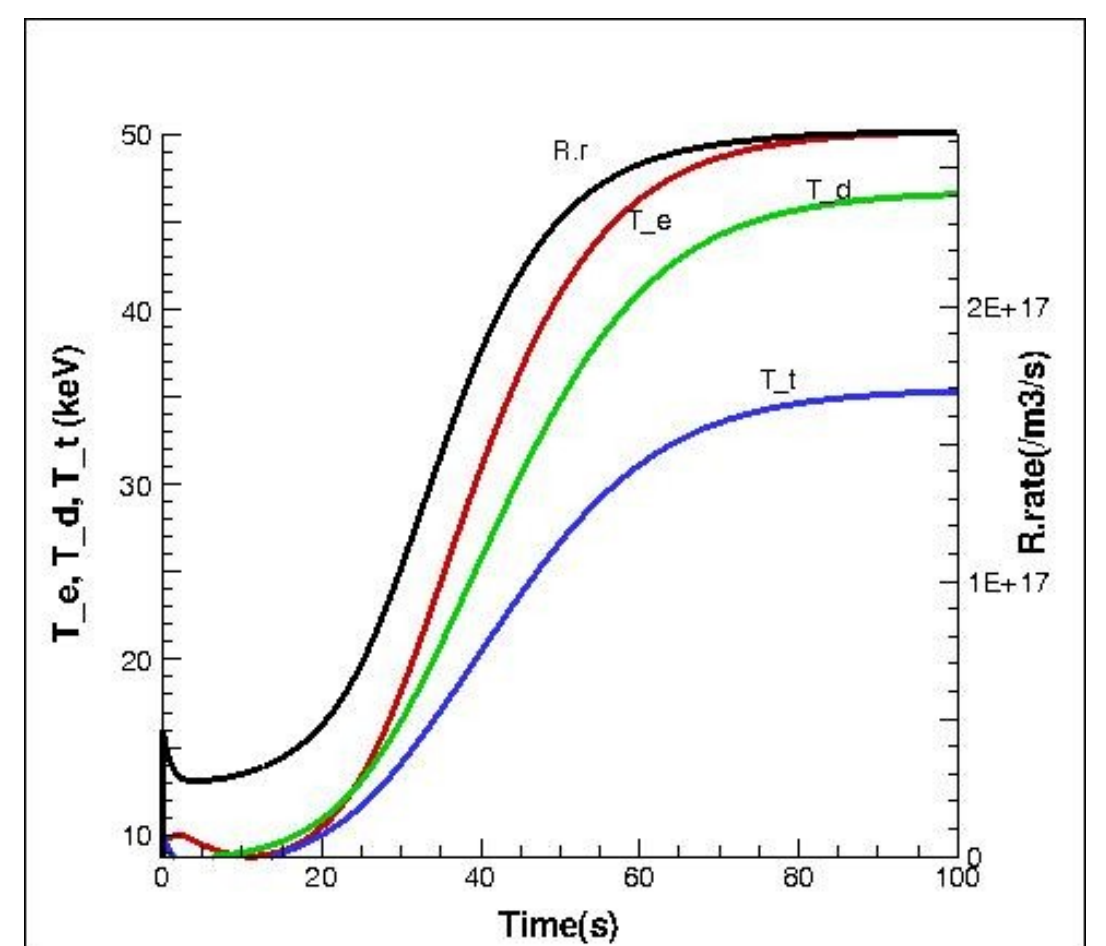
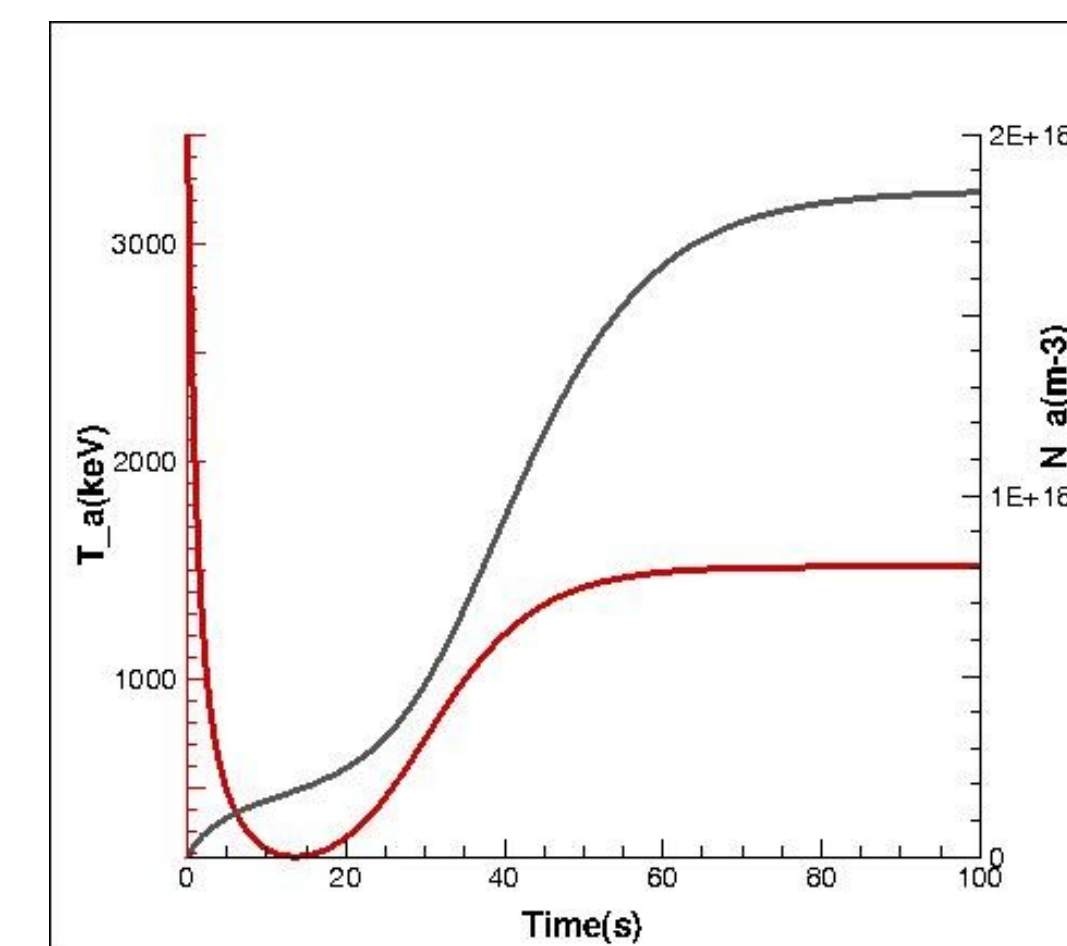
## Results from zero-dimensional model

### Alpha heating

#### Initial Conditions:

$$T_e = 10 \text{ keV} \\ n_e = 0.4 \times 10^{20} \text{ m}^{-3}$$

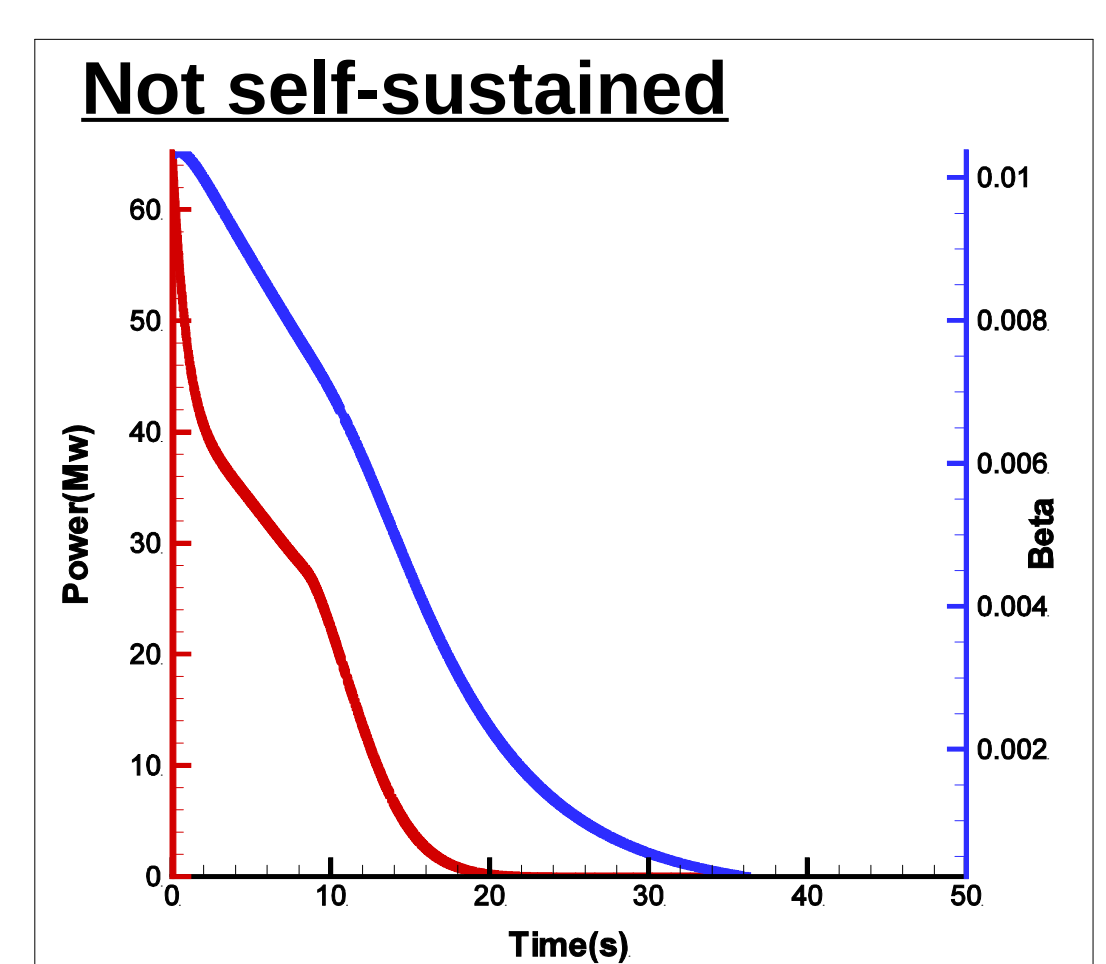
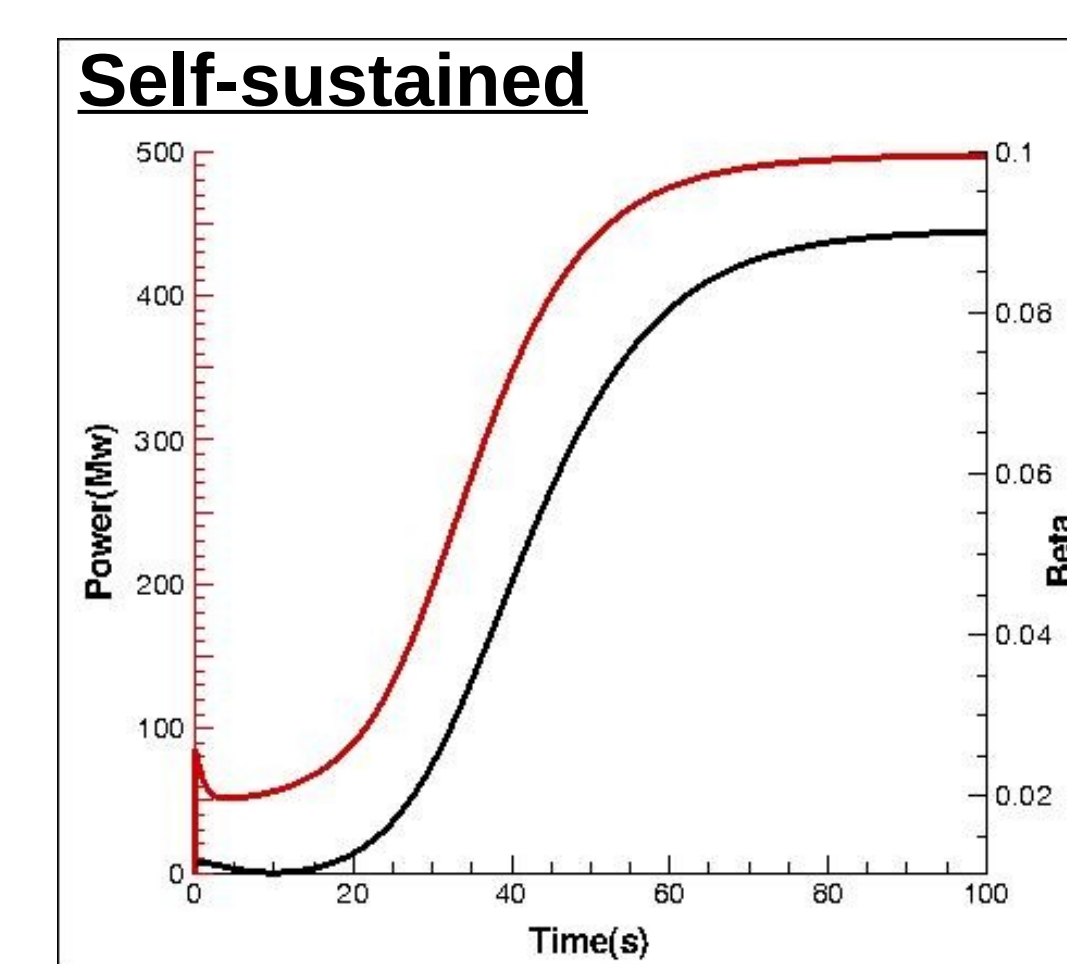
Alpha particles, originally generated with 3.5 MeV of energy, heat the rest of the plasma species



### Steady state

Depending on the initial conditions the burning plasma can either reach a steady state or extinguish.

IC for steady state:  
 $T_e = 10 \text{ keV} / n_e = 0.4 \times 10^{20} \text{ m}^{-3}$   
IC for extinguishing plasma:  
 $T_e = 9 \text{ keV} / n_e = 0.4 \times 10^{20} \text{ m}^{-3}$



## Zero-dimensional alpha heating model

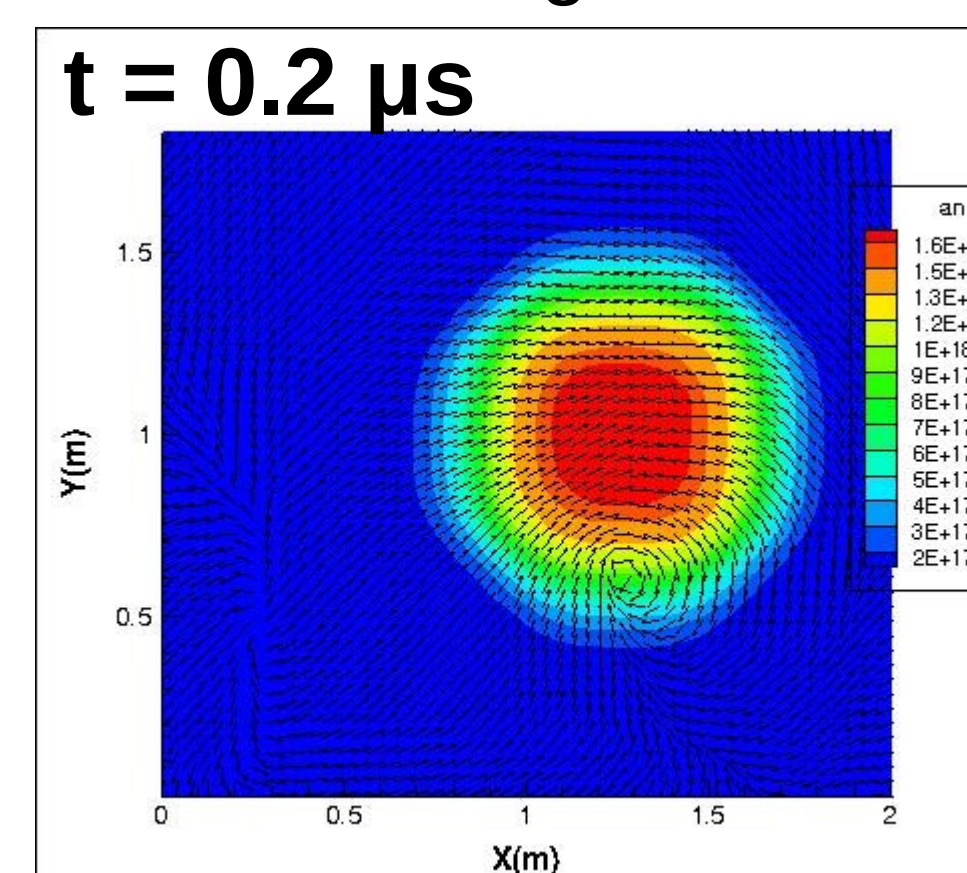
- Multi-fluid plasma burning model
- Conservation of the various plasma species particles (electrons, reacting ions and alphas generated by nuclear reactions)
- Energy balance of plasma species
- System of 8 ODEs for D/T plasma

- Output:
  - Power output
  - Reacting ions and alpha particle densities and temperatures
  - Under what initial conditions will the reactor operate in a steady state**

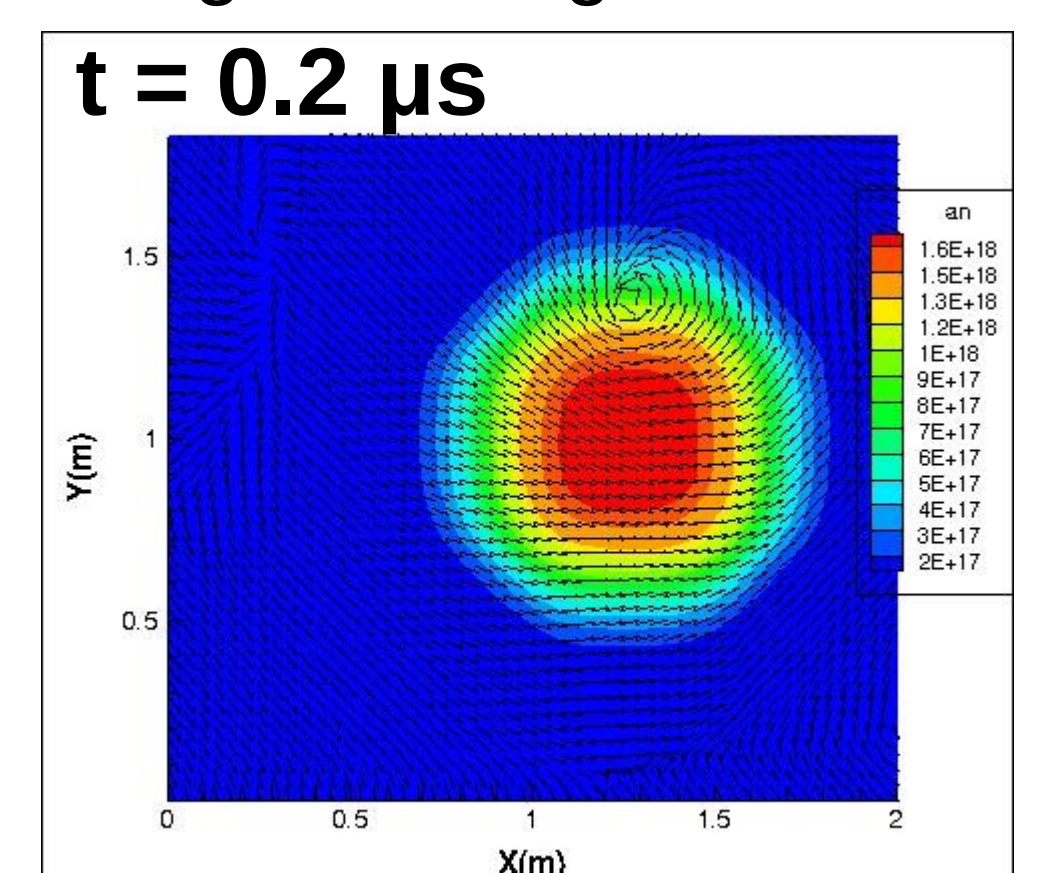
## 2D Scenario: Initial conditions from steady state

### Alpha particles densities and velocities

#### Positive magnetic field



#### Negative magnetic field



A plasma blob with it's initial conditions taken from the zero-dimensional model operating at steady state is placed at the center of the two dimensional computational domain

Parameters of the blob:  
Ion temperature = 40.5 keV  
Ion density =  $0.36 \times 10^{20} \text{ m}^{-3}$   
Alpha temperature = 1.5 MeV  
Alpha density =  $1.85 \times 10^{18} \text{ m}^{-3}$

## Summary

- For ITER-like magnetic fields:
  - a) For electrons and reacting ions the *gradB* drift dominates.
  - b) For the alpha particles the **ExB** rotations are substantial
- The two-fluid approximation allows the study of **ExB** rotations
- Similar 2D code in R-Z geometry and separate fluid for each reacting ion is under development