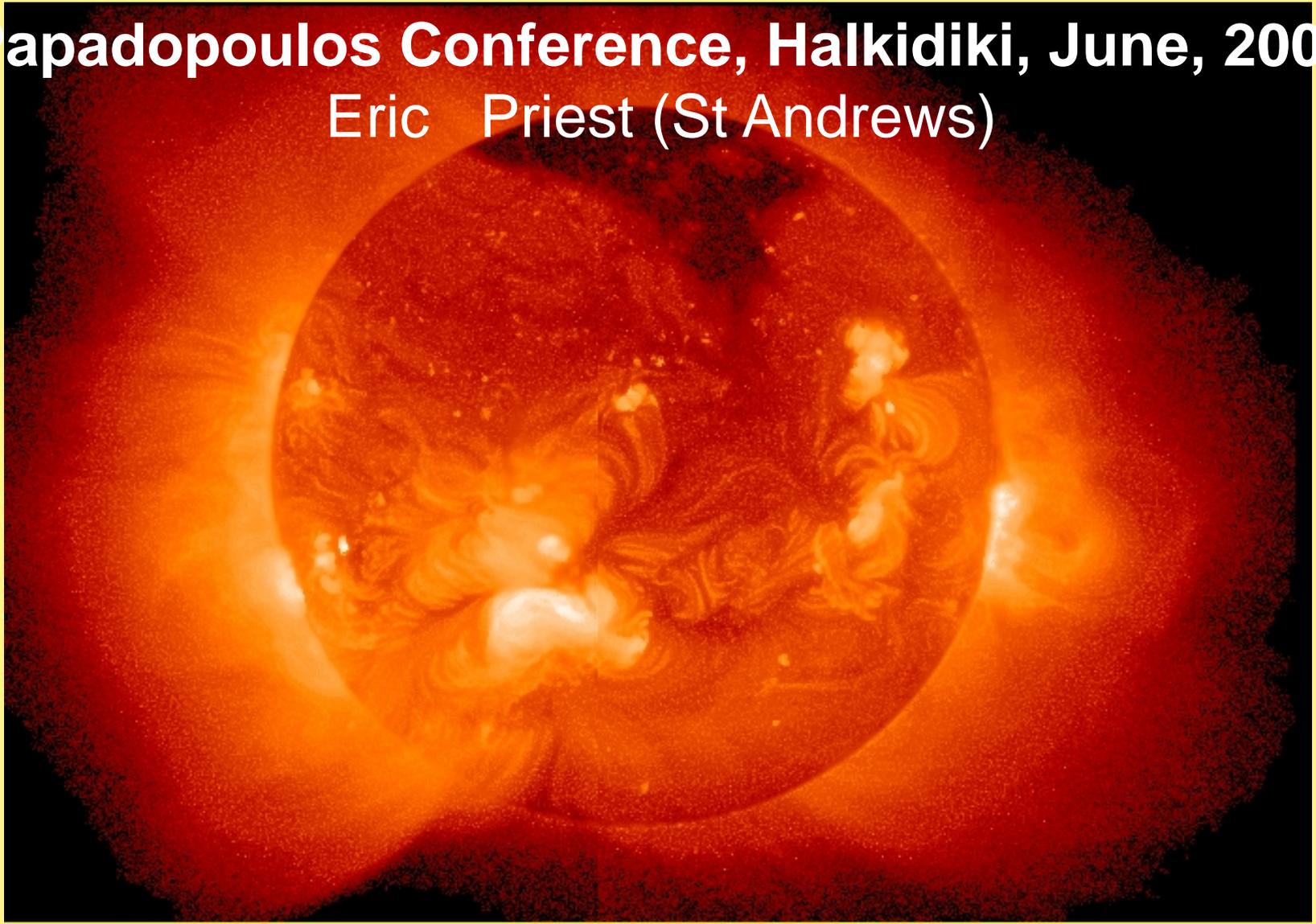


# **NONLINEAR PLASMA PHYSICS of the SOLAR CORONA**

**(Papadopoulos Conference, Halkidiki, June, 2009)**

Eric Priest (St Andrews)



# Introduction: Dennis Papadopoulos

PhD Maryland 1968 --> NRL 10 years --> Maryland University  
(I - 1969 - coll<sup>less</sup> shocks - plasma complic<sup>d</sup> --> MHD!)

\* **Dennis:** microscopic plasma astrophysics:  
**revolutionary ideas:**

- \* strong turbulence in beam-plasma interactions  
--> understand type III radio bursts
- \* anomalous transport & resistivity in ionosphere
- \* Collisionless shocks -->
  - Earth's bow shock - heat ions
  - Supernova shocks - heat electrons  
(at high  $M_A$  by 2 stream instab<sup>y</sup>)

**Approach:** \* Use state of art computing

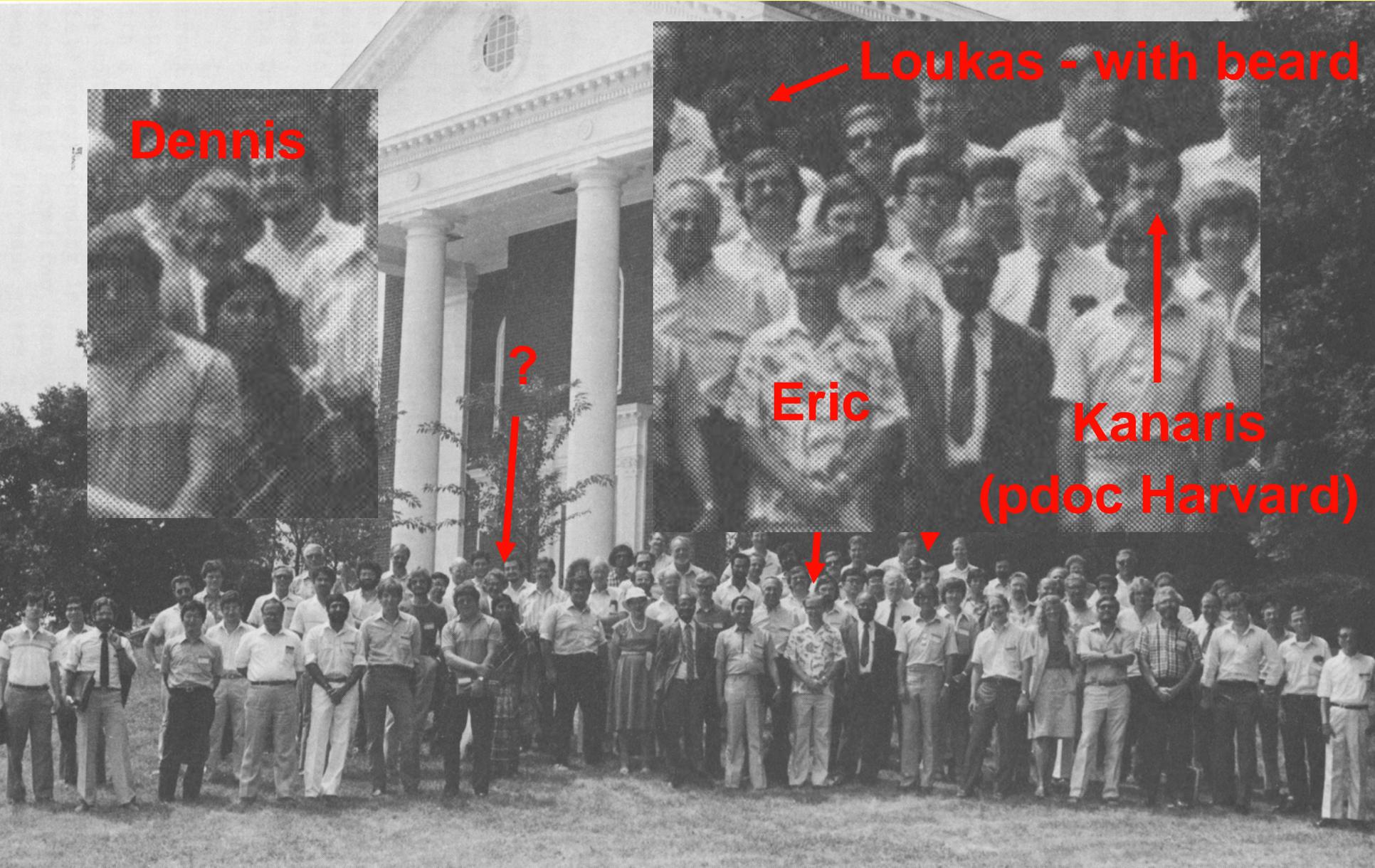
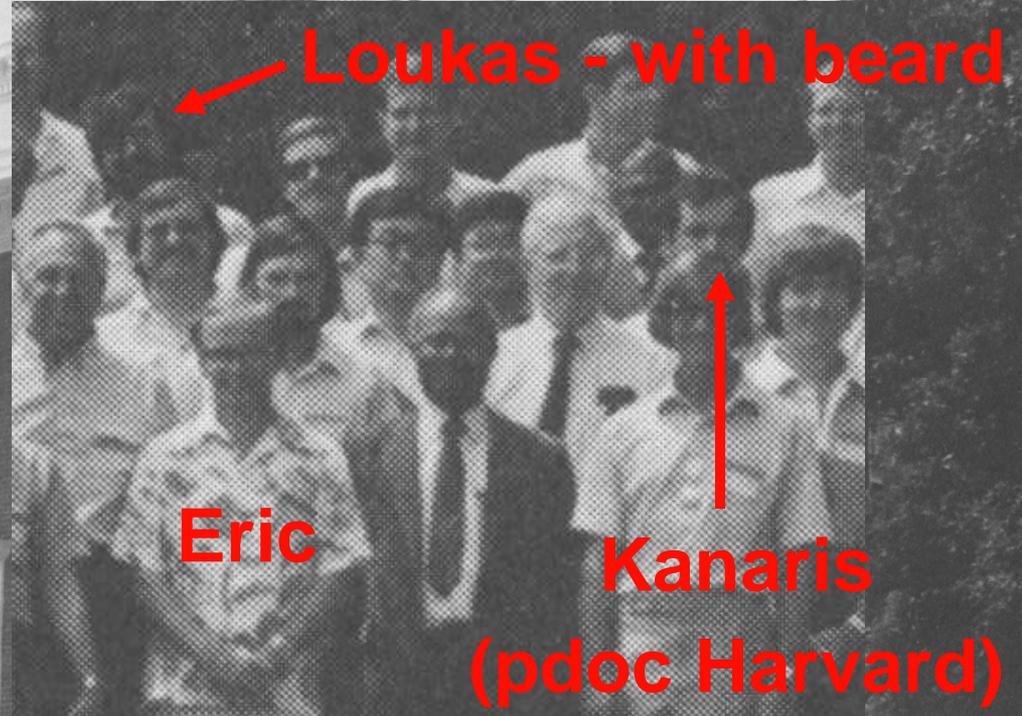
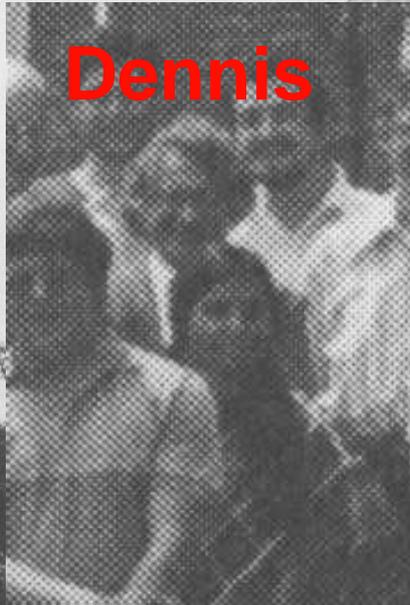
\* Highly creative ideas

# IAU Symposium, Maryland, 1979

(Dennis - invited review on physics of type III radio bursts)



# Symposium, Maryland, 1983



# Loukas Vlahos

PhD Maryland 1979 with Kundu & Dennis P

-> army -> Maryland (1981-1985) -> Thessaloniki

## Annecy SMY Workshop (1981)

I and student Peter Cargill (Ph D 81) met Loukas

--> Boulder 1982-84

Loukas persuaded Peter

--> Maryland 1984-1992 , NRL -1996 --> IC 1996

Parents: hope children fall into good company !

Peter <--> Dennis P

"Dennis taught me all I know about kinetic plasma phys."

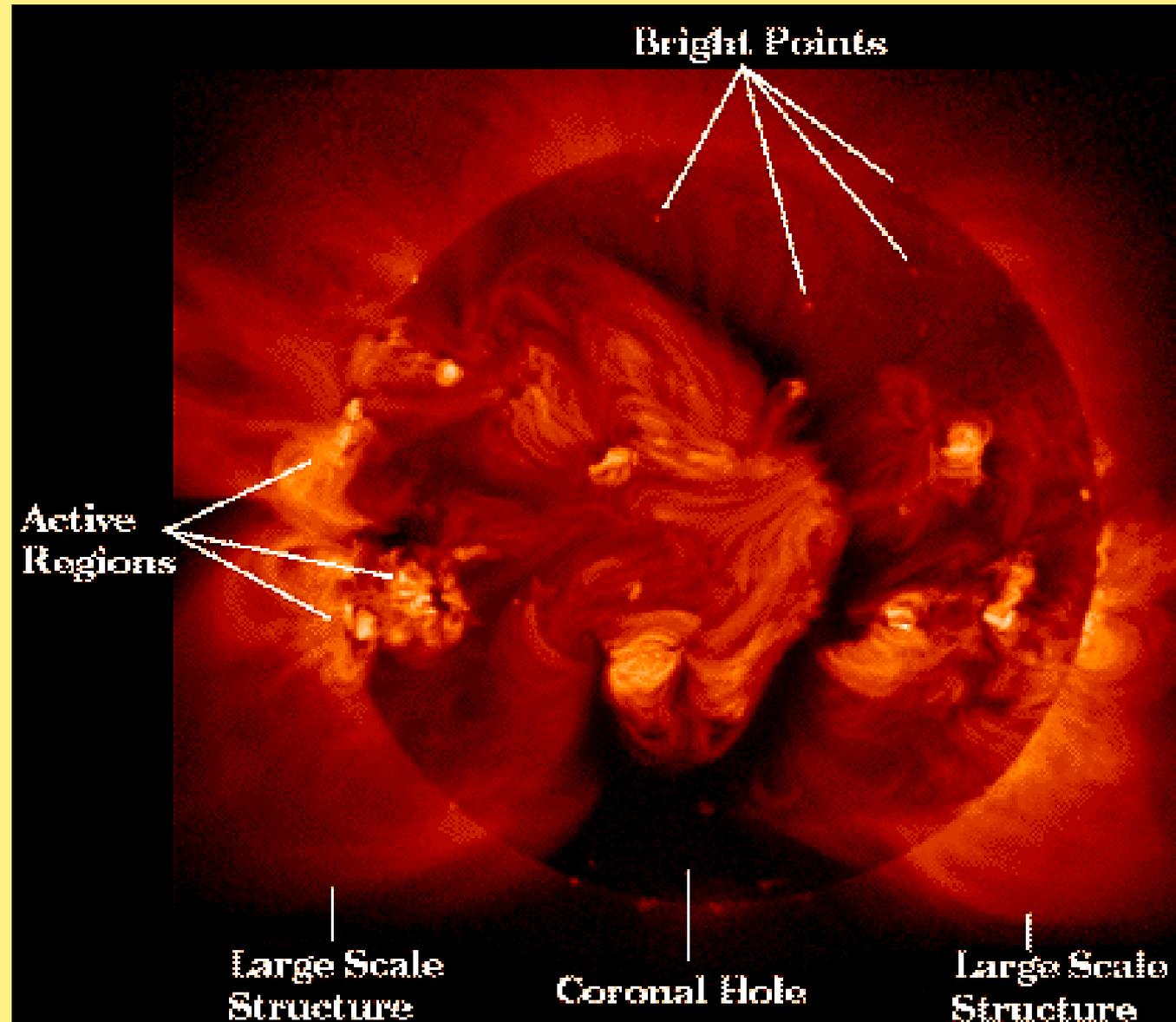


# 1. Introduction - The Corona

**Yohkoh**  
**(5 arcsec):**  
**a dynamic**  
**magnetic**  
**world**

- subtle  
interactions  
B & plasma

Coronal holes,  
Loops,  
X-ray bright pts



# In Corona:

## \* **Fundamental aspects plasma physics --**

Dennis P (& students) ground-breaking contributions:

**Particle acceleration, shock waves,  
instabilities, waves, reconnection**

## \* **Subtle coupling:**

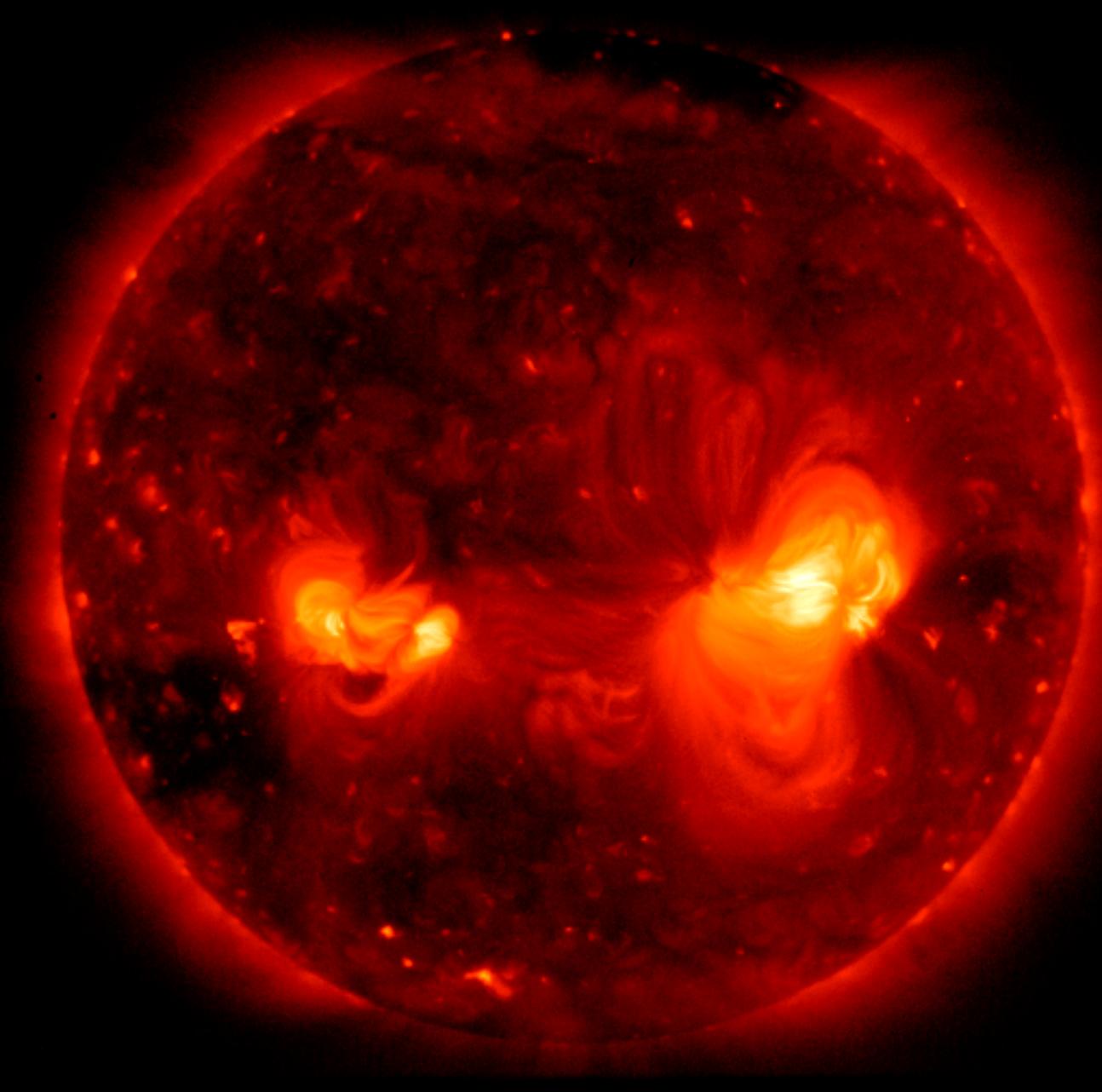
macroscopics (MHD) <----->

microscopics (kinetic plasma physics)

## \* MHD: global environment --

Microscopics --

transport coefficients & particle acceleration



Hinode  
(1 arcsec)

Stunning detail  
on structure  
& dynamics

**How is corona heated?**

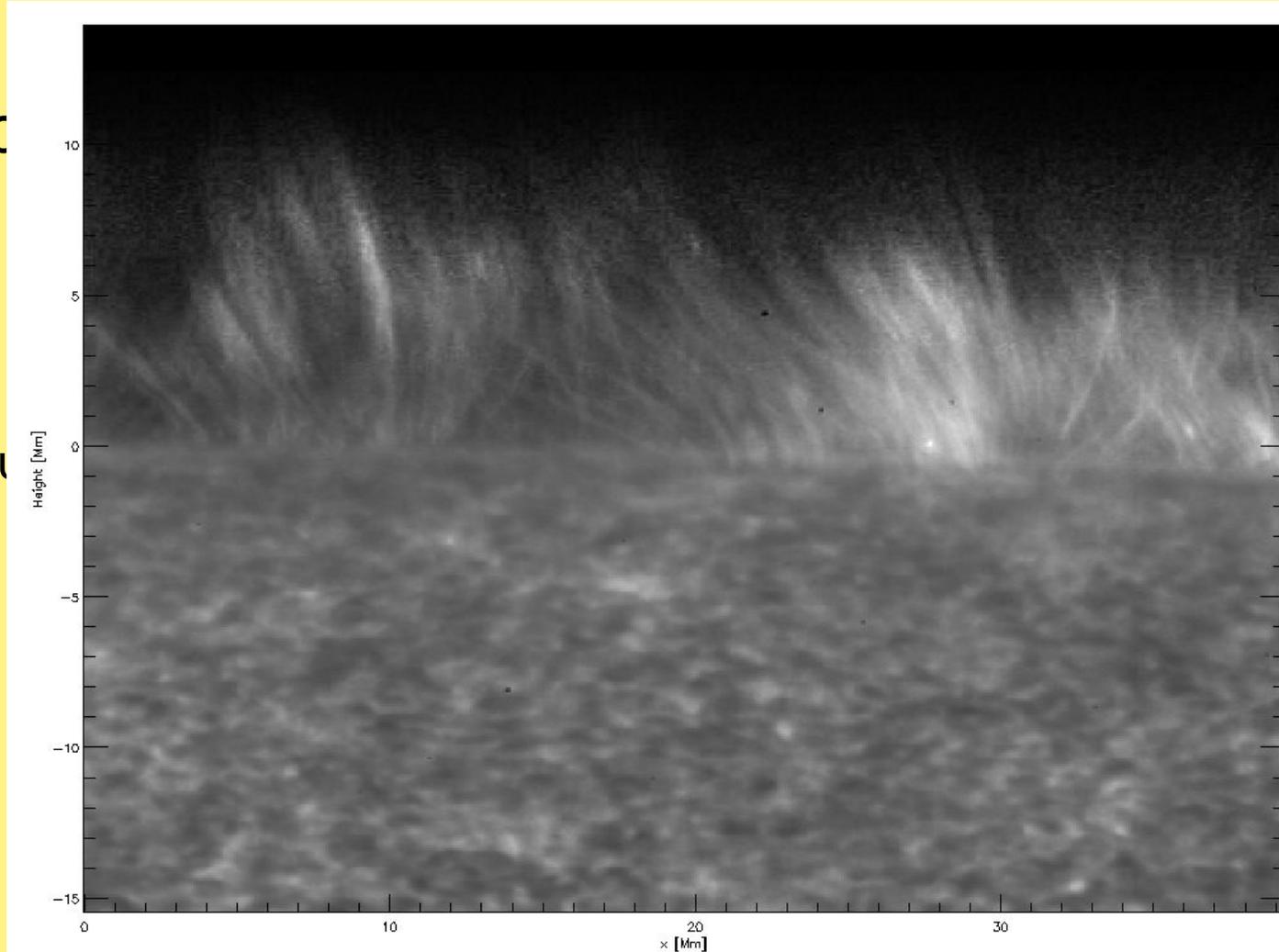
# Waves or reconnection?

- Low-freq. waves in loops [TRACE] -too weak to heat

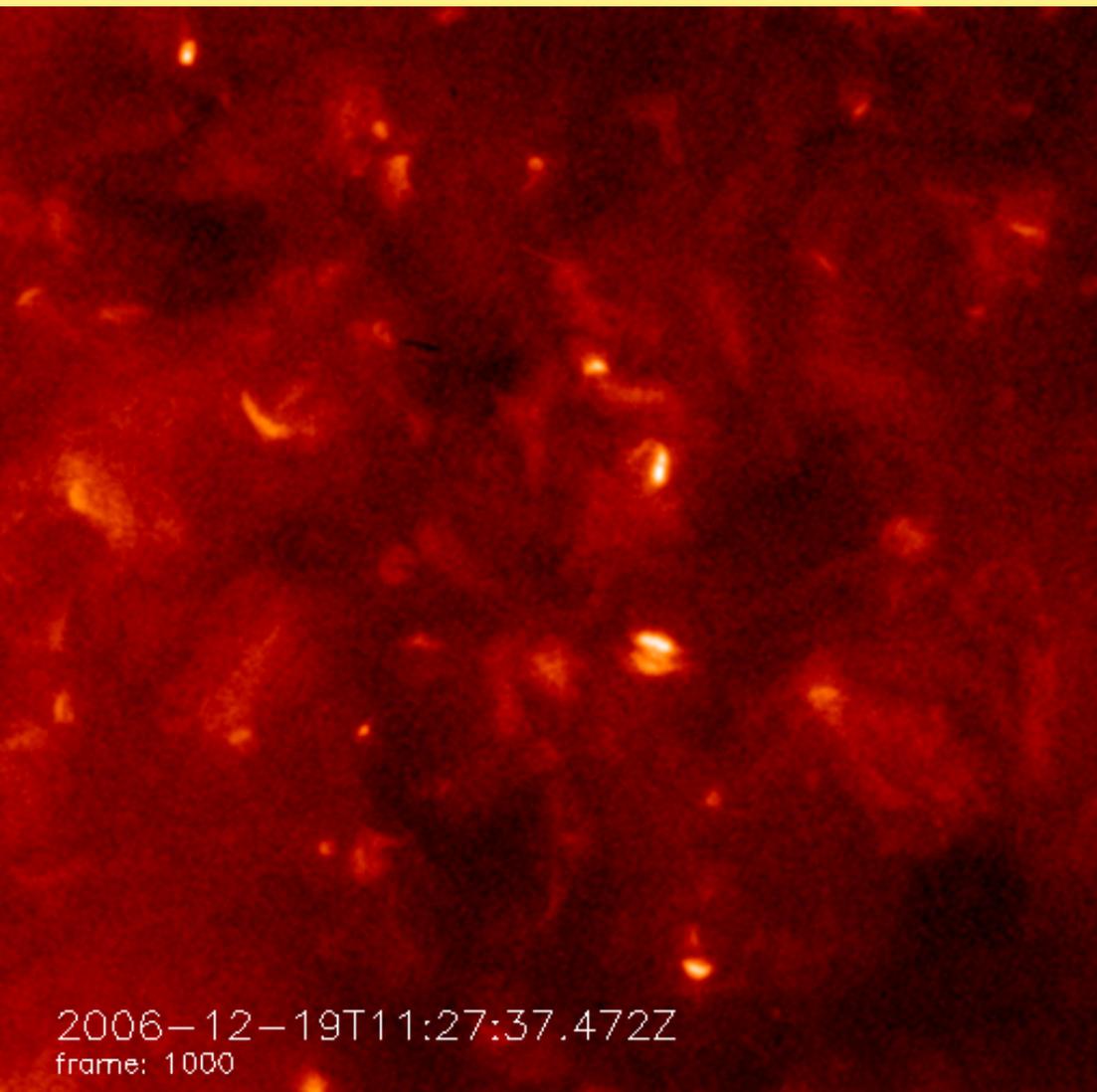
- Hinode --  
Chromospheric  
Spicules  
swaying

[Hansteen, Suematsu

--?? Solar wind/  
coronal heating



# Reconnection - most likely in low corona



Quiet Sun:  
[XRT on Hinode]

Many brightenings

**X-ray bright points** -  
above emerging and/or  
cancelling fields  
in photosphere

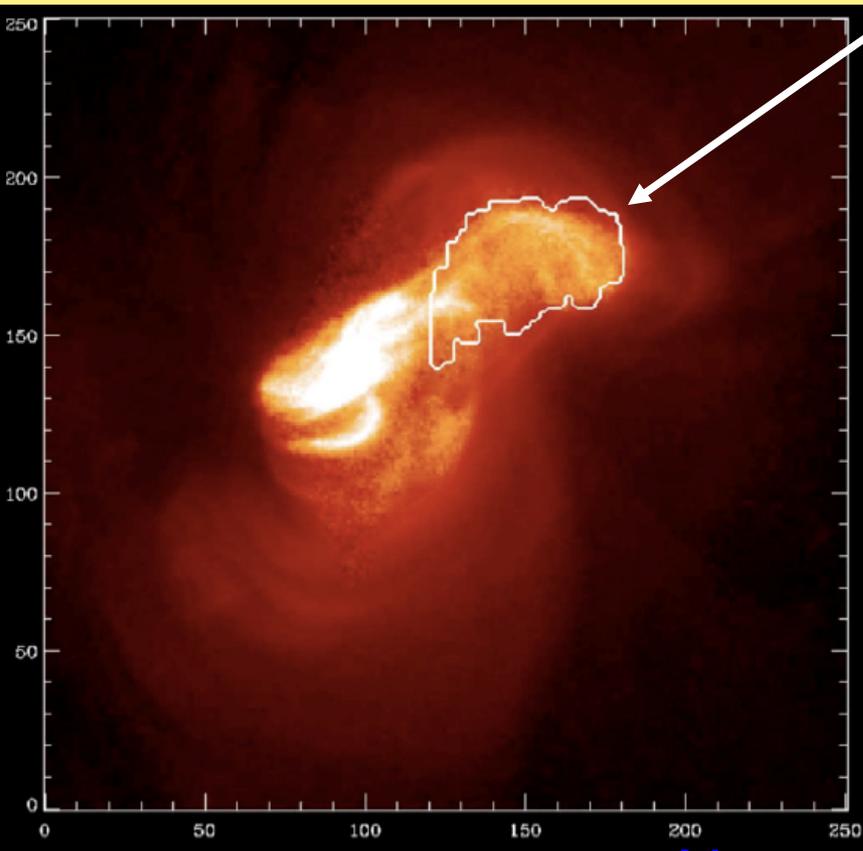
2006-12-19T11:27:37.472Z  
frame: 1000

[30-sec cadence, 12-hour duration]

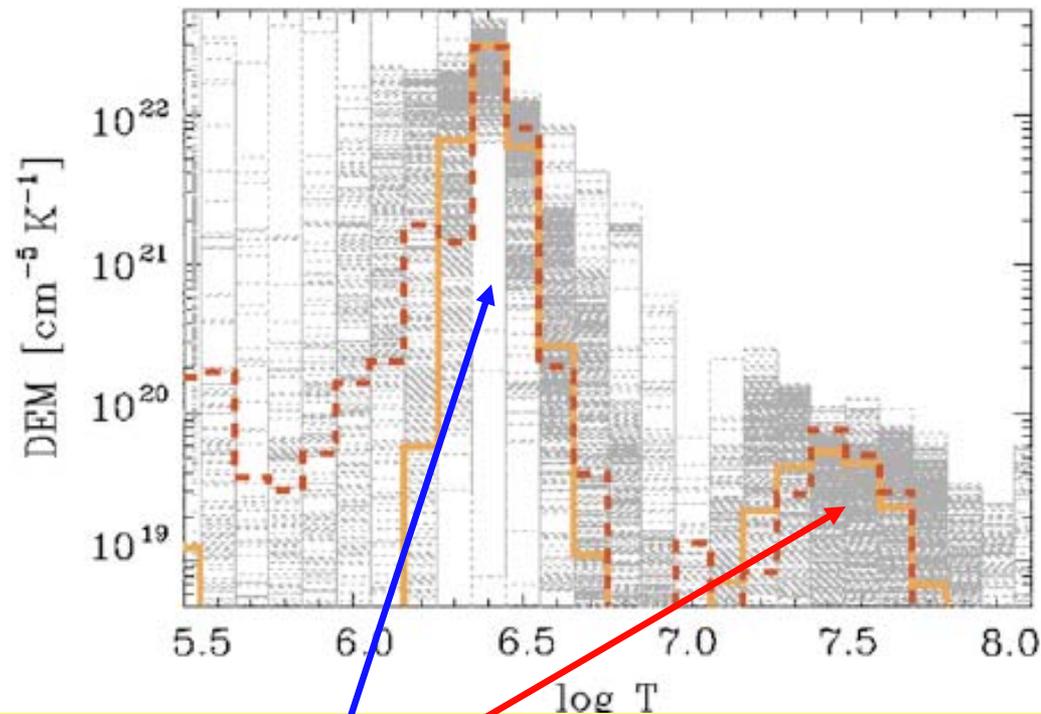
# Hinode XRT - active region

(Schmeltz et al, 2009; Reale et al, 2009)

## Observations inside white region



Differential emission measure

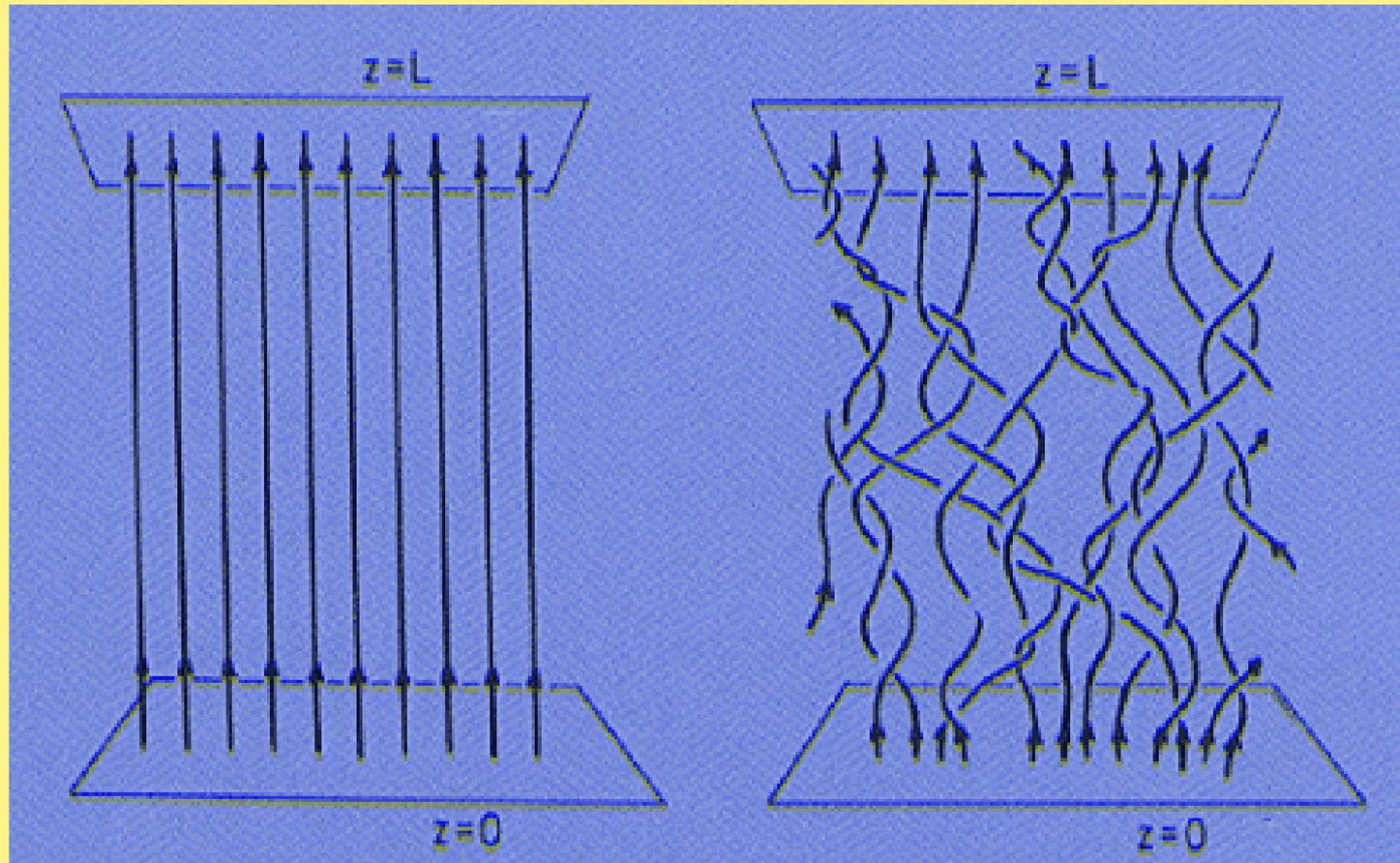


Normal active region emission at 3 MK

Plus emission (peak?) at 10-30 MK (?nanoflare

## 2. Coronal Heating Models

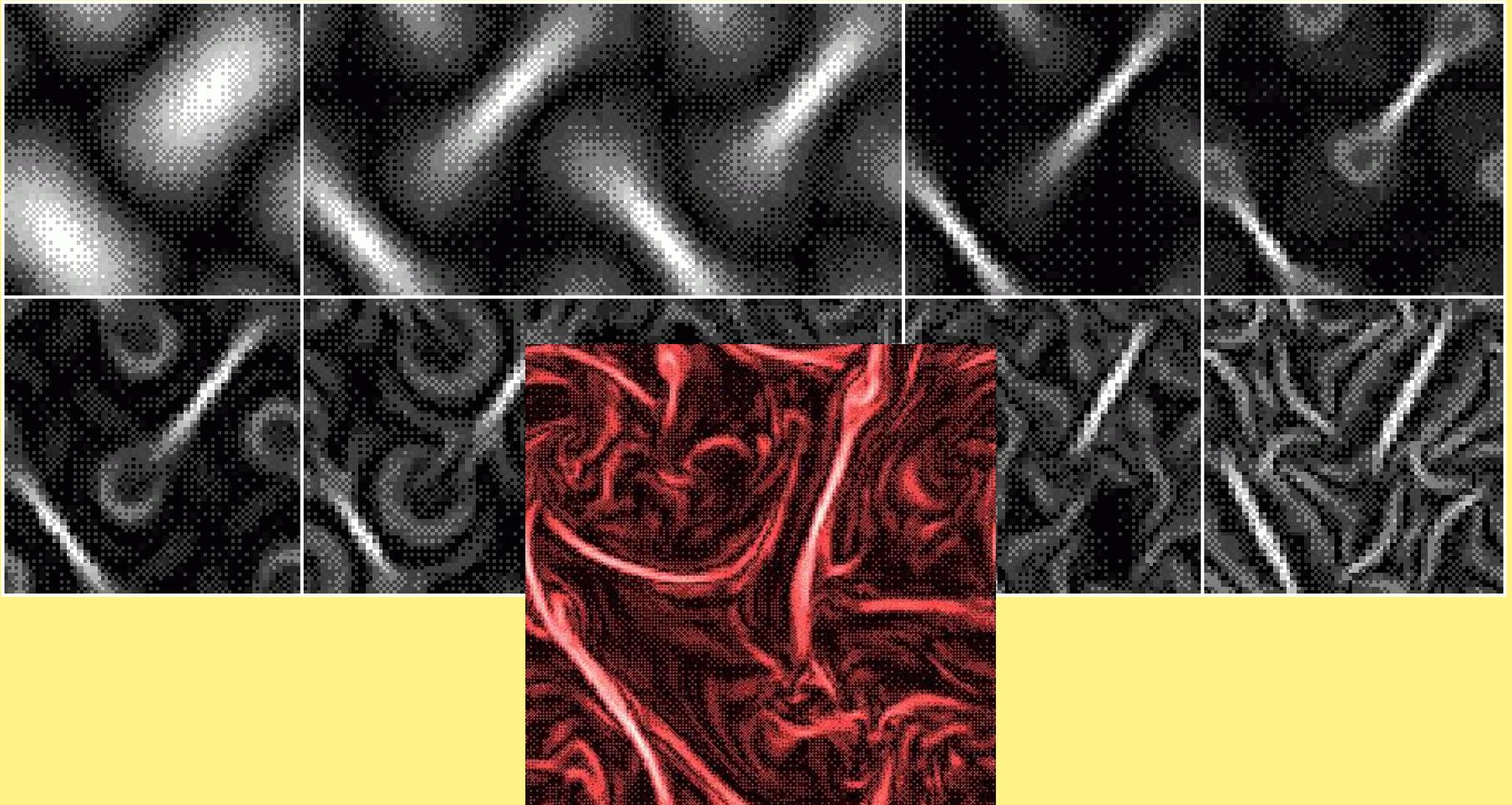
### Parker's classical Nanoflare Model by braiding (1972)



Initial B uniform / motions braiding

# Numerical Experiment (Galsgaard)

Braiding --> Current sheets grow --> turb. recon.



# Active Region as a Nonlinear Driven Dissipative System (Vlahos, 2008):

\* **Photospheric flux** elements: power-law distribution ( $N = F^{-1.85}$ )

[percolation model, Vlahos et al 1982]

Hinode + SOHO (Parnell 2009):

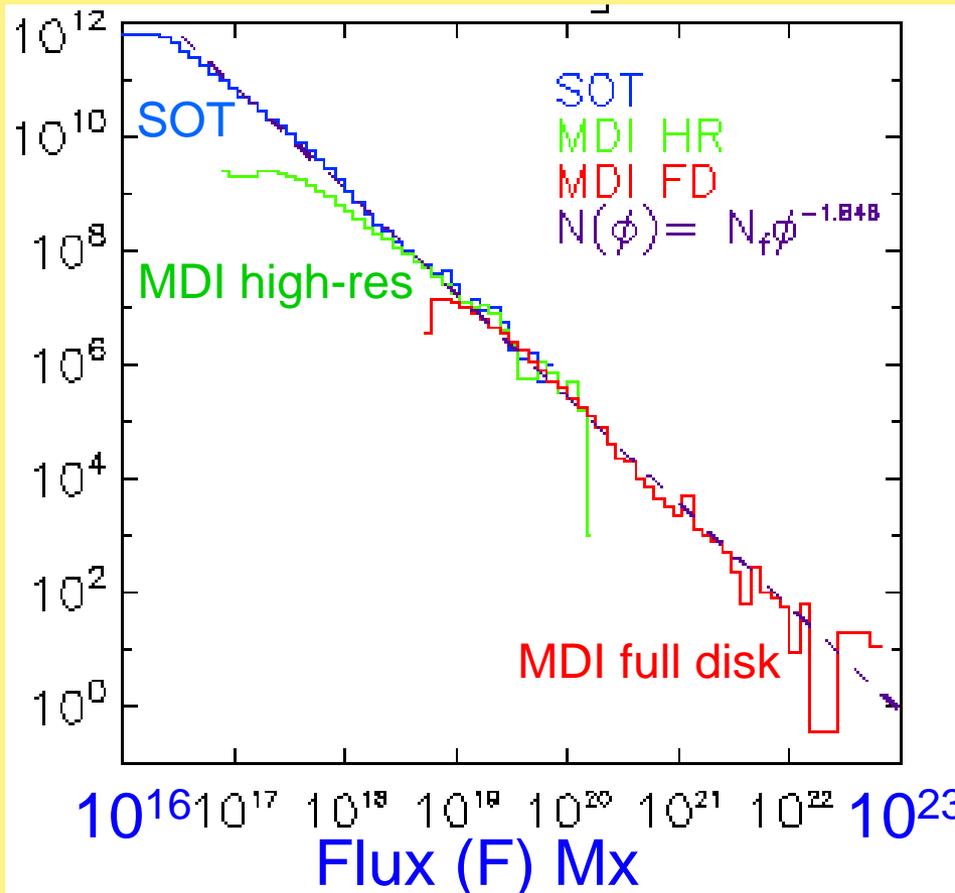
\* **In corona**, observed nanoflares have power-law distribution --

-- active region is in **SOC** (self-organised critical) state,

as current sheets form at all scales and reconnect.

\* --> **stochastic acceleration** of p'cles in fractal E's

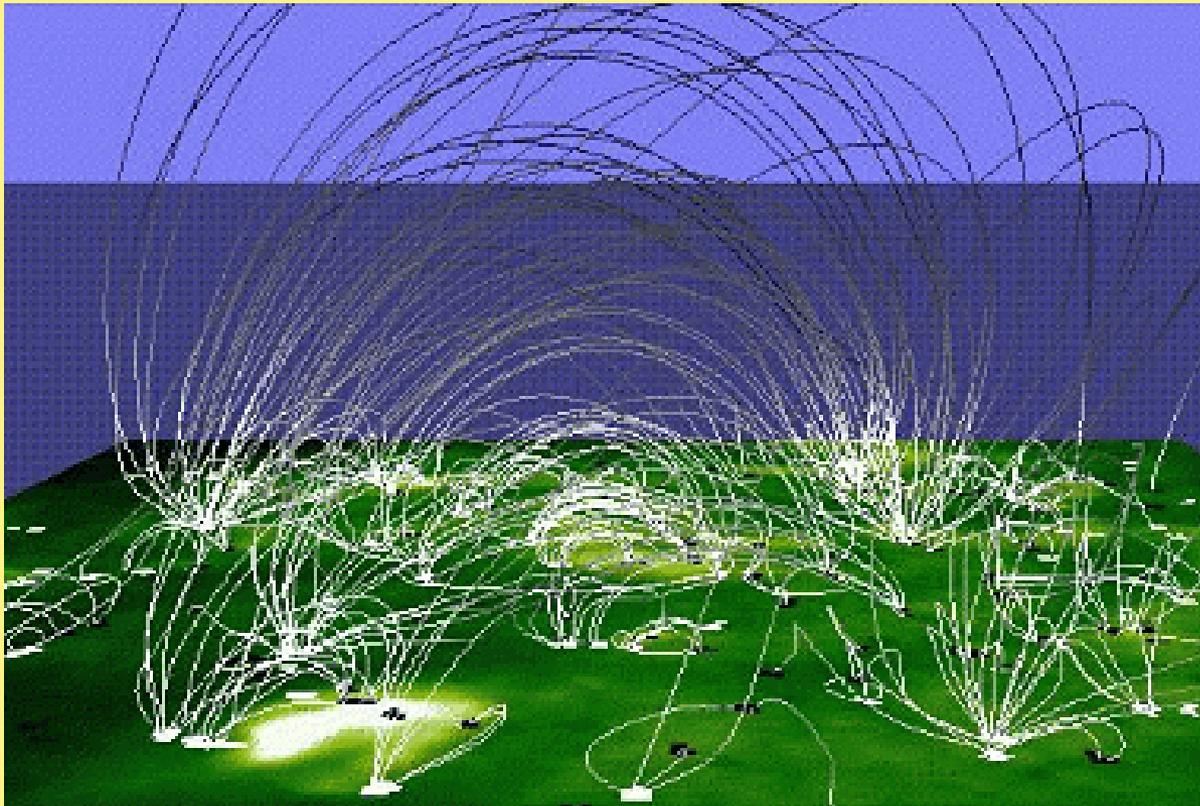
[Isliker et al, 1998; Isliker & Vlahos, 2003; Vlahos et al, 2004; Turkmani et al, 2006; Chapman, 1998..2009]



# 3. Coronal Tectonics Model

(development of Parker's model)

## 3.1 Effect “Magnetic Carpet”



Magnetic sources in surface are concentrated

# From observed magnetograms - construct coronal field lines

- each source connects to 8 others

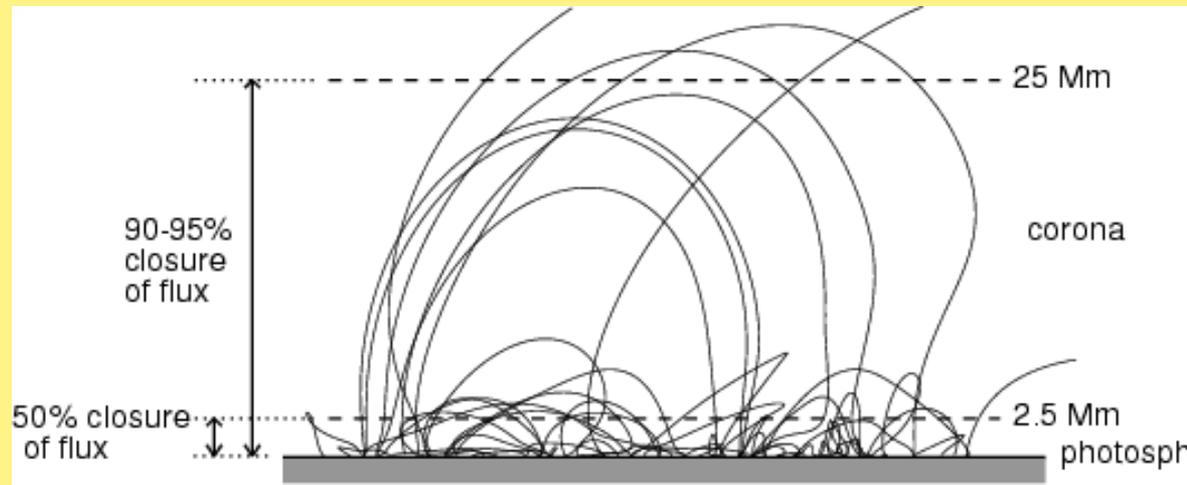
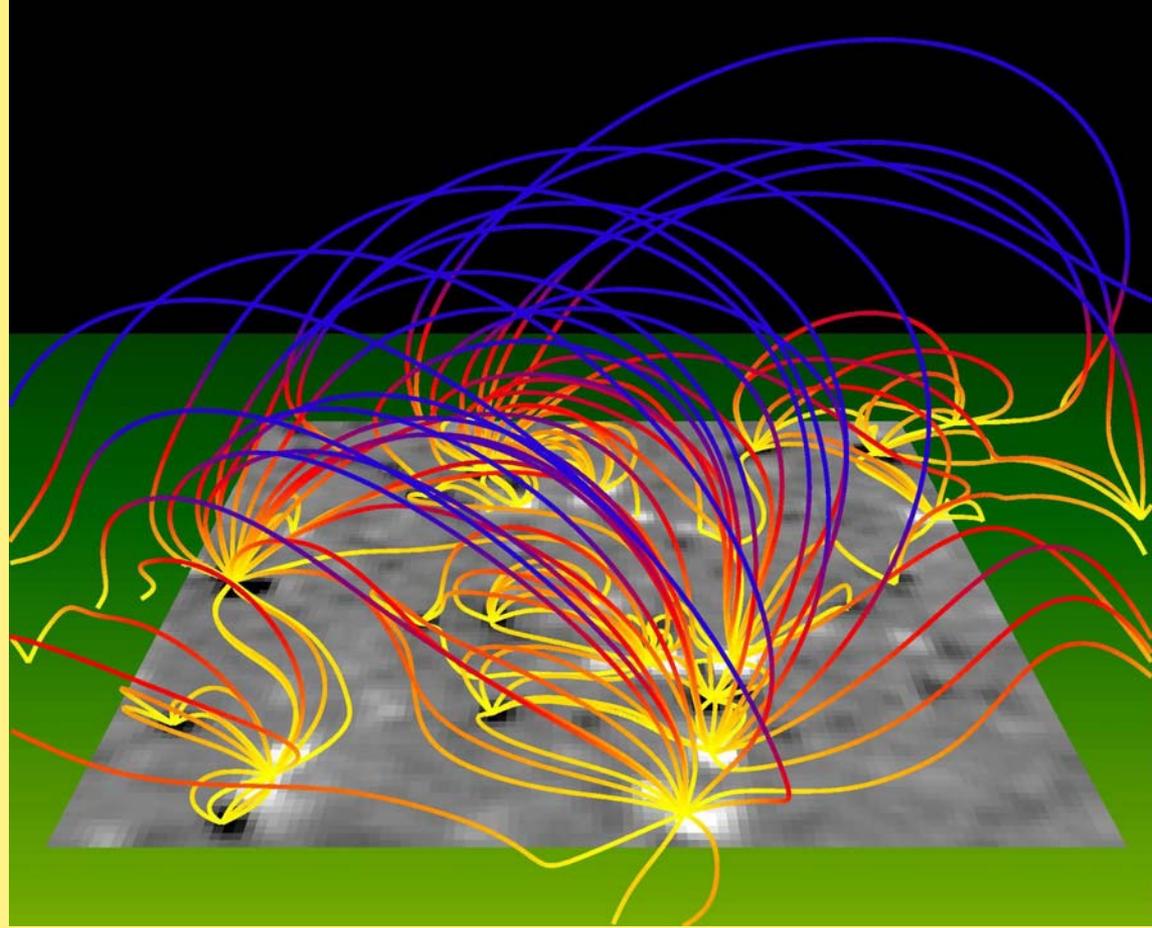
Time for all field lines to reconnect

**only 1.5 hours**

→ more complexity & heating low down  
(Close et al)

? describe structure

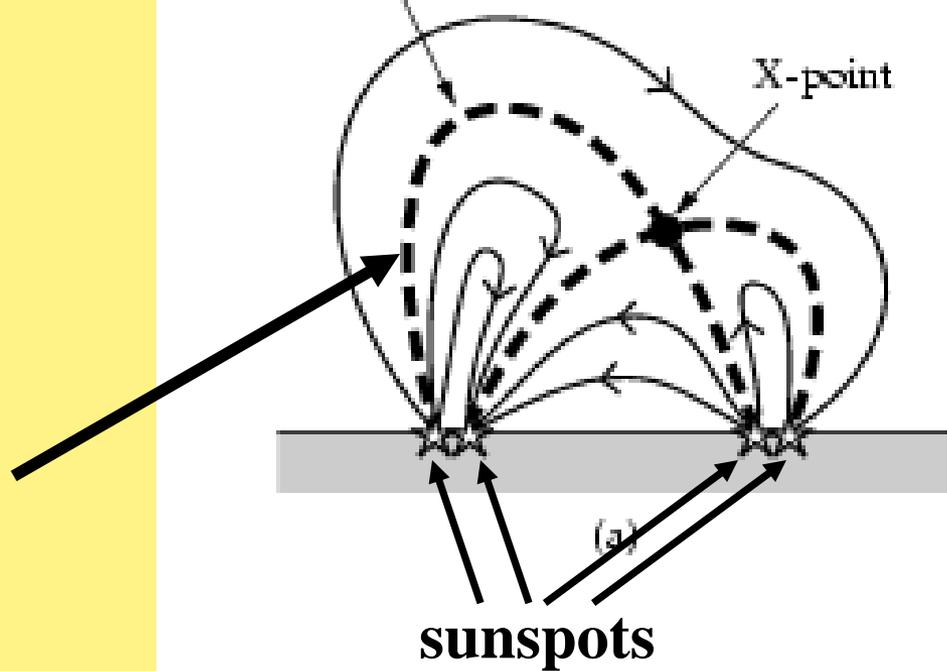
? nature of reconn<sup>n</sup>



# Topology of Coronal Fields - Complex

In 2D --

Separatrix curves



In 3D --

Separatrix surfaces

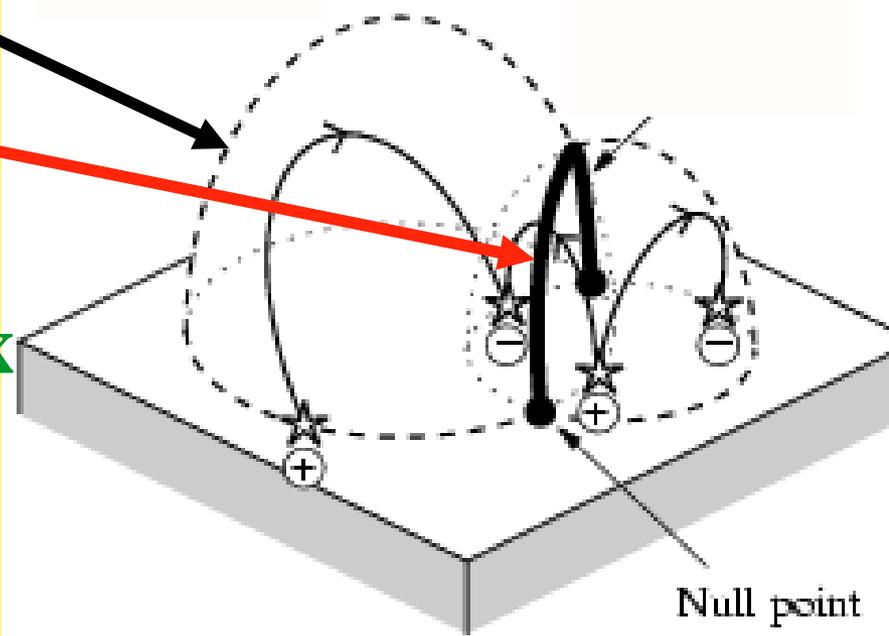
-- intersect in **Separator**

• **Reconnection can transfer flux**

In complex fields:

**SKELETON**--

set separatrices



# 3D RECONNECTION--

## Many New Features

- In 2D, reconnection at **null points**,  $B = 0$
- In 2D, magnetic lines slip through plasma --  
but change connections only at X

QuickTime™ and a  
YUV420 codec decompressor  
are needed to see this picture.

- In 3D, fieldlines **continually change connections** in

# 3D Reconnection

can occur

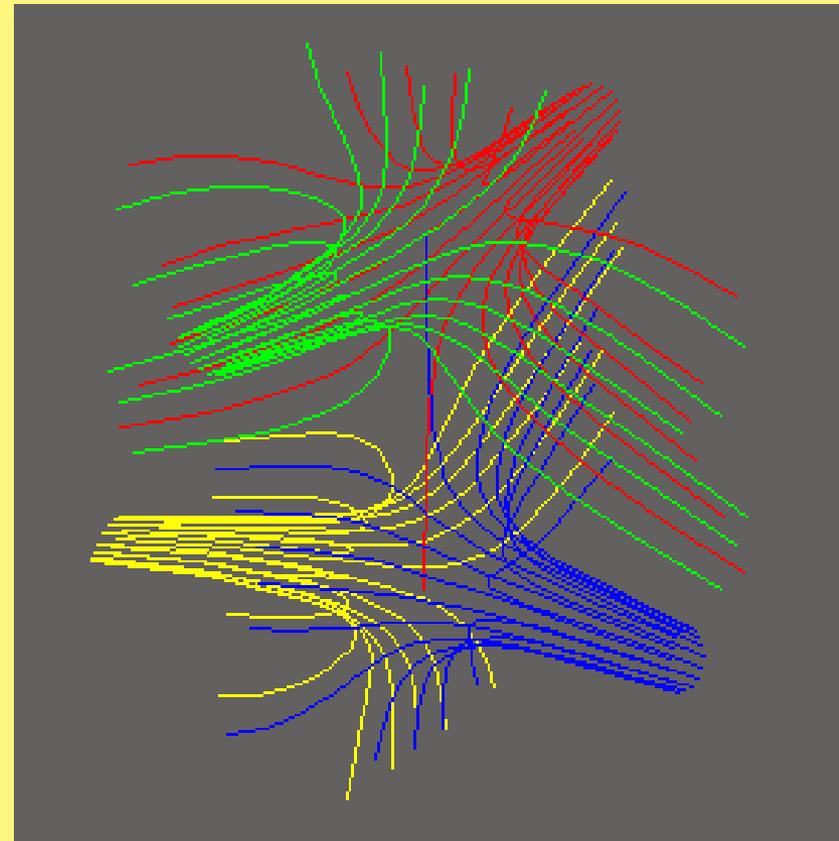
at a null point **or in absence of null (QSLs)**

**At Null -- 3 Types of Reconnection:**

**Spine** reconnection

**Fan** reconnection

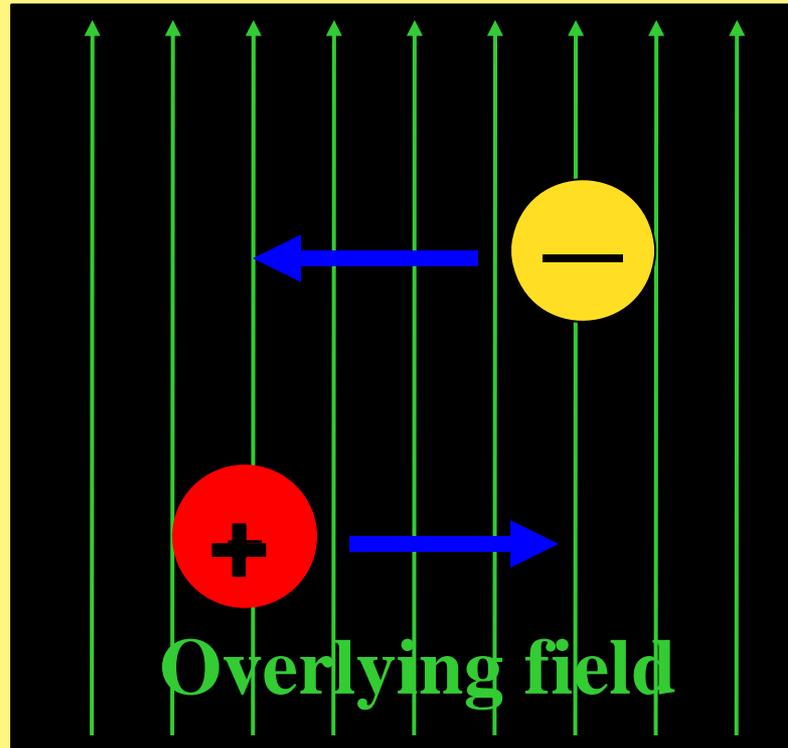
**Separator** reconnection



# Numerical Experiment:

## “Simple” binary interaction of 2 photosph<sup>c</sup> sources

[Haynes, Parnell, Galsgaard, Priest]

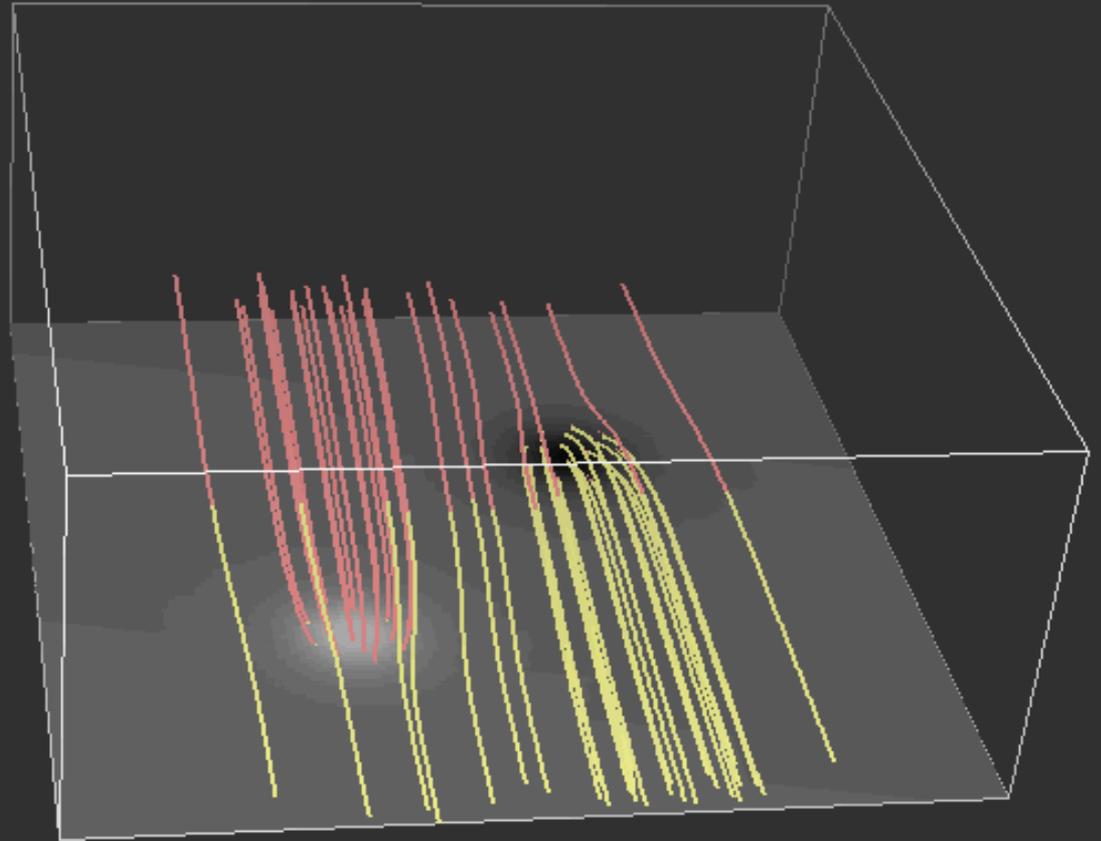


- Two source fragments (of opposite polarity).
- + Overlying field
- Sources pass by each other

Numerical  
experiment

**B-lines**

Current



How does reconnection occur ?

Nulls,  $\text{sep}^{\text{rs}}$ , nonnulls?

# Construct magnetic skeleton -- movie

- and + sources  
in overlying B.

→ Separatrix  
surfaces.

QuickTime™ and a  
YUV420 codec decompressor  
are needed to see this picture.

Move sources  
--> flux tube  
joining sources

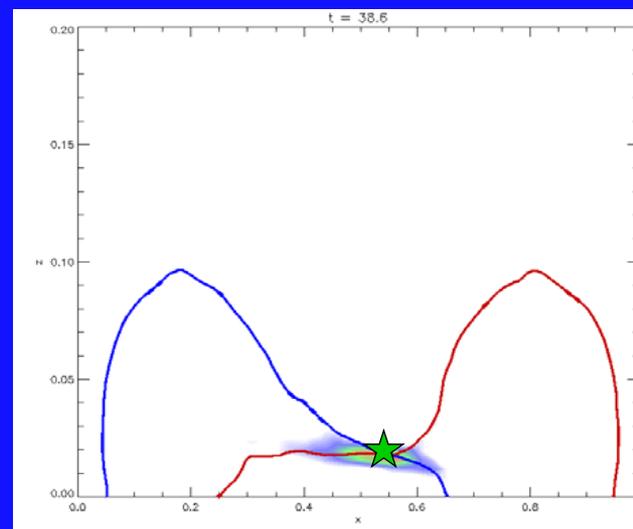
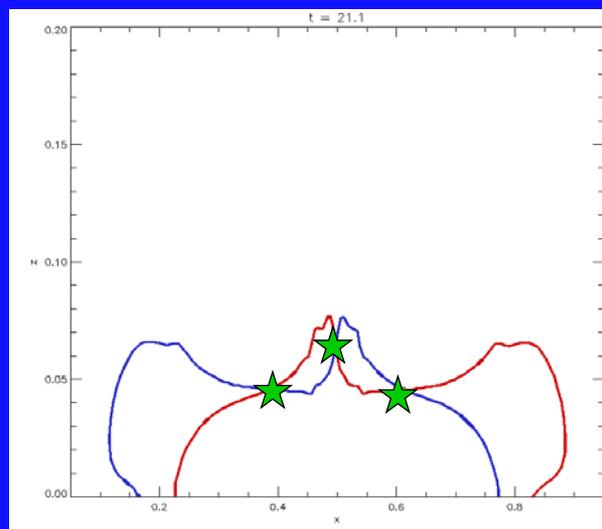
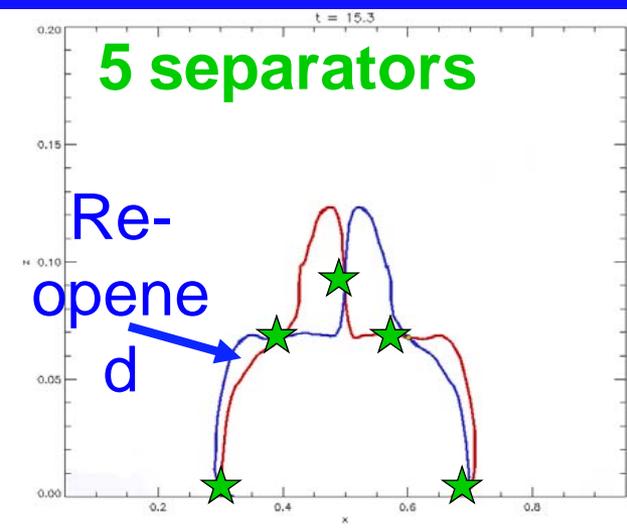
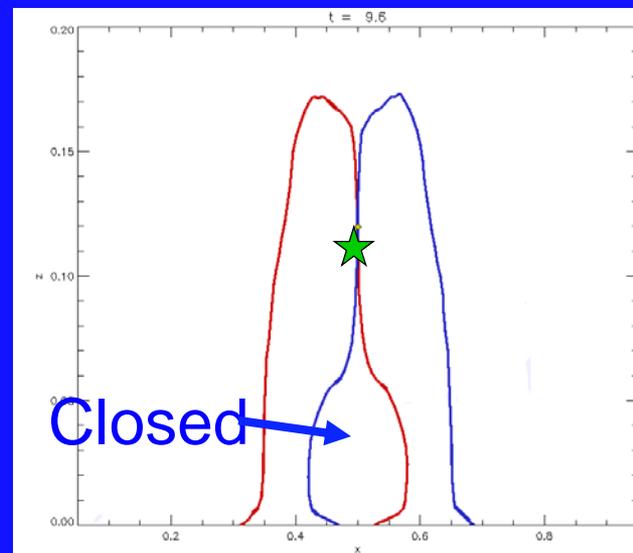
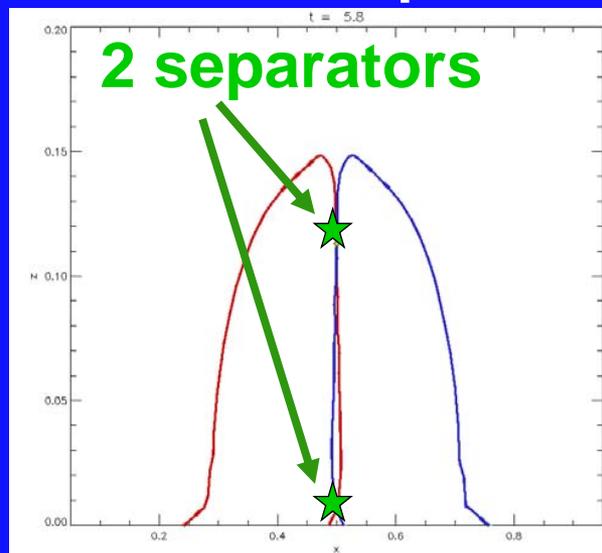
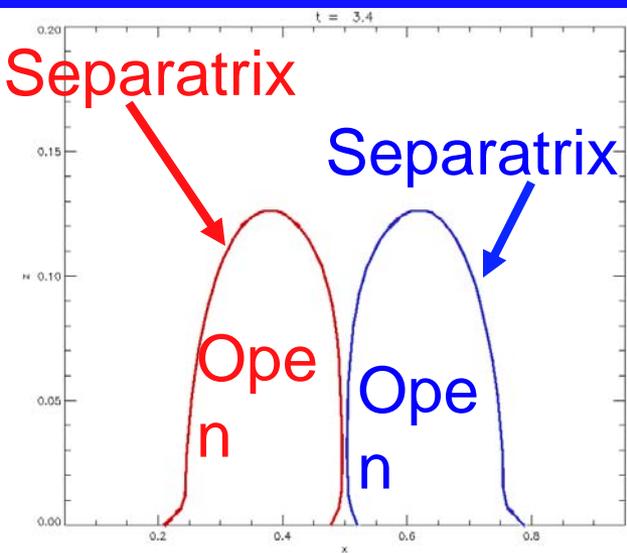


Separator

# Movie of vertical cut across skeleton

QuickTime™ and a  
YUV420 codec decompressor  
are needed to see this picture.

# Cross-sections of Separatrix Surfaces



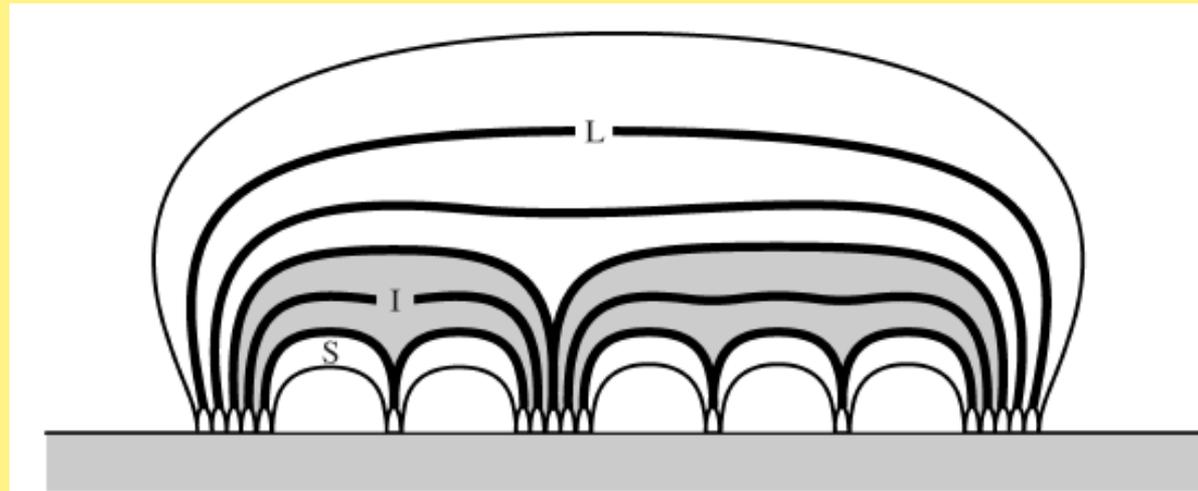
# Coronal Tectonics Model

(updated version of Parker nanoflare/topological dissipation)

[Priest, Heyvaerts & Title]

- Each "Loop" --> surface in many sources

- Flux from each source separated by separatrix surfaces



- As sources move

--> **J sheets on separatrices & separators**

--> Reconnect --> Heat

- **Corona filled w. myriads of J sheets, heating impulsively**

# Fundamental Flux Units

- **Intense tubes** (B -- 1200 G, 100 km,  $3 \times 10^{17}$  Mx)

- Single X-ray  
bright point --

**100 sources**

800 sep<sup>rs</sup>, 1600 sep<sup>ces</sup>

- Each TRACE  
Loop --

**10 finer loops**

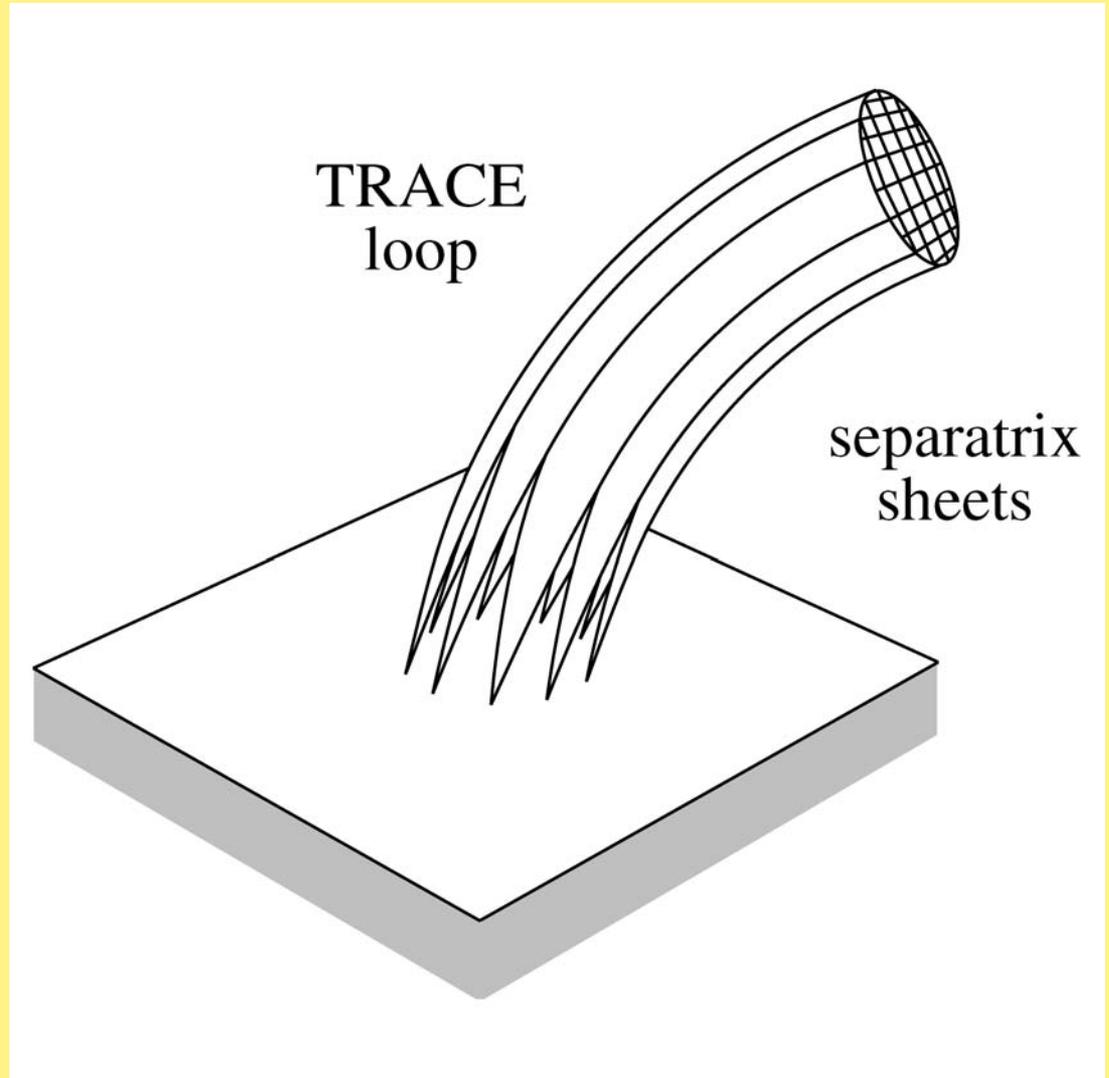
80 sep<sup>rs</sup>, 160 sep<sup>ces</sup>



# TRACE Loop

Reaches to surface in many footpoints.

**Separatrices form web in corona**



## 4. If reconnection heats corona at many sheets,

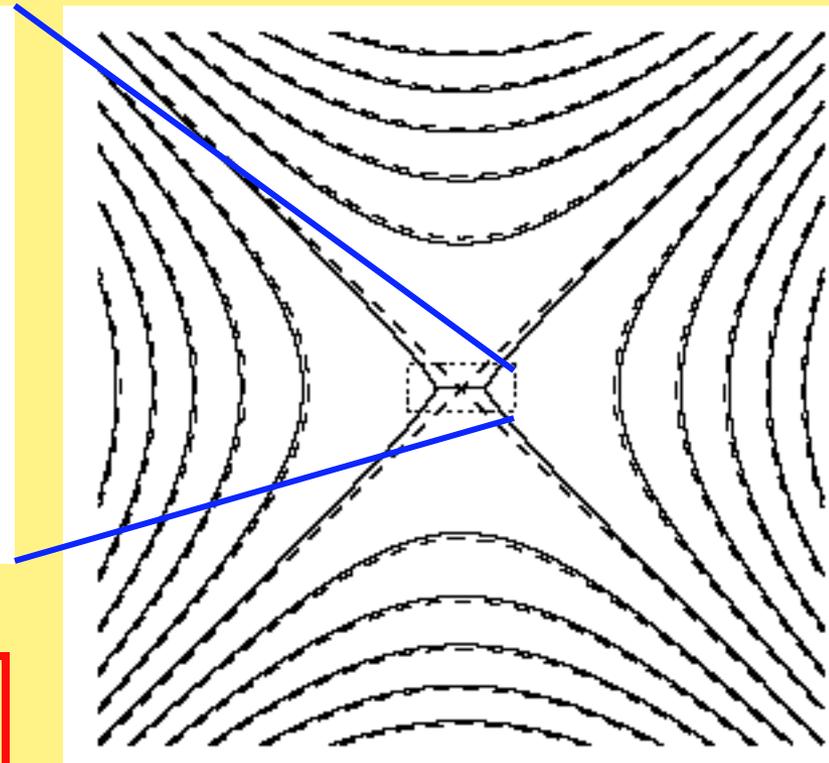
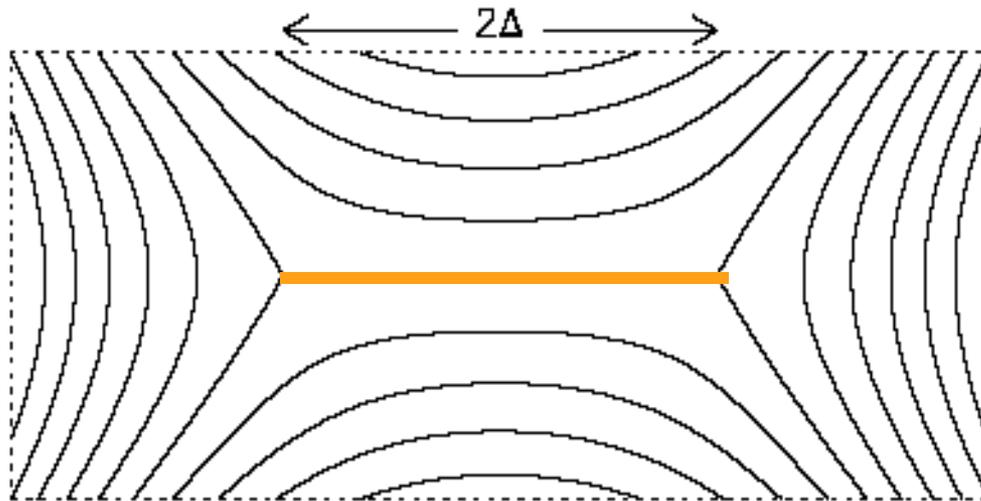
### 1. How does energy spread out ?

- conduction along B
- reconnection jets
- waves across B
- fast particles

### 2. If reconnection time-dependent, how much energy liberated locally/globally?

Simple model problem  
[Longcope & Priest]

# Magnetic field of Current Sheet in X



$$B_y + iB_x = B' \sqrt{w^2 - \Delta^2} = d\Psi / dw$$

At large  $r$ ,  $B = B_0 + B_1$

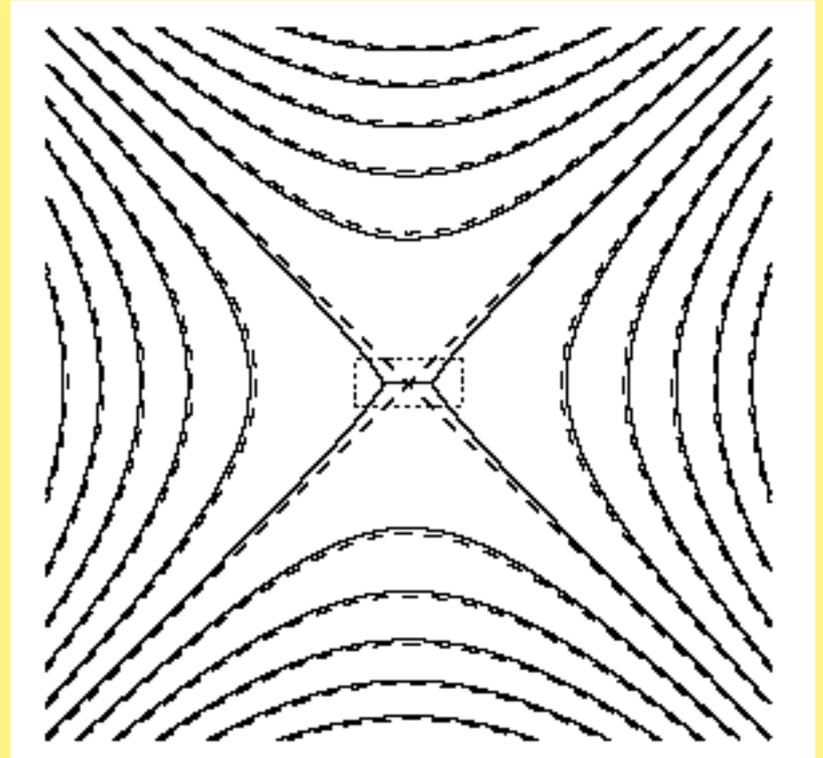
$$B_0 = -B' [y \hat{x} + x \hat{y}], \quad B_{1\phi} = \frac{I_0}{2\pi r} \text{ (line current),} \quad \omega_A = \frac{B'}{\sqrt{4\pi\rho}}$$

Lots of energy far from CS

# Suppose sheet reconnects

Current ( $I$ ) dissipates

Local process but has  
global consequences:



Decrease  $I$  -->  $\mathbf{B}$  must change at large distances

How ??

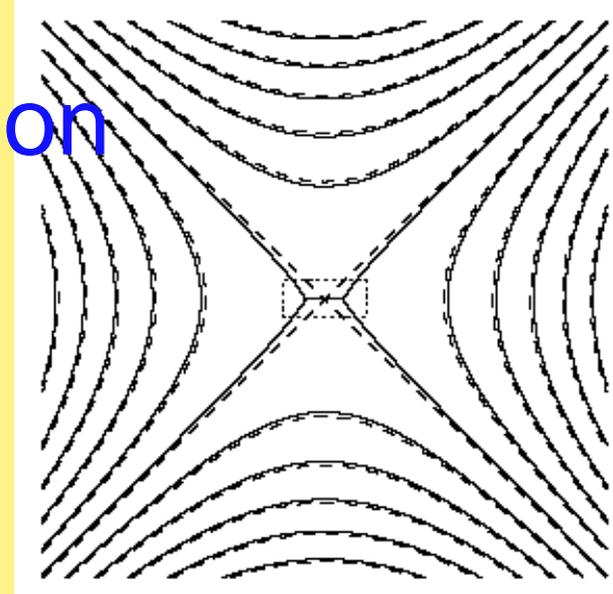
# Model for effect of reconnection

Linearize about X-point  $\mathbf{B}_0$  :

$$\frac{\partial \mathbf{B}_1}{\partial t} = \nabla \times (\mathbf{v}_1 \times \mathbf{B}_0) + \eta \nabla^2 \mathbf{B}_1,$$

$$\rho_0 \frac{\partial \mathbf{v}_1}{\partial t} = \mathbf{j}_1 \times \mathbf{B}_0.$$

$$\mathbf{B}_0 = -B'[y\hat{\mathbf{x}} + x\hat{\mathbf{y}}]$$



Assume  $B_1$  @  $t=0$  is due to current sheet

$\eta$  is “turned on”

current diffuses  
i.e. reconnection

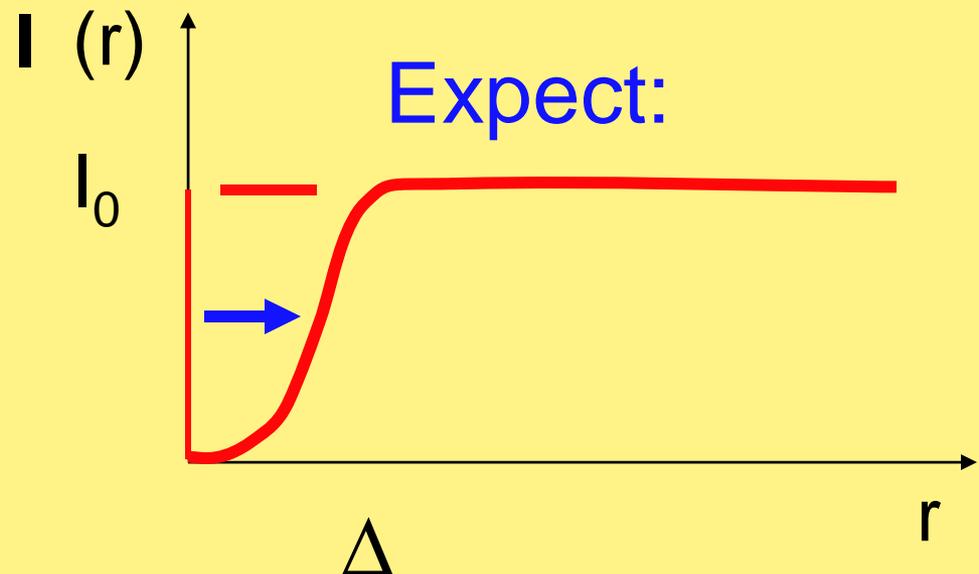
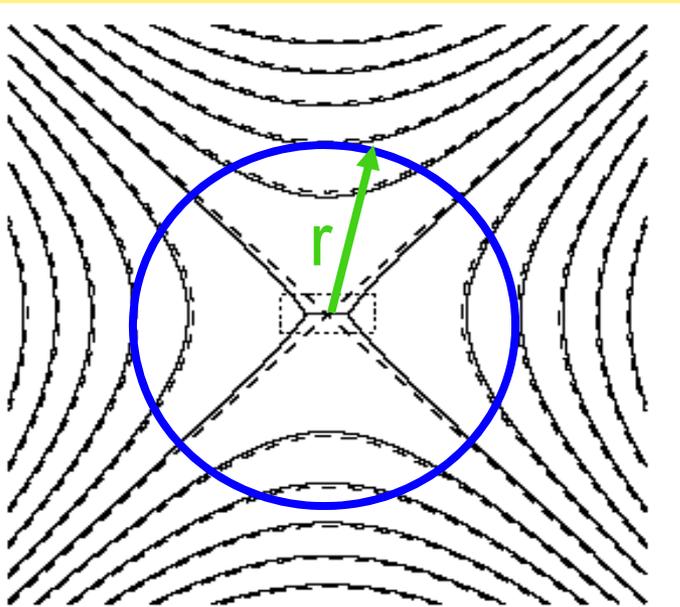
# Combine equations:

Put  $rB_{1\phi} = I(r, t)$  = twice current enclosed in  $r$

$$\frac{\partial^2 I}{\partial t^2} = \omega_A^2 r \frac{\partial}{\partial r} \left( r \frac{\partial I}{\partial r} \right) + \eta r \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial^2 I}{\partial r \partial t} \right)$$

wave

diffusion



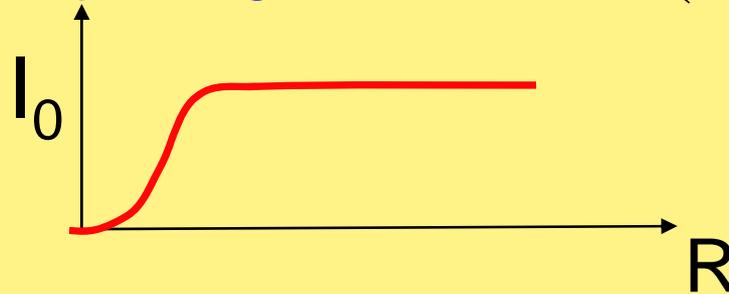
~~$$\frac{\partial^2 I}{\partial t^2} = \omega_A^2 r \frac{\partial}{\partial r} \left( r \frac{\partial I}{\partial r} \right) + \eta r \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial^2 I}{\partial r \partial t} \right)$$~~

wave

diffusion

(i) Large  $r$  (wave) limit: when  $R = \ln(r / \ell_\eta) \gg 1$

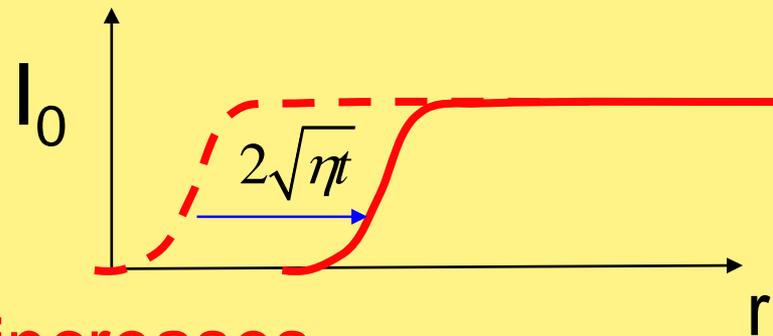
$$I(R,t) = I_0 - F(t-R)$$



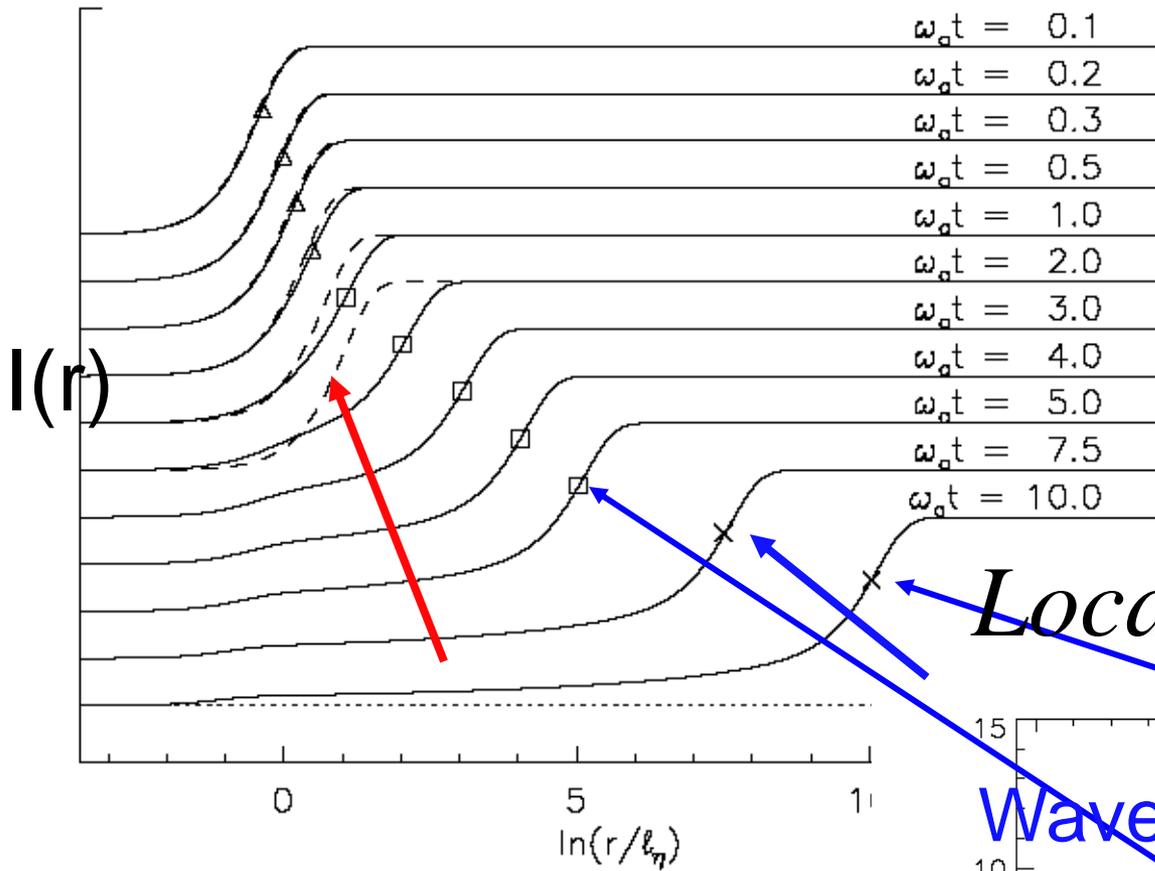
$$\ell_\eta = \sqrt{\frac{\eta}{\omega_A}}$$

(ii) Small  $r$  (diffusive) limit:

$$I(r,t) = I_0 - I_0 \exp\left(-\frac{r^2}{4\eta t}\right)$$



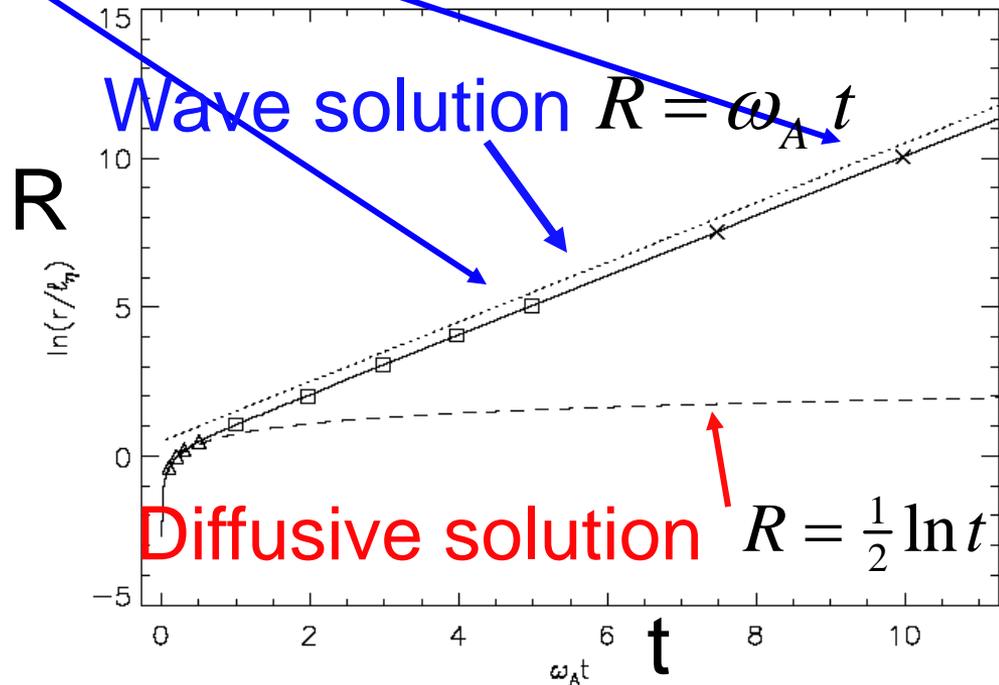
**NB**  $j = \frac{1}{r} \frac{\partial I}{\partial r} \rightarrow 0$  at origin as  $t$  increases



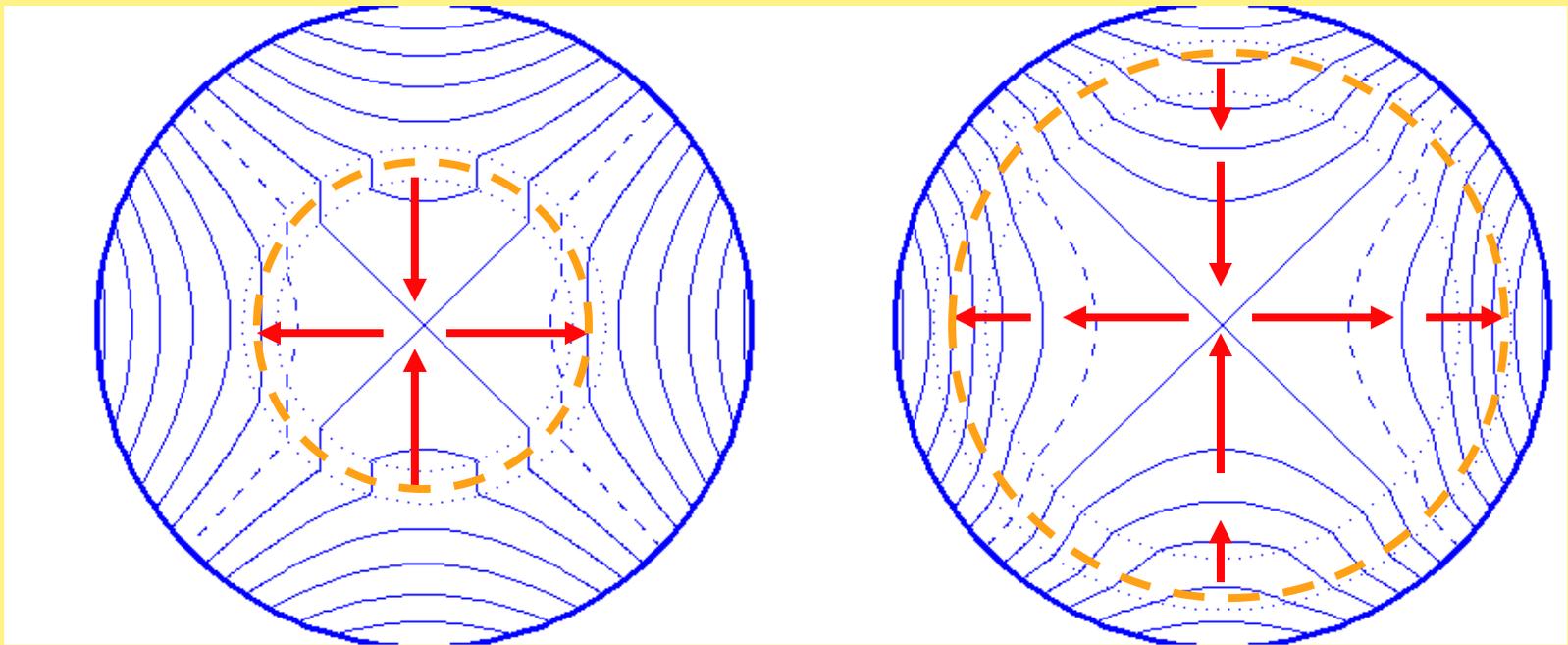
# Numerical Solution

Location where  $I = \frac{2}{3} I_0$

Transition:  
diffusive to  
wave solution

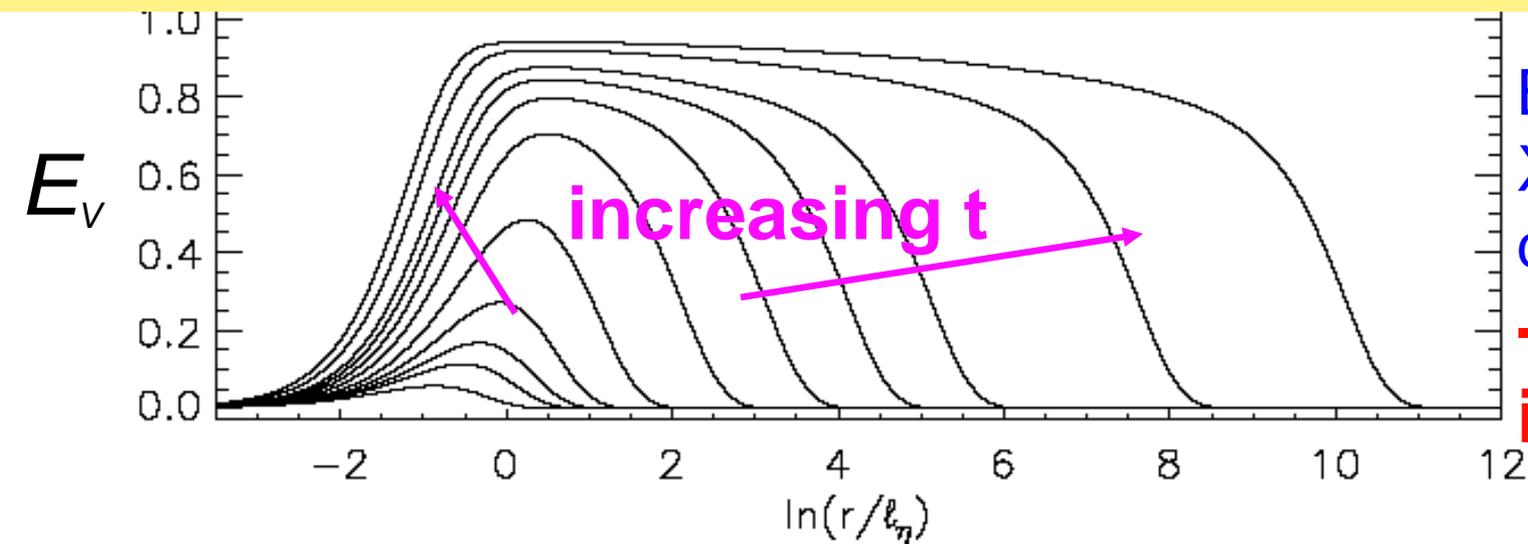


# Sheath of Current propagates out



In wake of sheath a flow, assoc<sup>d</sup> with

$$E_V(r, t) \hat{\mathbf{z}} = -\mathbf{v}_1 \times \mathbf{B}_0$$



But flow near X does not disappear  
-- it slowly increases !

# Resolving the Paradox - 3rd regime

At large  $t$  (i.e.,  $t > 1/\omega_A$ )

$$\cancel{\frac{\partial^2 I}{\partial t^2}} = \omega_A^2 r \frac{\partial}{\partial r} \left( r \frac{\partial I}{\partial r} \right) + \eta r \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial^2 I}{\partial r \partial t} \right)$$

Advection = diffusion

$$I(r, t) = \frac{I_0}{2\omega_A t} \left[ 1 - \exp\left(-\frac{\omega_A^2 r^2 t}{\eta}\right) \right]$$

$$j = \frac{1}{r} \frac{\partial I}{\partial r} = \frac{I_0 \omega_A}{\eta} \exp\left(-\frac{\omega_A^2 r^2 t}{\eta}\right)$$
$$= \frac{I_0 \omega_A}{\eta} \quad \text{at} \quad r = 0$$

**Peak in  $j$  remains at  $X$   
and  
produces a steady  $E$   
(indep of  $\eta$ )  
i.e. fast reconnection**

# 5. Summary

- **3D Reconnection** v. diff. from 2D
  - **Coronal heating** model in complementary ways:
    - as self-organised critical state
    - by coronal tectonics model
      - updated version of Parker braiding
  - Response to enhanced  $\eta$  in current sheet (CS):  
magnetic energy --> K.E. in wave -- later dissipate.
  - **But Dennis - prophet** - far ahead of time
- need revolution**, based on his ideas, to fully understand corona  
w. coupling micro <--> macro

