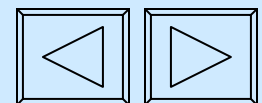


Magnetic topologies: where will reconnection occur ?

Magnetic reconnection :
an attractive mechanism for **energy release** in the corona
(heating, flares, CMEs ...)

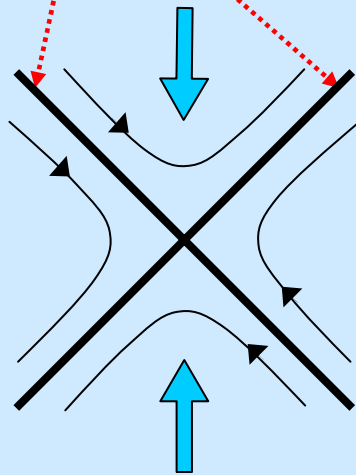
How to quantify this in 3D configurations ?

Pascal Démoulin

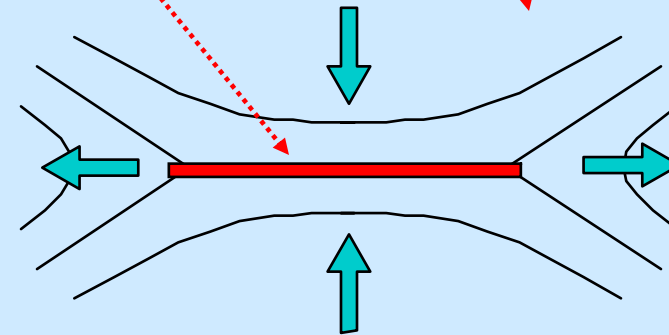
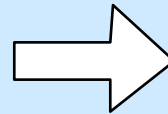


Separatrices in 2D => current sheet => reconnection

Magnetic
null point

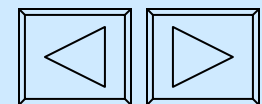


External forcing



externally driven flows

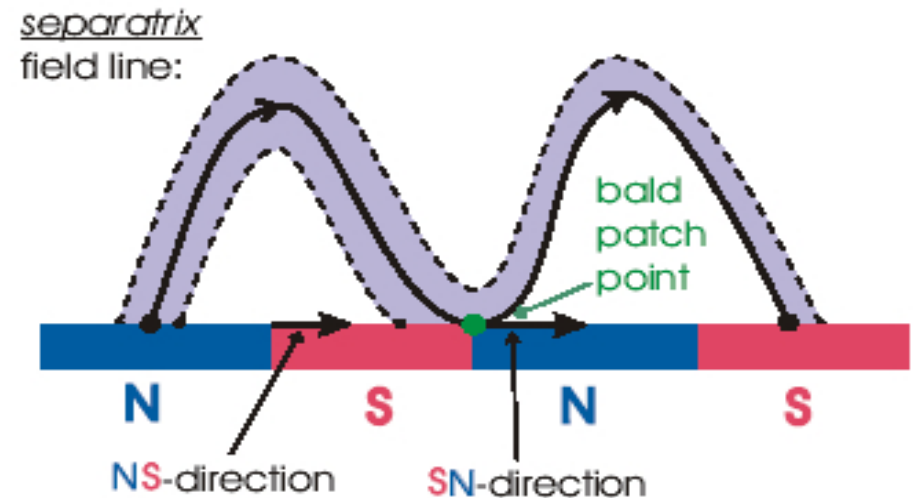
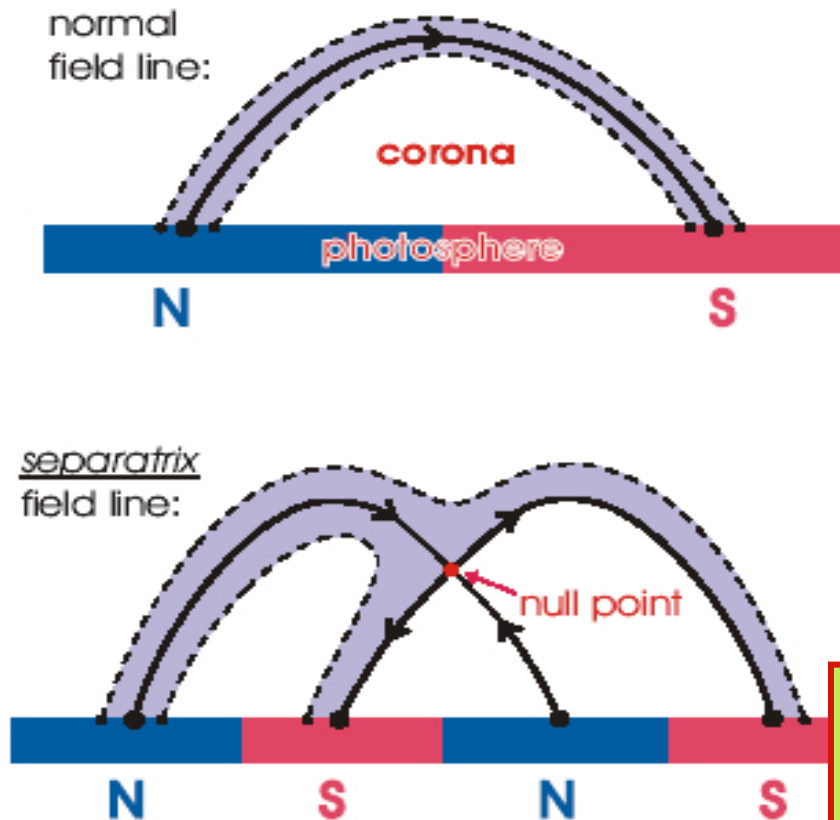
(Parker, Sonnerup, Sweet, Syrovatskii)



Separatrices in 2D and 2.5D cases => reconnection

Basic magnetic topologies for $\vec{B}(x, y)$

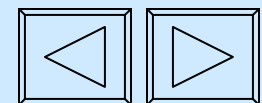
field-line connectivity \rightarrow topology



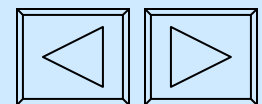
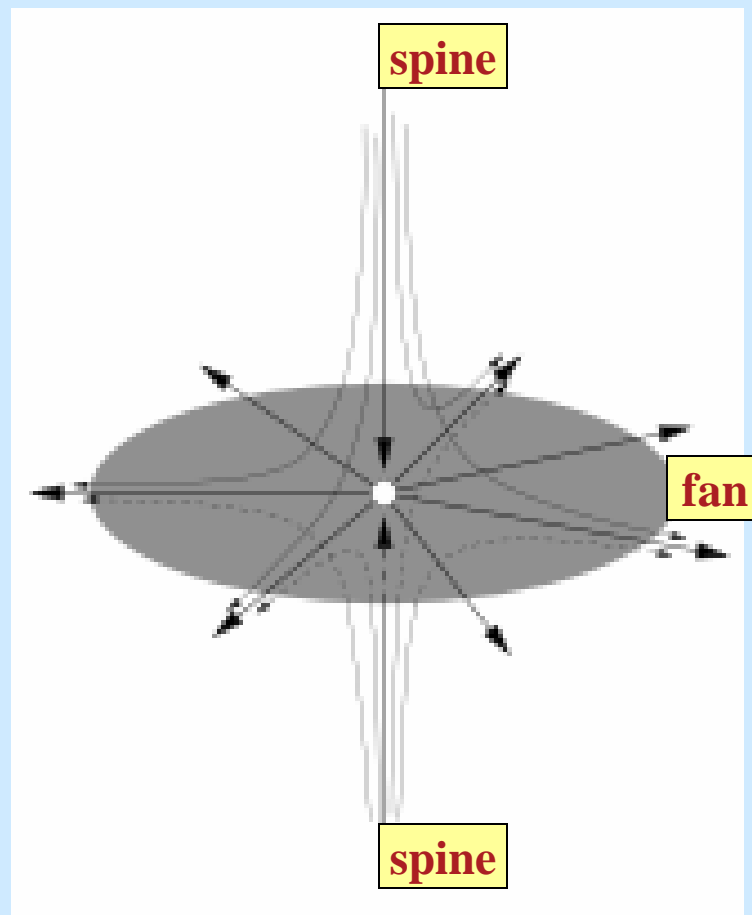
Boundary motions or internal instability

=> **current sheet formation** on the separatrices

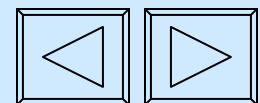
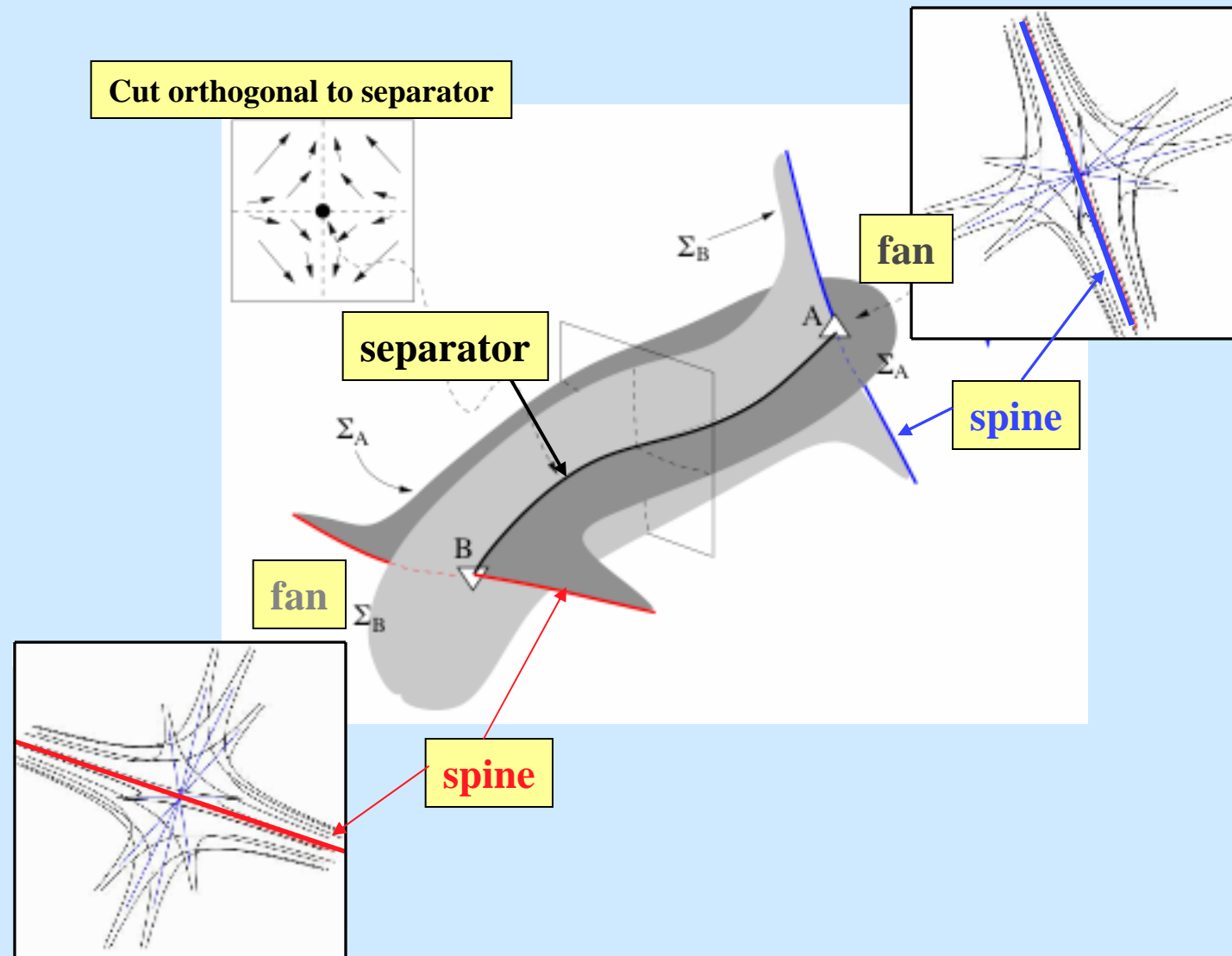
=> **magnetic reconnection** (with finite resistivity)



Magnetic topology around a null point



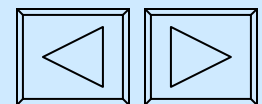
Magnetic topology with 2 null points



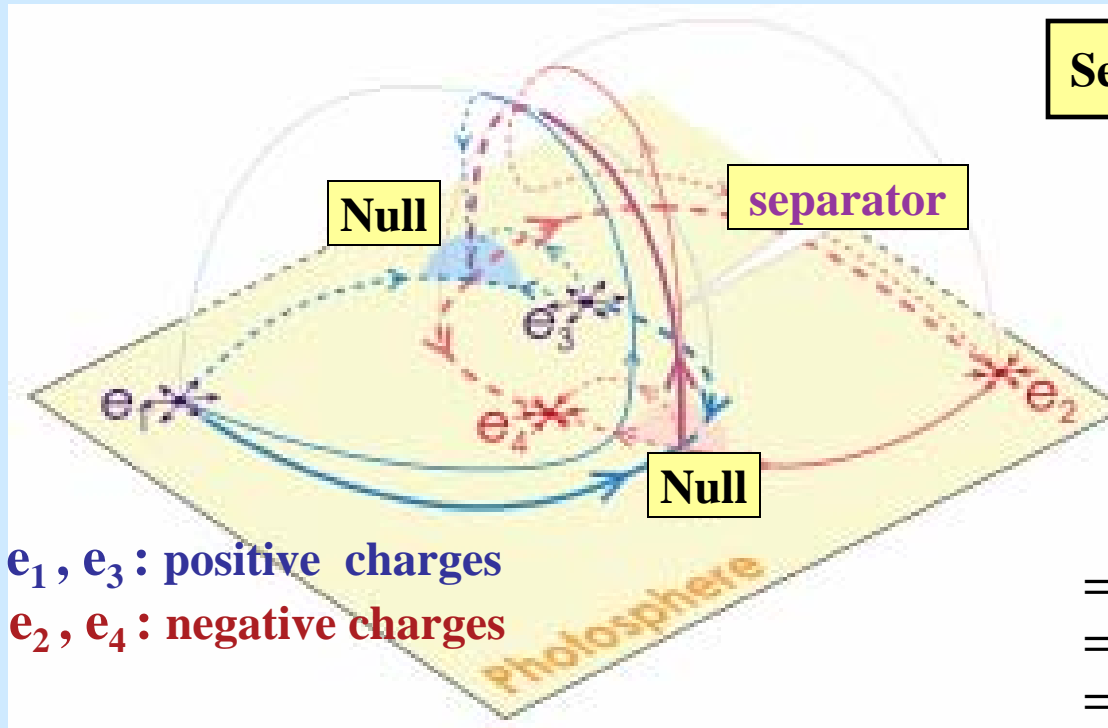
Next :

The magnetic field is described with **photospheric magnetic charges**

This models the concentration in **very thin flux tubes**



Configuration with 4 magnetic charges

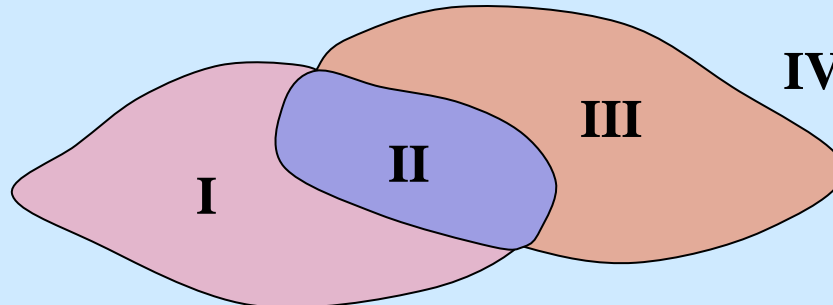


e_1, e_3 : positive charges
 e_2, e_4 : negative charges

Separatrices: 2 intersecting cupola

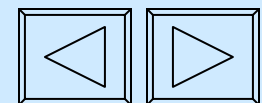
Motion of the charges

- => Current sheet at separator
- => Reconnection (with $E_{||}$)
- => Flux exchange between domains



4 connectivity domains

(Sweet 1969, Baum & Brathenel 1980,
Gorbachev & Somov 1988, Lau 1993)



Main properties

Skeleton :

Null points + spines + fans + separators

“summary of the magnetic topology”

(Molodenskii & Syrovatskii 1977, Priest et al. 1997,
Welsch & Longcope 1999, Longcope & Klapper 2002)

Classification of possible skeletons (with 3 & 4 magnetic charges)

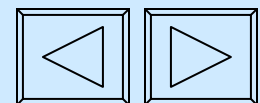
(Beveridge et al. 2002, Pontin et al. 2003, 1980,
Gorbachev & Somov 1988, Lau 1993)

Global bifurcations :

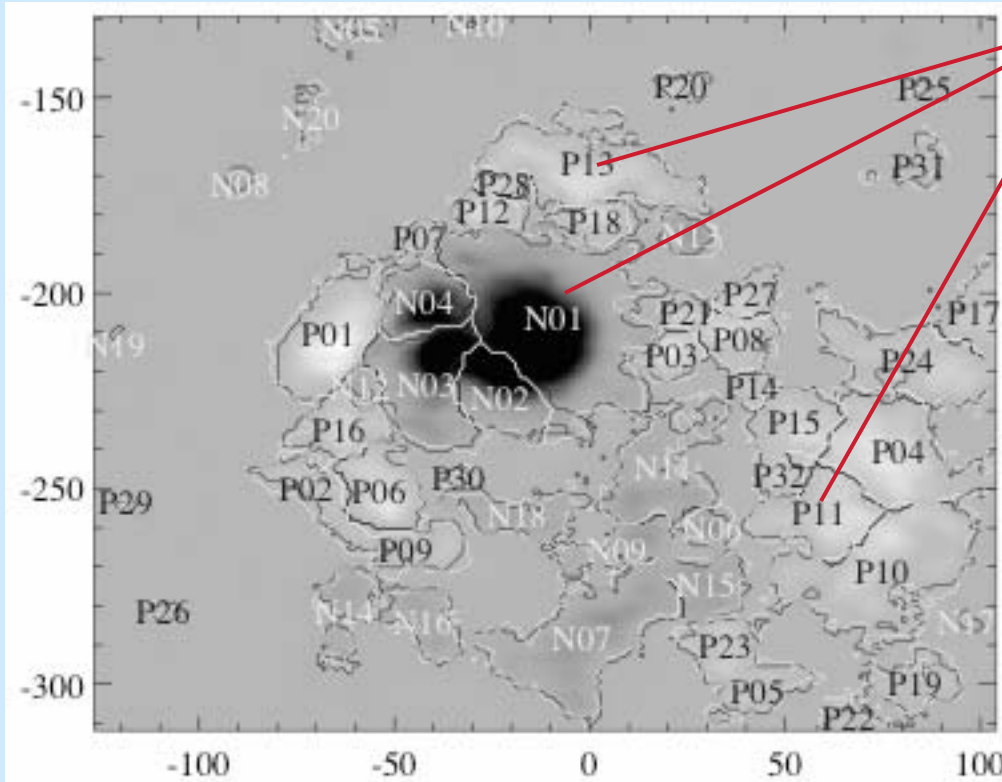
They modify the number of domains

- separator bifurcation (2 fans meet)
- spine-fan bifurcation (fan + spine meet)

(Gorbachev et al. 1988,
Brown & Priest 1999, Maclean et al. 2004)



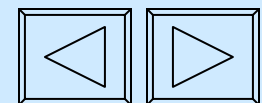
Magnetic charge topology for an AR (I)



Partition of the magnetogram
in flux regions

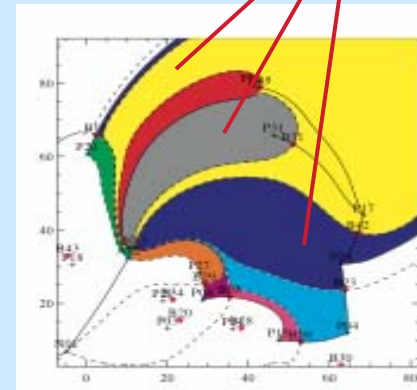
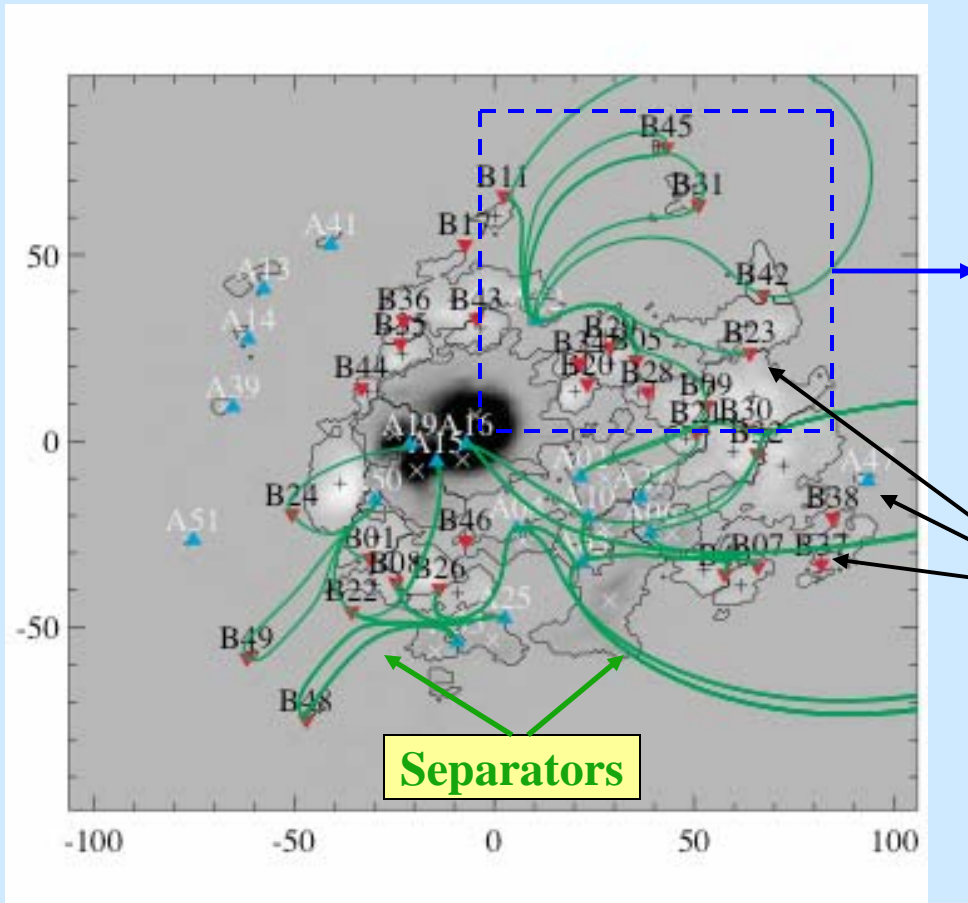
Then, **replace** the flux regions
with magnetic charges with same flux

(Mandrini et al. 1991, 1993,
Démoulin et al. 1992, 1994,
Longcope & Silva 1998)



Magnetic charge topology for an AR (II)

Connectivity domains



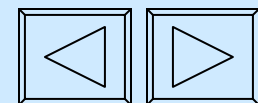
Photospheric nulls ▲ ▼

Suppose no flux outside magnetic charges

(Barnes et al. 2005)

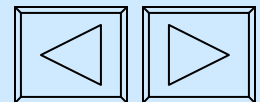
Charge evolution: build up of currents at separators

(Longcope et al. 2001, 2005)



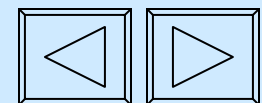
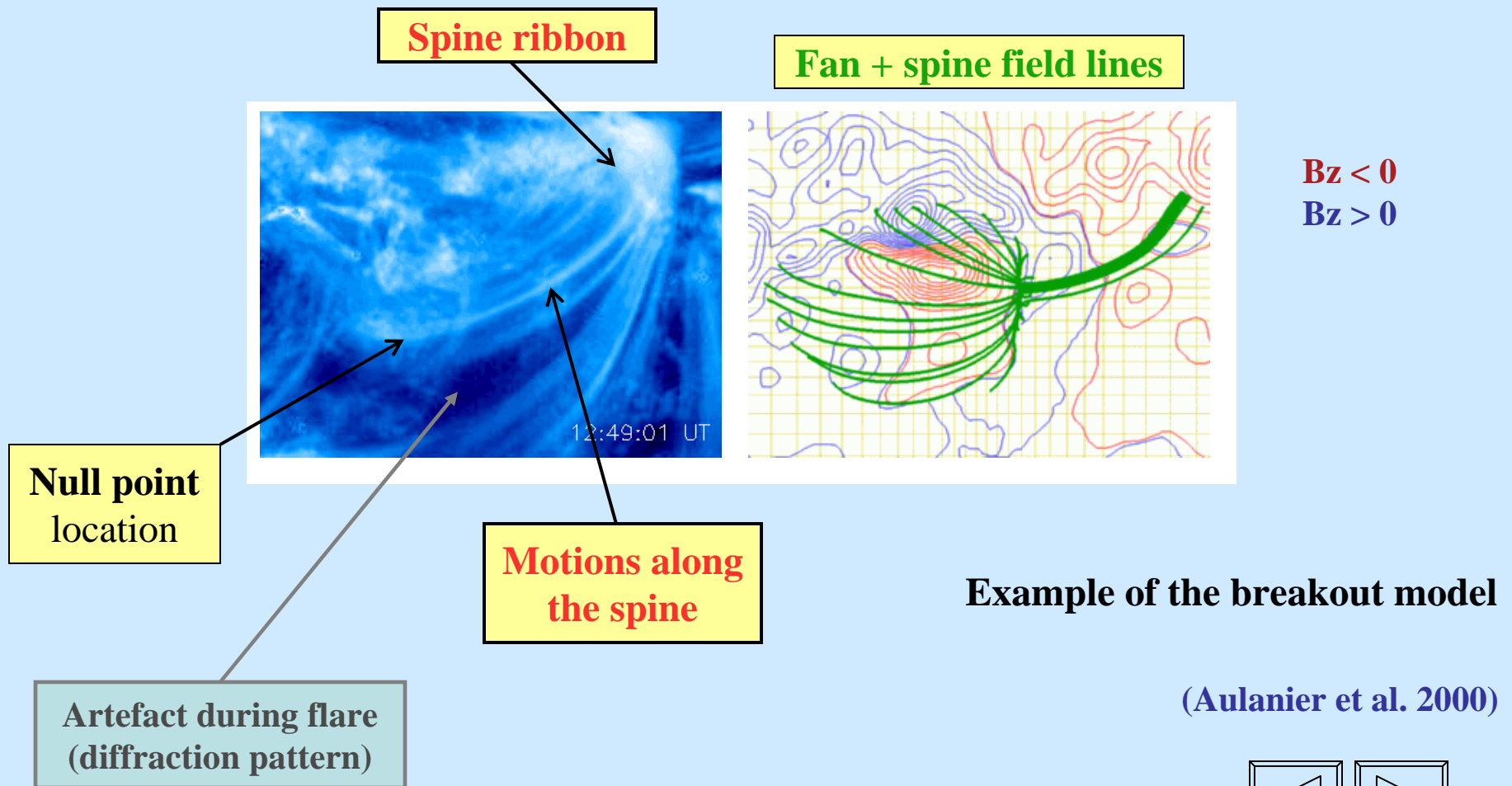
Next :

Magnetic topology properties which **do not need
a description of the magnetic field with **magnetic charges**
(or large flux-free photospheric regions)**



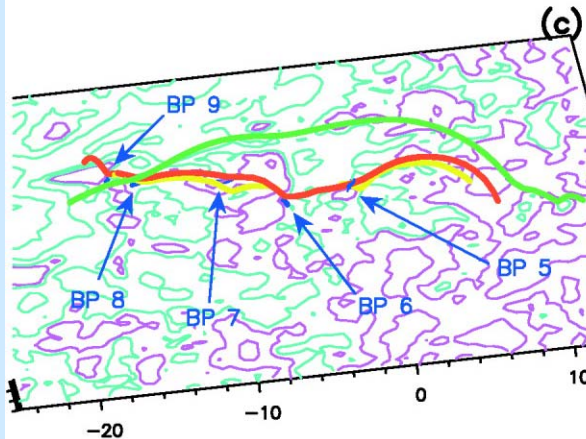
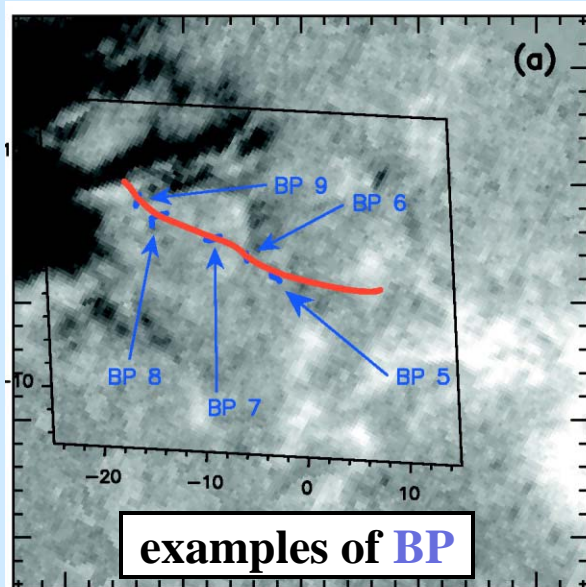
Coronal magnetic null points

Bastille day flare: **eruptive flare** within a complex magnetic topology:
reconnection at the **coronal** null point triggers a CME



Magnetic bald patches (BP)

Magnetic **dips** at the photospheric level



Below the photosphere: Parker instability

=> undulatory flux tubes

=> **Dips** with **dense plasma** in the emerging flux tubes

=> Flux tubes **cannot emerge** further

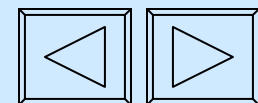
Association: BP <-> Ellerman bomb

(signature of energy release)

Reconnection at BP separatrices
needed for further emergence

(the dense dipped part is left behind)

(Pariat et al. 2005)



Coronal nulls & Bald Patches in observations

Coronal nulls :

Above mixed field: **rare** & density **decreases rapidly** with height (0.05 height^{-3})

(Schrijver & Title 2002, Longcope et al. 2003)

Associated with some flares

(Mandrini et al. 1991, Gaizauskas et al. 1999, Aulanier et al. 2000)

Bald Patches separatrices :

Associated with:

- some flares
- some UV brightenings
- some chromospheric events

(Aulanier et al. 1998)

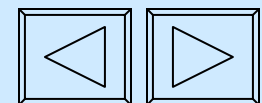
(Fletcher et al. 2001)

(Mandrini et al. 2002, Pariat et al. 2005)

BUT many flare ribbons and loops are **NOT** related
to **Bald Patch** and **Null Points** separatrices

(Démoulin et al. 1994, ...)

=> Reconnection must occur in broader conditions



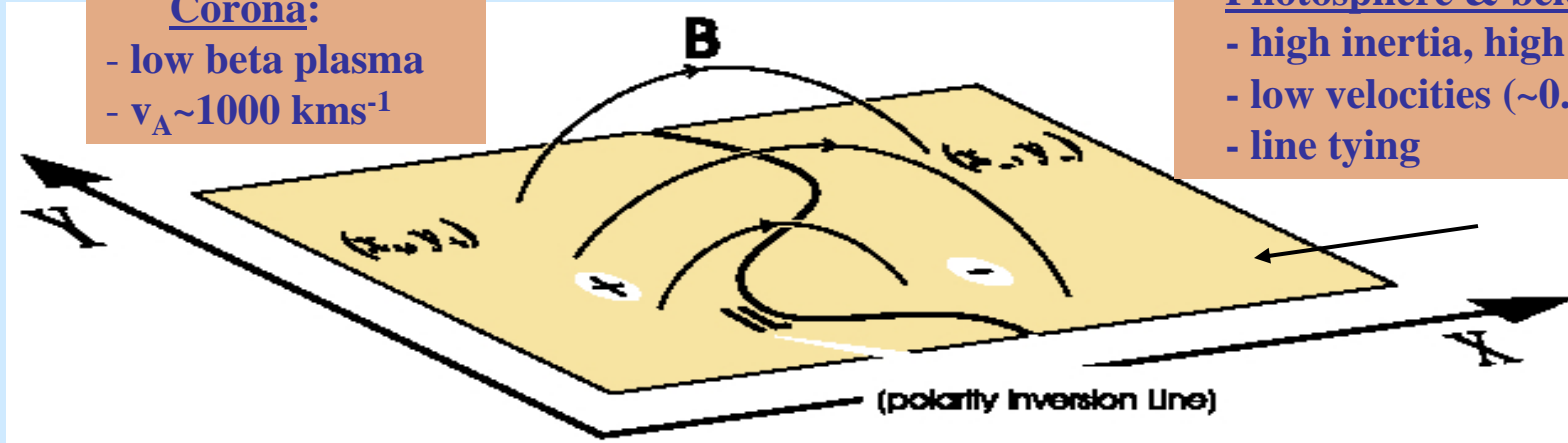
Definition of Quasi-Separatrix Layers

Corona:

- low beta plasma
- $v_A \sim 1000 \text{ kms}^{-1}$

Photosphere & below:

- high inertia, high beta
- low velocities ($\sim 0.1 \text{ kms}^{-1}$)
- line tying



Field line mapping to the “boundary” :

$$x_+, y_+ \rightarrow x_-, y_- : x_-(x_+, y_+), y_-(x_+, y_+)$$

Jacobi matrix :

$$F = \begin{pmatrix} \partial x_- / \partial x_+ & \partial x_- / \partial y_+ \\ \partial y_- / \partial x_+ & \partial y_- / \partial y_+ \end{pmatrix}$$

Initial QSL definition : regions where

$$N \equiv \| F \| \gg 1$$

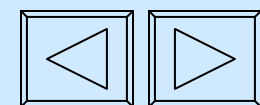
(Démoulin et al. 1996)

Better QSL definition : regions where
Squashing degree

$$Q \equiv \frac{\| F \|^2}{B_{n,+} / B_{n,-}} \gg 1$$

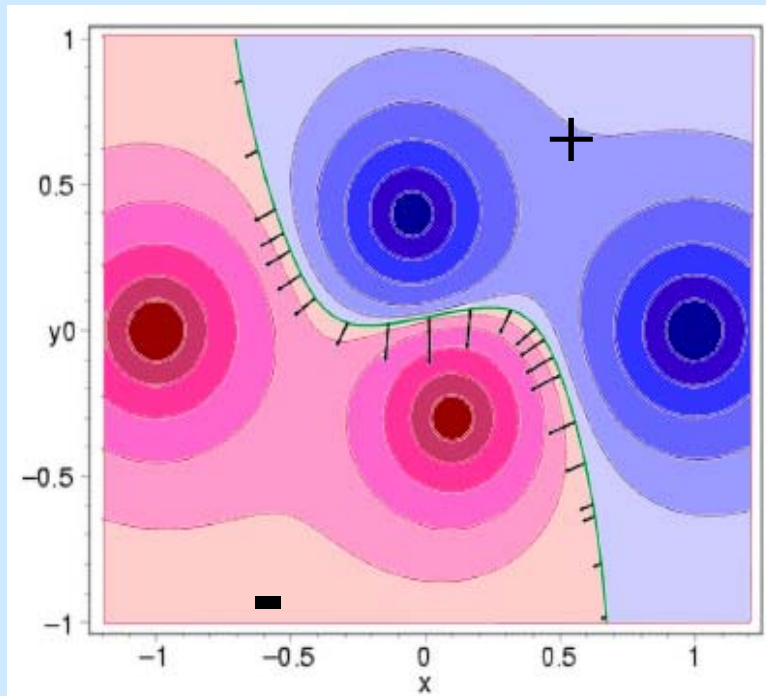
(Titov et al. 2002)

Same value of Q at both feet of a field line : $Q_+ = Q_-$



A basic theoretical configuration

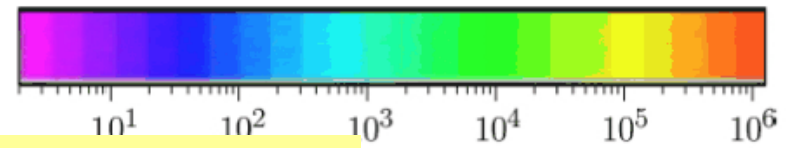
“magnetogram”
created with 4 magnetic concentrations



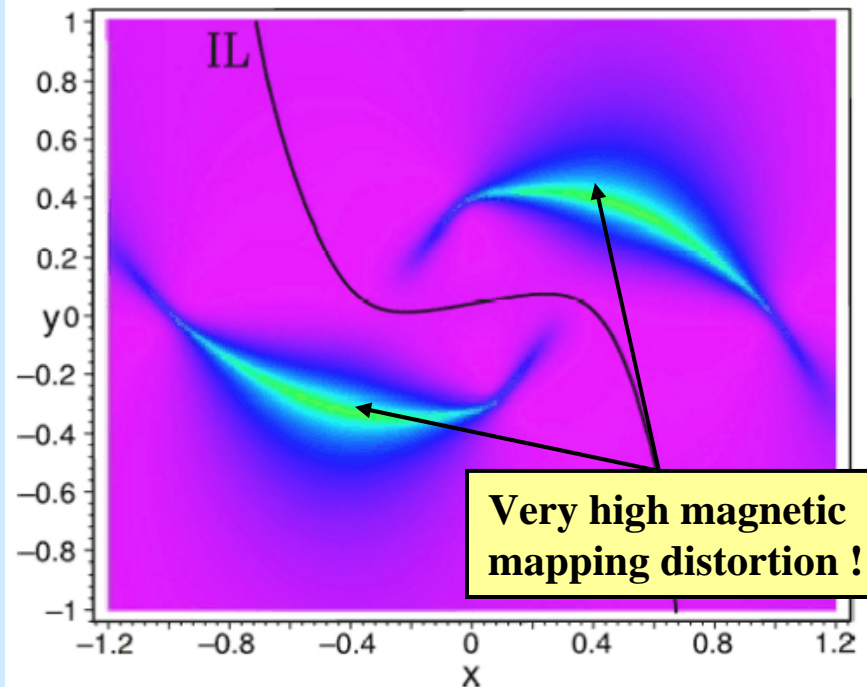
Above the magnetogram:

- No magnetic null
- No bald patch

No separatrices ... but QSLs

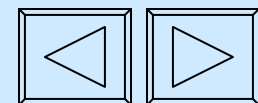


Squashing degree : Q

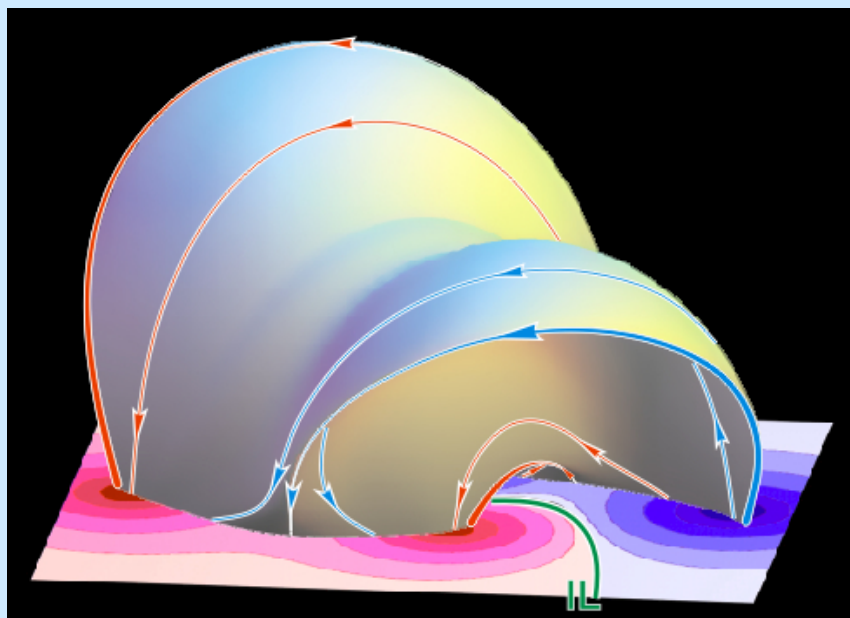


Very high magnetic
mapping distortion !

(Titov & Hornig 2002)

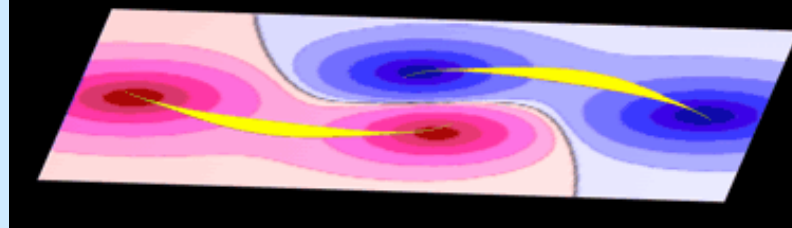


3D QSL shape



Magnetic connectivities

V. S. Titov
Theoretische Physik IV, Ruhr-Universität Bochum



Volume **inside the surface $Q = \text{constant}$** :
QSL shape

Summary :



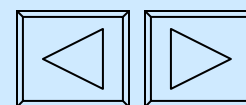
Boundary
 $B_n < 0$

X shape

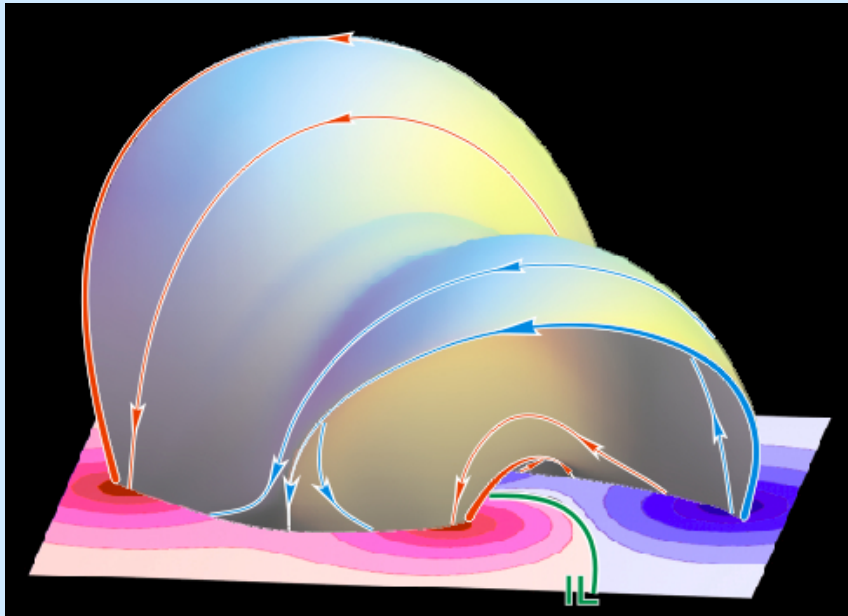
Boundary
 $B_n > 0$

Hyperbolic Flux Tube

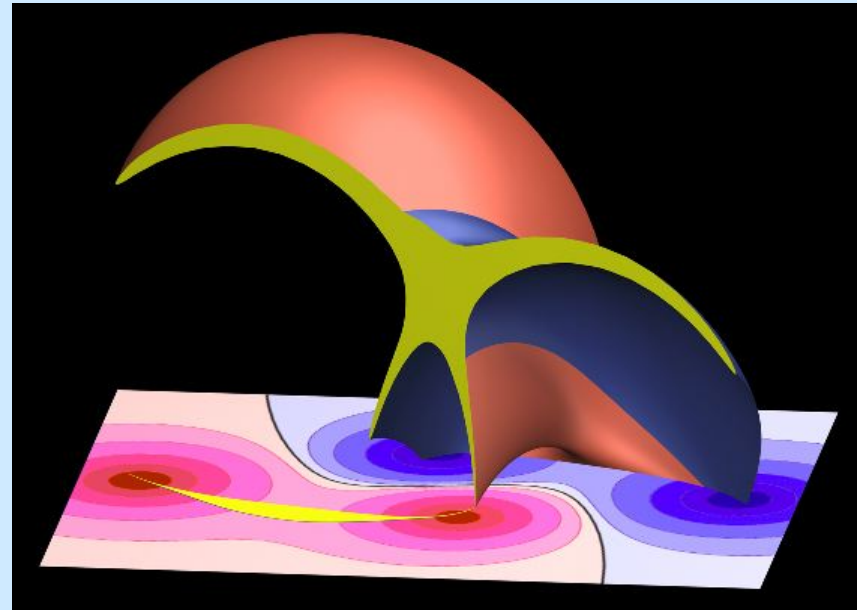
(Titov et al. 2002)



3D QSL shape



Magnetic connectivities



Volume **inside the surface $Q = \text{constant}$** :
QSL shape

Summary :



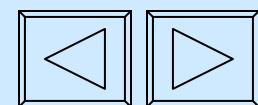
Boundary
 $B_n < 0$

X shape

Boundary
 $B_n > 0$

Hyperbolic Flux Tube

(Titov et al. 2002)



Does energy release occur at QSLs in solar flares ?

Input the photospheric magnetogram



Compute the coronal field



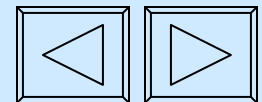
Compute QSLs



Compare to observed flare signatures

Various flaring configurations analyzed

(Bagala et al. 2000, Démoulin et al. 1997, Gaizauskas et al. 1999, Mandrini et al. 1996, 1997, Schmieder et al. 1997)



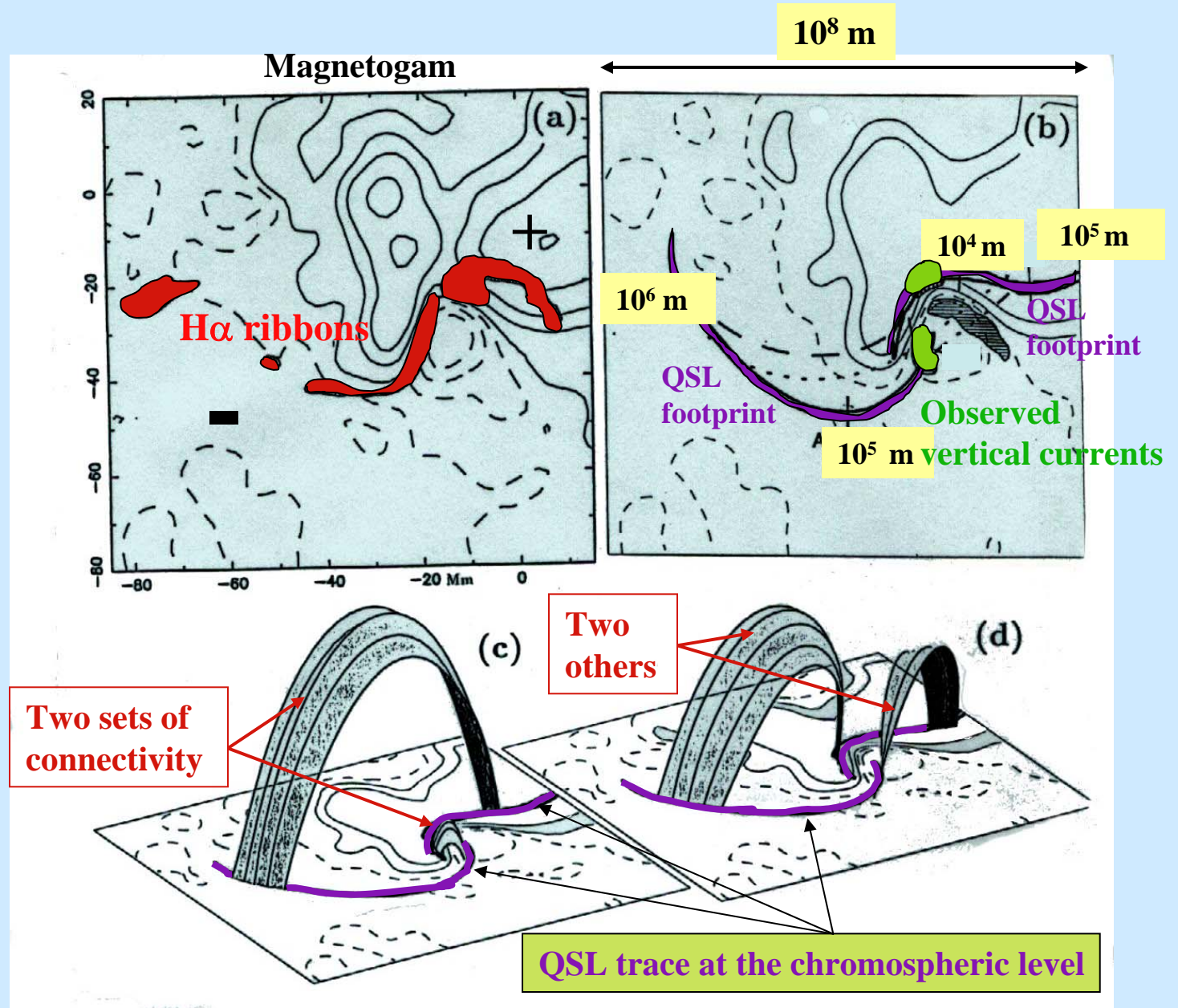
Example of flaring bipolar region

M4 flare
Nov. 5, 1980
AR 2776

H α ribbons
located on the QSL
(at chromospheric level)

NO magnetic null

QSL thickness
 $\sim 10^{-4}$ size AR
(lower if B
photospheric
more concentrated)



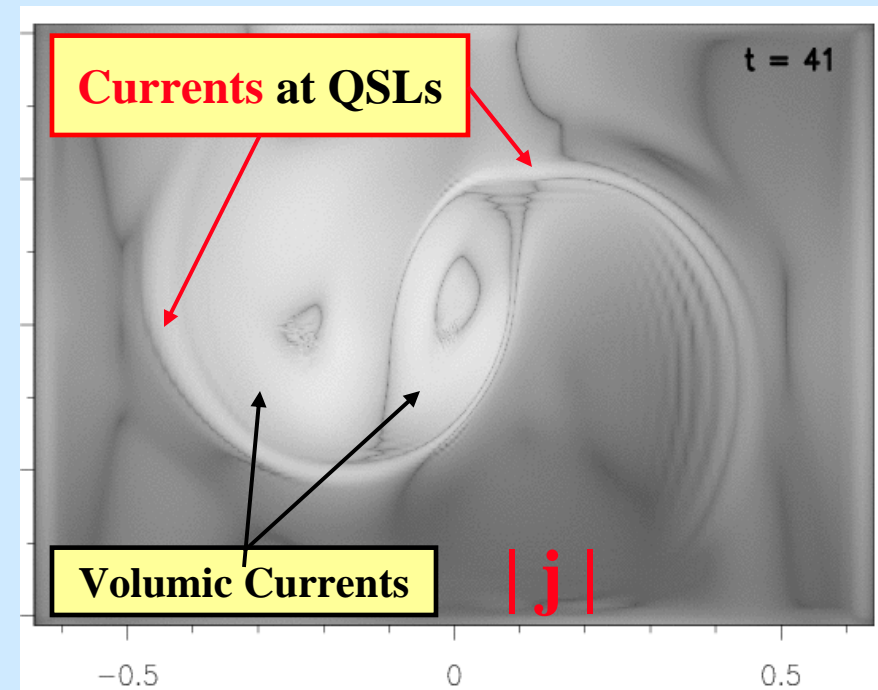
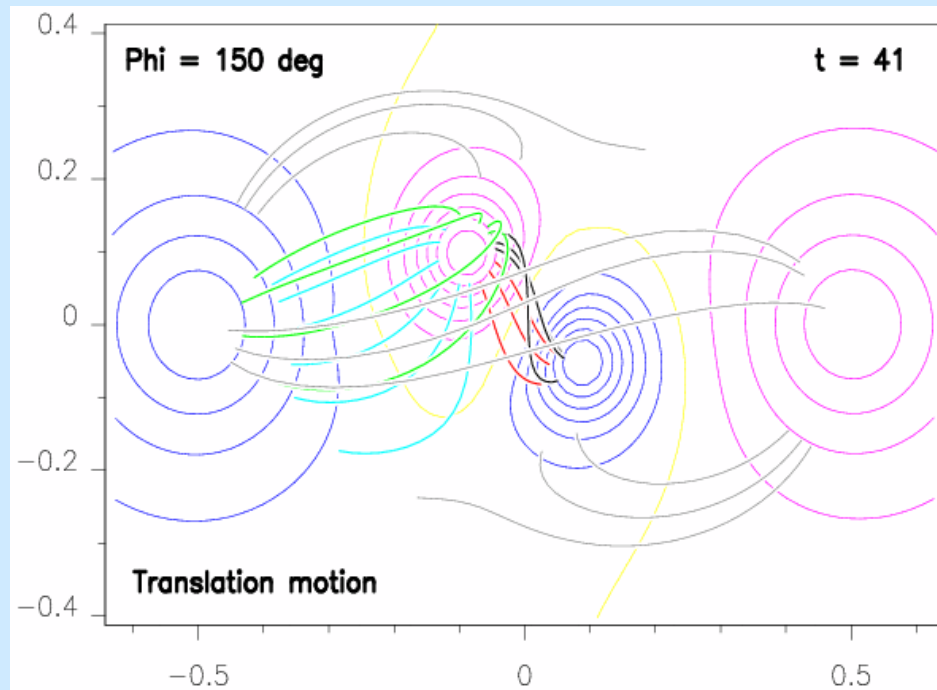
Formation of current at QSLs

- Expected theoretically
- Found in MHD simulations with stagnation type flows

(Démoulin et al. 1997)
(Milano et al. 1999,
Galsgaard et al. 2003)

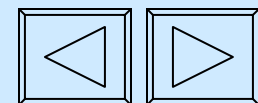
New MHD simulations (initial configurations with thin QSLs)

(Aulanier et al. 2005)



Do **NOT** need special motions

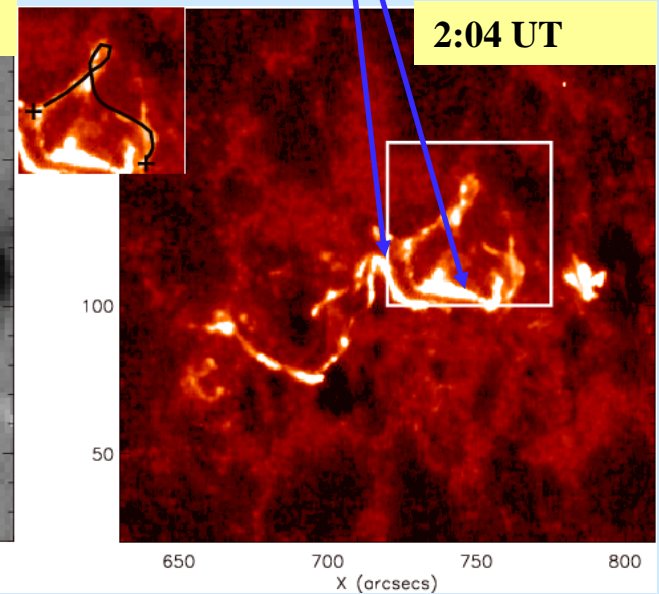
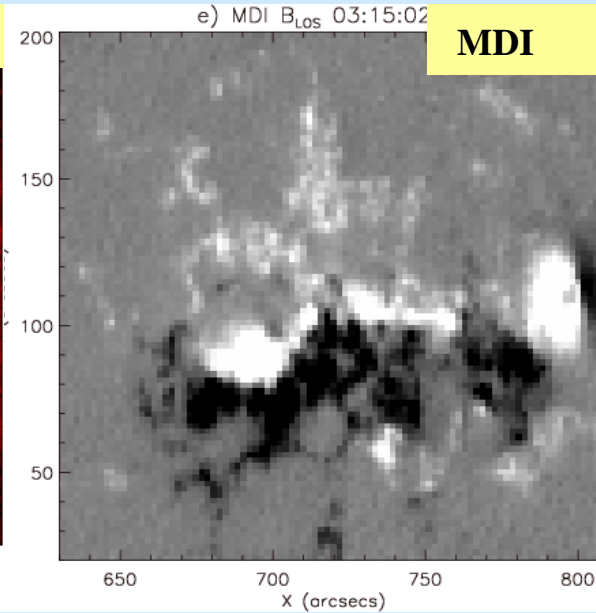
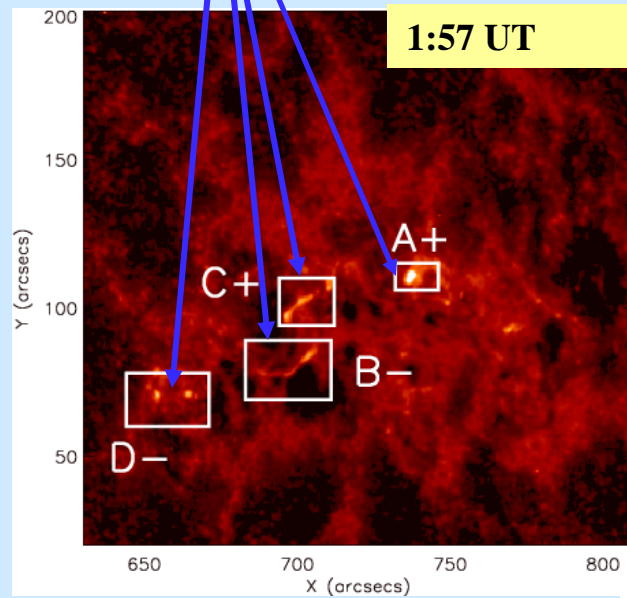
(opposite conclusion than Galsgaard et al. 2003)



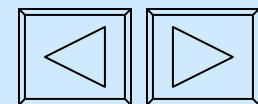
Example of an eruption

**quadrupolar reconnection (breakout)
4 ribbons**

**reconnection behind the twisted flux rope
(with kink instability) 2 J-shaped ribbons**



(Williams et al. 2005)



Brief summary

Discret photospheric field :
(Model with magnetic charges)

--> Photospheric null points --> Skeleton

Separatrices

Separator



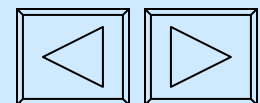
**Generalisation to
continuous field distribution :**

Quasi-Separatrix Layers

Hyperbolic Flux Tube

Indeed, a little bit more complex.....

More still to come....



Where reconnection occurs in 3D ?

1. Generalization of 2D cases to 3D :

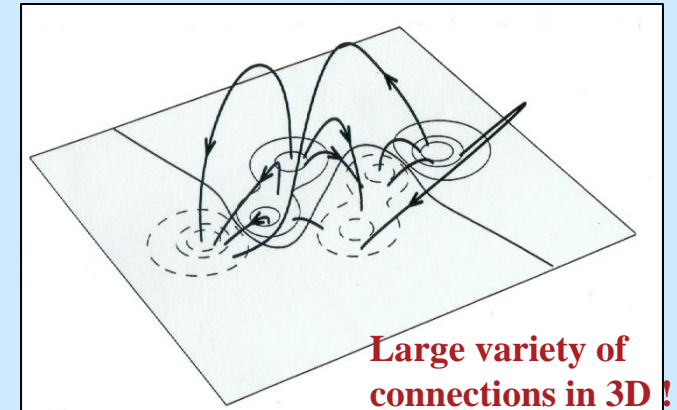
Bald **P**atch and **N**ull **P**oints separatrices

BUT many flare ribbons and loops

NOT related to **BP** & **NP** separatrices

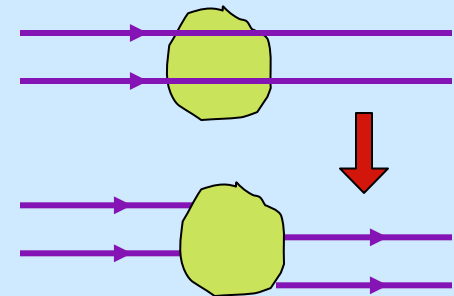
=> **Reconnection must occur in broader conditions**

(Démoulin et al. 1994)



2. One possibility: reconnection where resistivity is enhanced

“General magnetic reconnection” : $\int_{f.l.} \vec{E} \cdot \frac{\vec{B}}{B} ds \neq 0$

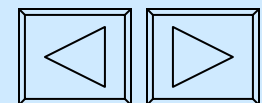


Why an increase of resistivity at some locations ?

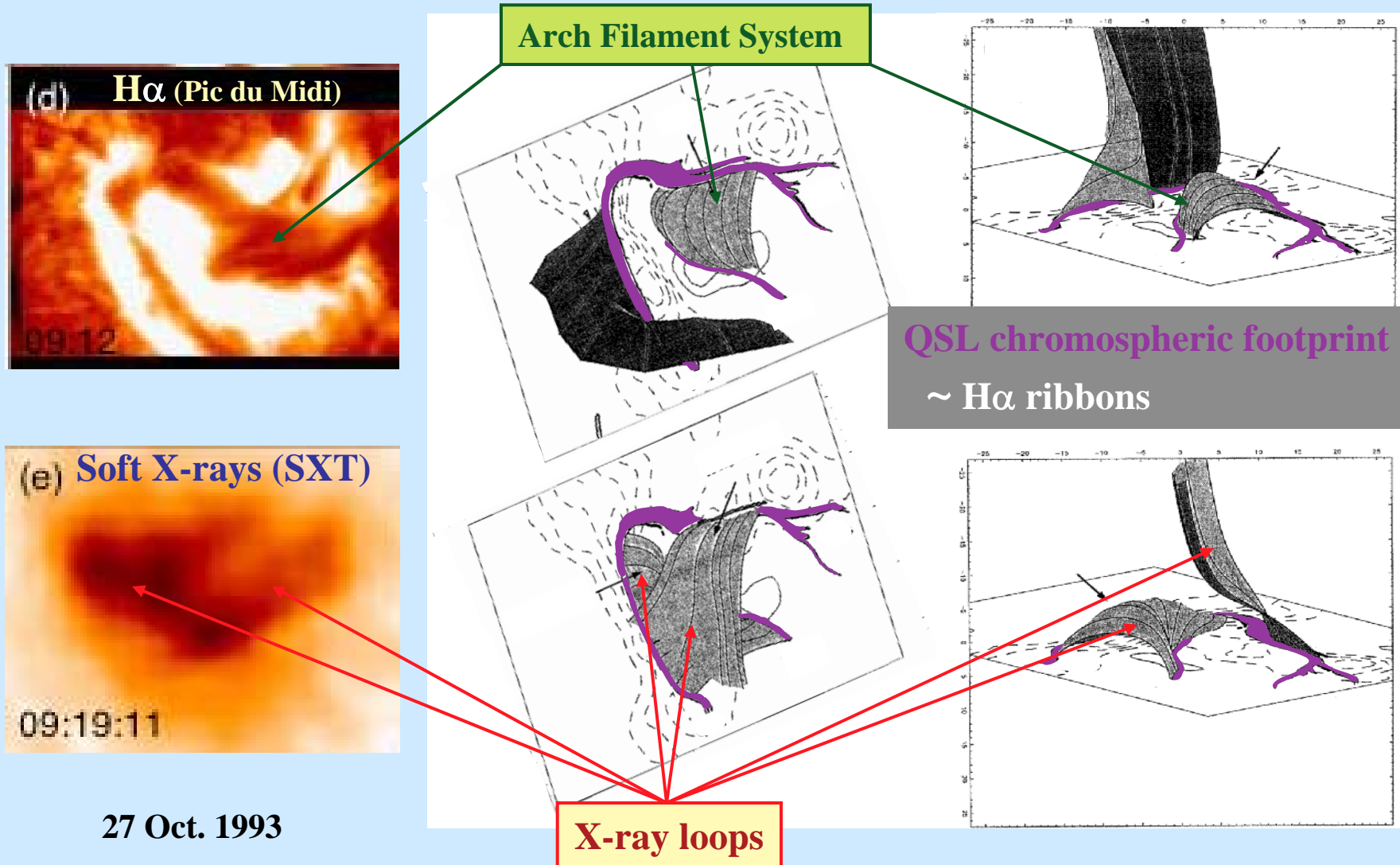
From flare studies, the reconnection is linked to the 3D organisation of magnetic field lines

(Schindler et al. 1988
Birn et al. 1989
Hesse et al. 1990)

Possibility of resistivity enhancement at separatrices.....+ QSLs !

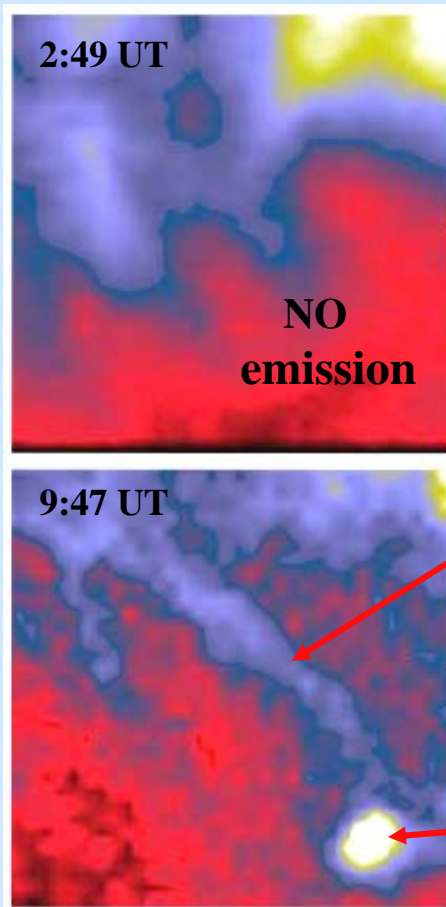


A different type of flaring configuration

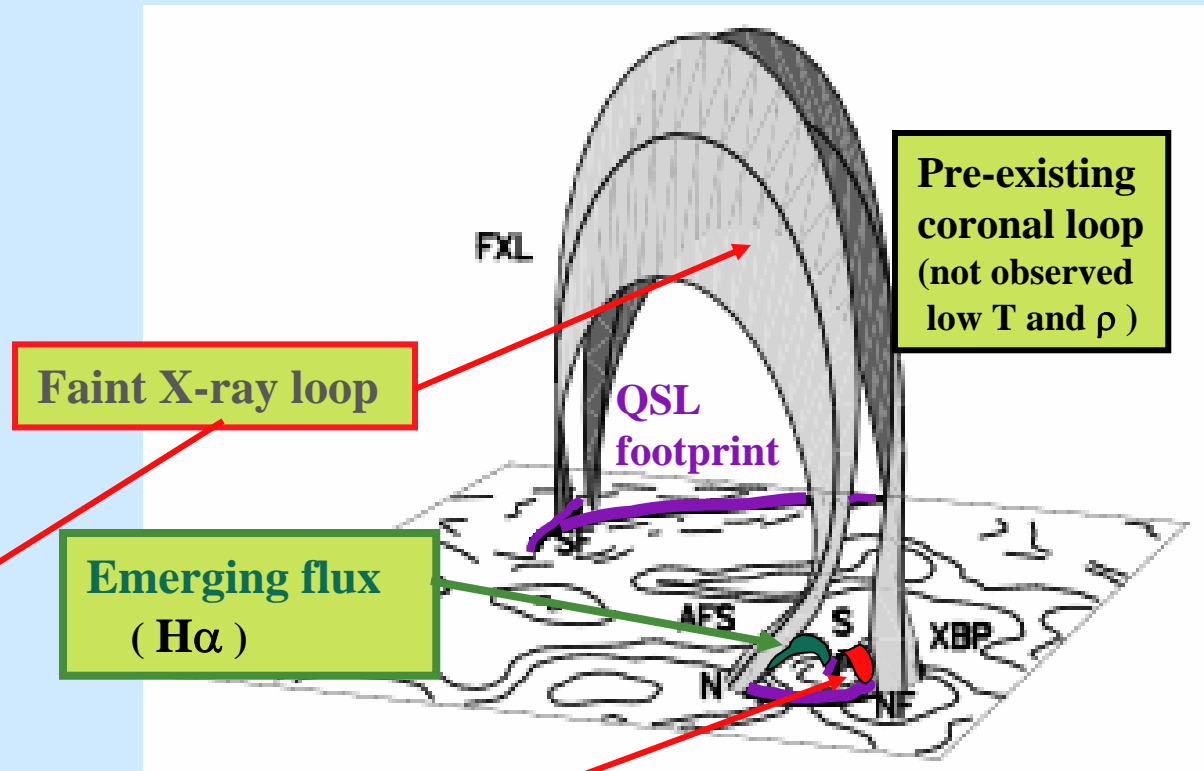


Reconnection at QSLs : X-ray bright point

Soft X-rays, May 1 1993
Yohkoh / SXT

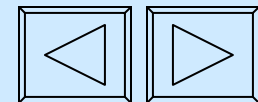


Model from magnetic extrapolation



(Mandrini et al. 1996)

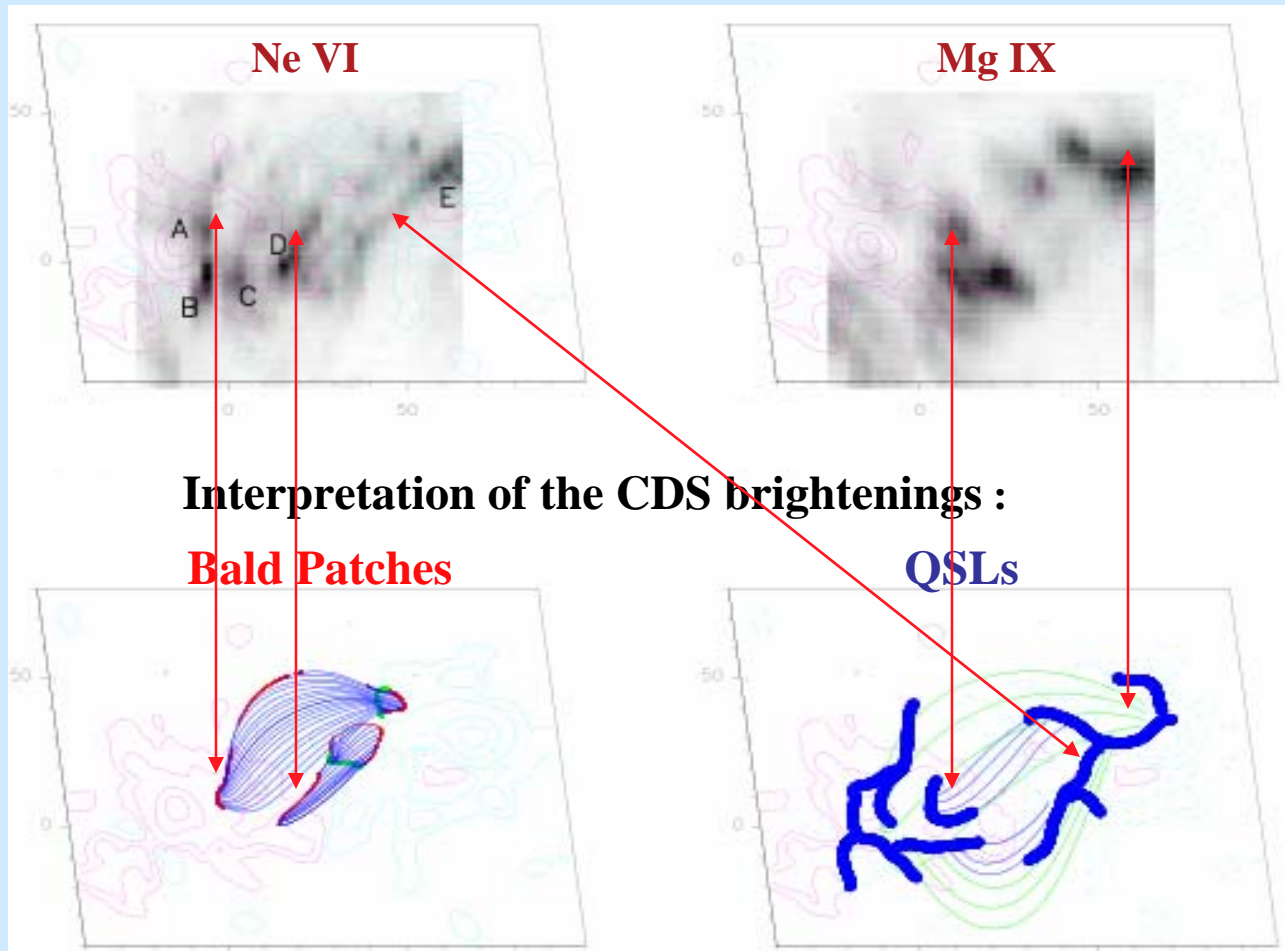
Energy release occurred when the QSL thickness is lower than 100 m



Transition Region Brightenings

CDS / SoHO

Inversed
contrast



Interpretation of the CDS brightenings :

Bald Patches

QSLs

Mg / Ne abundances in CDS
brightenings associated to :

compared to :

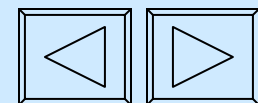
Bald Patches : [0.7, 1.7]

QSLs : [2.0, 3.9]

photosphere: [0.2,0.3]

corona: [1.4,2.0]

(Fletcher et al. 2001)

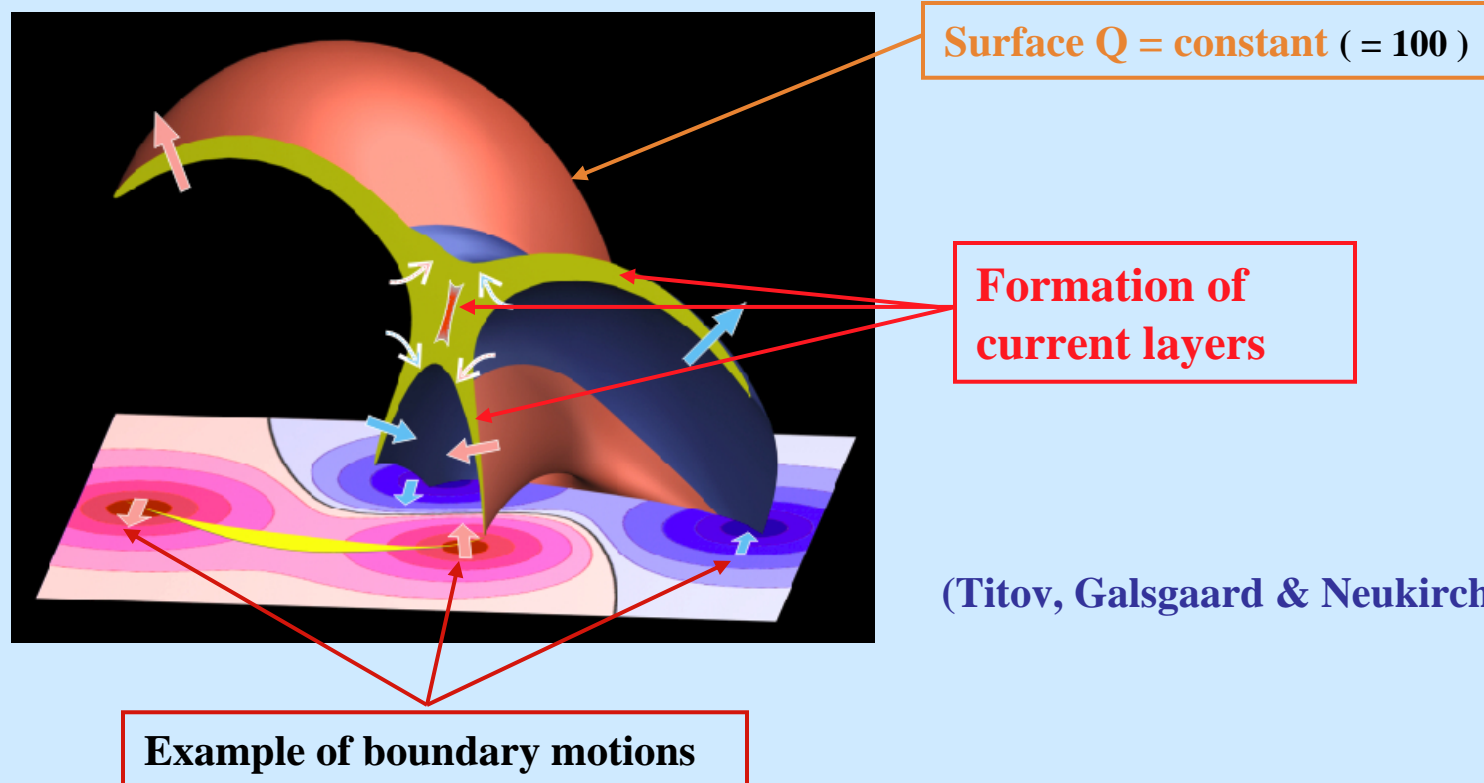


Formation of current layers at QSLs (1)

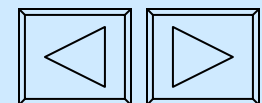
- Expected theoretically : - with almost any boundary motions
- with an internal instability

Using Euler potential representation: magnetic shear gradient across QSL

(Démoulin et al. 1997)



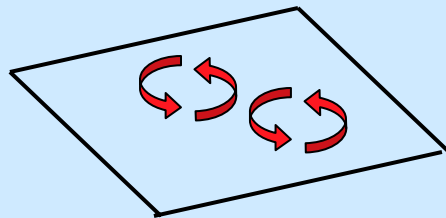
(Titov, Galsgaard & Neukirch. 2003)



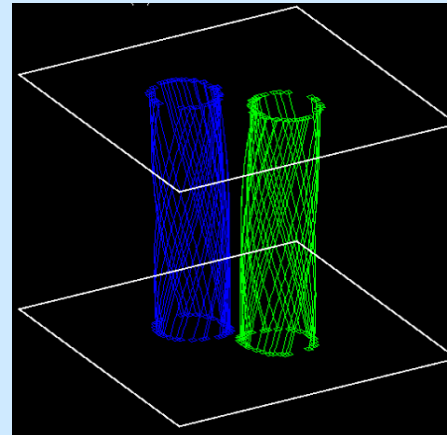
Formation of current layers at QSLs (2)

- Found in MHD simulations

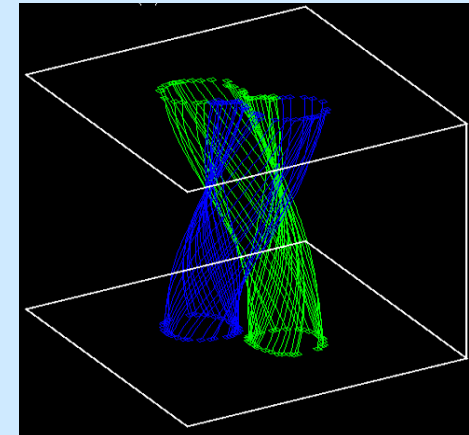
- Start from a uniform B field
- Apply twisting motions



Two twisted flux tubes are formed



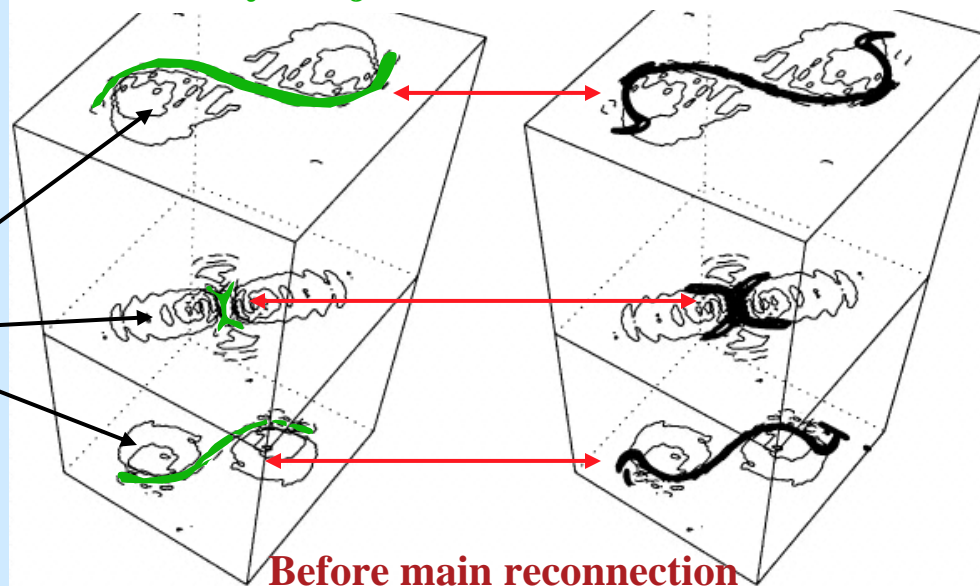
Then they reconnect



Current layer ($j < 0$)

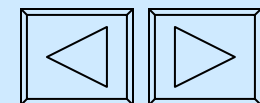
QSL footprint

Twisted flux
tube currents
($j > 0$)



Before main reconnection

(Milano et al. 1999)



How can we characterize 3D field-line linkage ?

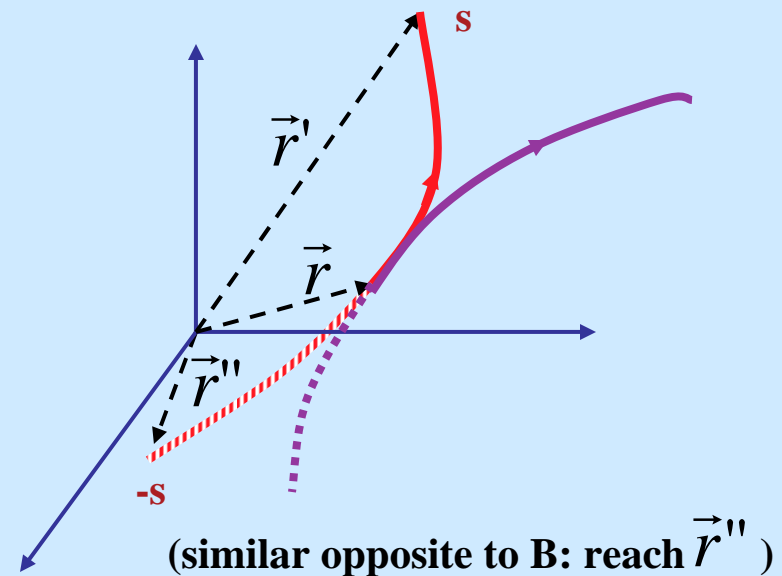
Compute field line starting at \vec{r}
up to a curvilinear length s // to B: reach \vec{r}'

Field line mapping: $\vec{r} \rightarrow \vec{r}': \vec{r}'(\vec{r}, s)$

Modify \vec{r} , how \vec{r}' change ?

Jacobi matrix:

$$F_{(\vec{r}, s)} \equiv \left(\partial \vec{r}' / \partial \vec{r} \right)_s$$



	$\vec{r}'(\vec{r}, s)$	$\ F \ $
Most locations	Continuous	$\ F \ \approx 1$
Separatrix	Discontinuous	singular (delta function)
QSL	Drastic changes	$\ F \ \gg 1$

