

# Constraints from Galaxy Cluster in the photometric Euclid Survey

Barbara Sartoris

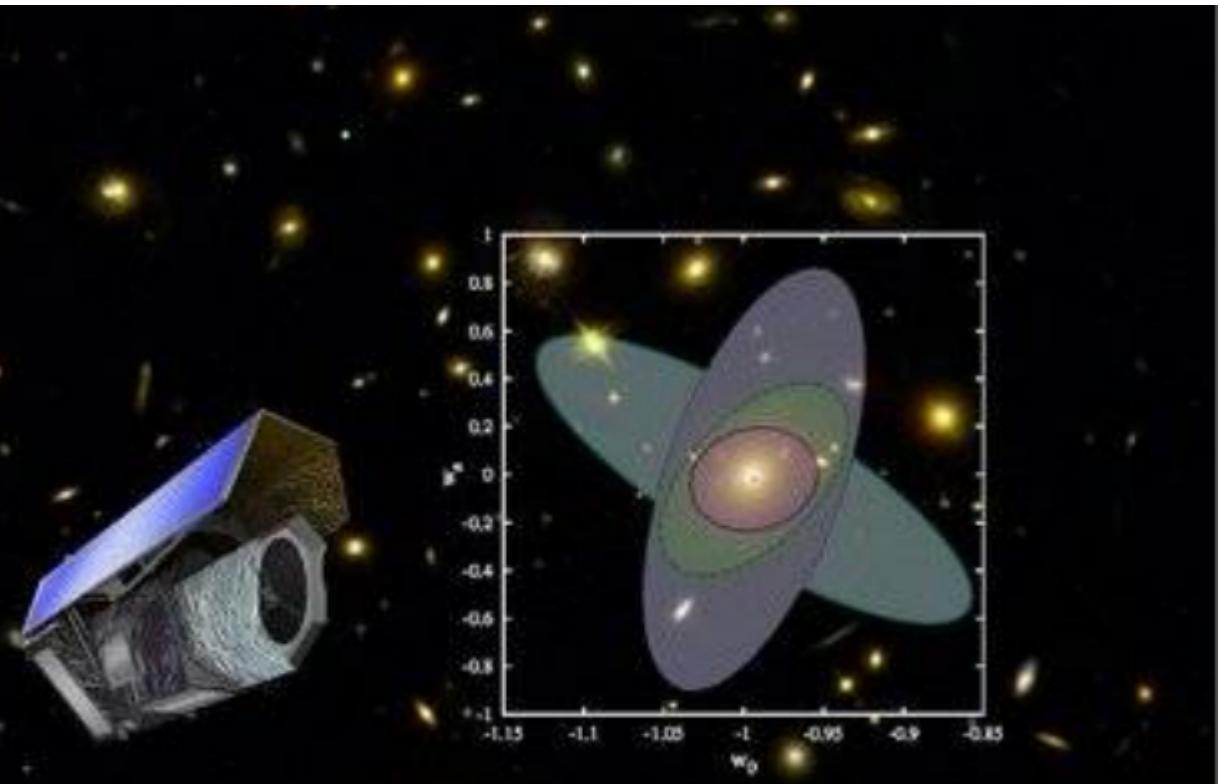
Mykonos, 17 VI 2016



University of Trieste

INAF - Osservatorio  
Astronomico di Trieste

# Cluster cosmology



ESA medium mission with the aim of estimate the DE EoS measuring the cosmological Weak Lensing and the galaxy clustering

Launch: 2020

Galaxy clusters are “additional cosmological probes” for Euclid

Three essential tools are required for cluster cosmological:

- an efficient method to identify clusters over a wide redshift range
- a robust observable estimator of the cluster mass
- a method to compute the selection function  
(or equivalently the survey volume within which clusters are found)

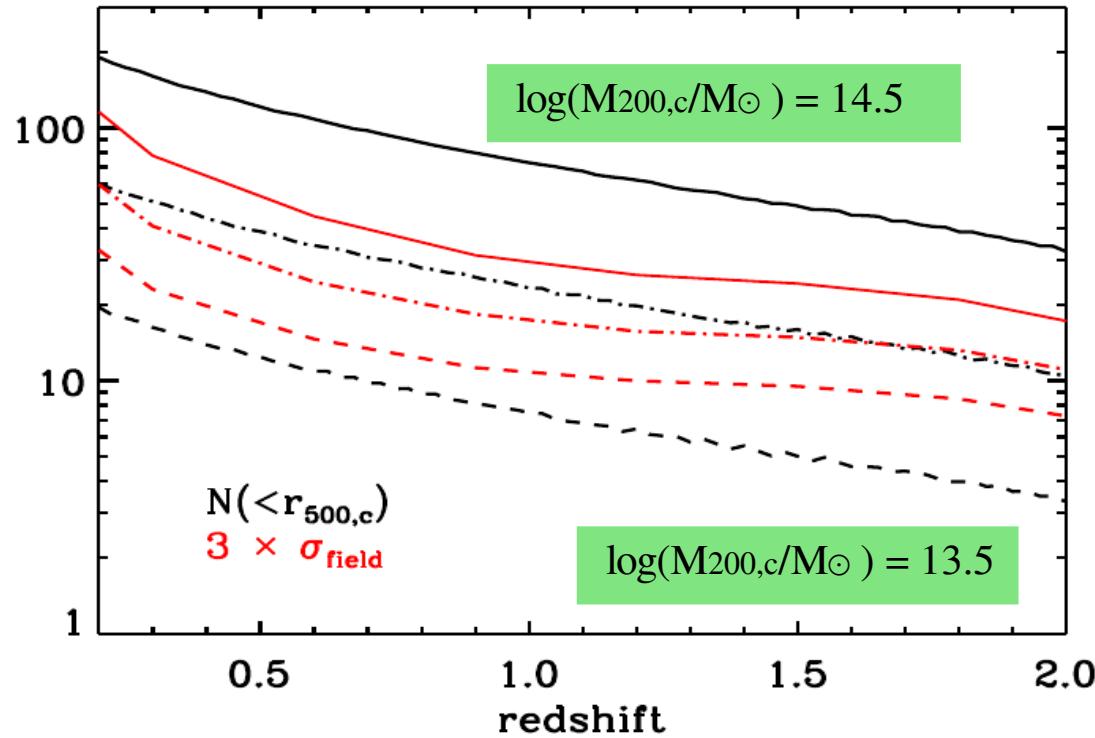
# The Euclid mission

SURVEYS									
	Area (deg2)	Description							
Wide Survey	15,000 (required) 20,000 (goal)	Step and stare with 4 dither pointings per step.							
Deep Survey	40	In at least 2 patches of $> 10 \text{ deg}^2$ 2 magnitudes deeper than wide survey							
PAYLOAD									
Telescope	1.2 m Korsch, 3 mirror anastigmat, $f=24.5 \text{ m}$								
Instrument	VIS	NISP							
Field-of-View	$0.787 \times 0.709 \text{ deg}^2$	$0.763 \times 0.722 \text{ deg}^2$							
Capability	Visual Imaging	NIR Imaging Photometry			NIR Spectroscopy				
Wavelength range	550– 900 nm	Y (920-1146nm),	J (1146-1372 nm)	H (1372-2000nm)	1100-2000 nm				
Sensitivity	24.5 mag $10\sigma$ extended source	24 mag $5\sigma$ point source	24 mag $5\sigma$ point source	24 mag $5\sigma$ point source	$3 \cdot 10^{-16} \text{ erg cm}^{-2} \text{ s}^{-1}$ $3.5\sigma$ unresolved line flux				
Detector Technology	36 arrays $4k \times 4k$ CCD	16 arrays $2k \times 2k$ NIR sensitive HgCdTe detectors							
Pixel Size Spectral resolution	0.1 arcsec	0.3 arcsec			0.3 arcsec $R=250$				

B. Sartoris, A. Biviano, C. Fedeli, J. Bartlett, S. Borgani, M. Costanzi, C. Giocoli, L. Moscardini, J. Weller, B. Ascaso, S. Bardelli, S. Maurogordato, and P. Viana (published on MNRAS)

Forecast on constraints from galaxy cluster in the photometric Euclid survey

# Selection function of cluster photometric survey



$$\log(M_{200,c}/M_\odot) = 14.0$$

$$\log(M_{200,c}/M_\odot) = 13.5$$

These counts have been obtained integrating the LF of Lin+03 down to the limiting magnitude  $H_{AB} = 24$ , as a function of redshift for clusters of different masses.

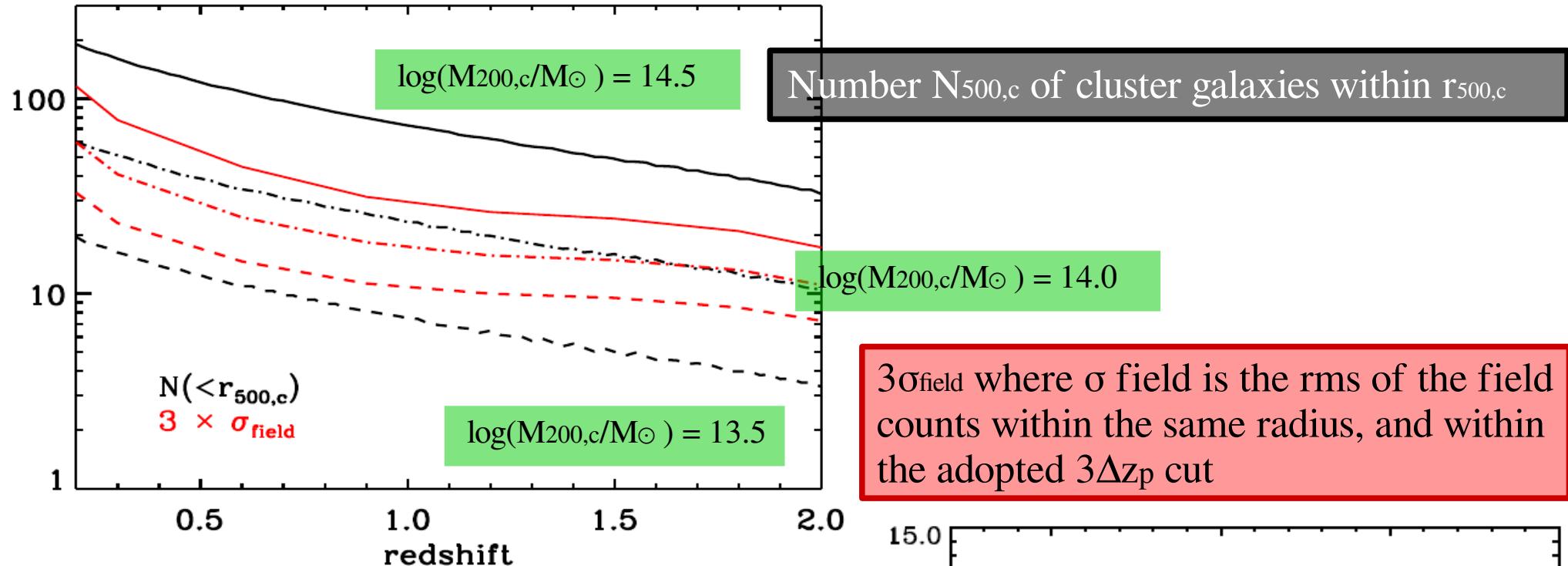
Evolution with  $z$ : no redshift evolution of  $\varphi^*$  and  $\alpha$ . For  $M^*$  redshift evolution we assume a passive evolution over the full cluster mass range.

$3\sigma_{\text{field}}$  where  $\sigma_{\text{field}}$  is the rms of the field counts within the same radius, and within the adopted  $3\Delta z_p$  cut

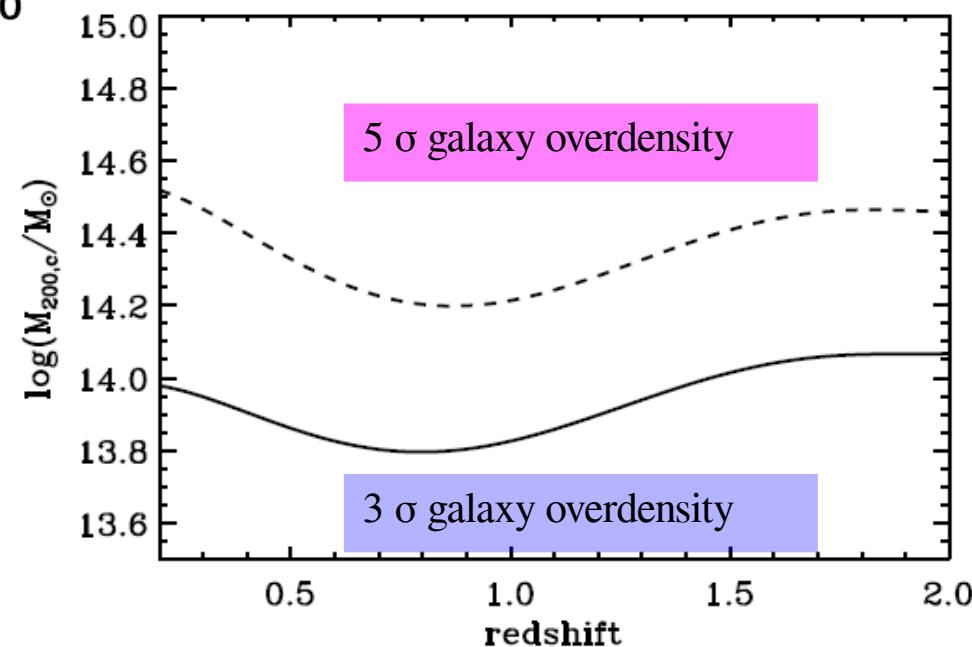
Non-cluster members are all those galaxies that are more than  $3\Delta z_p$  away from the mean cluster redshift.

Euclid required accuracy of  $\Delta z_{\text{phot}} \equiv 0.05(1+z_{\text{cl}})$ , (Euclid phot+ground-based data).

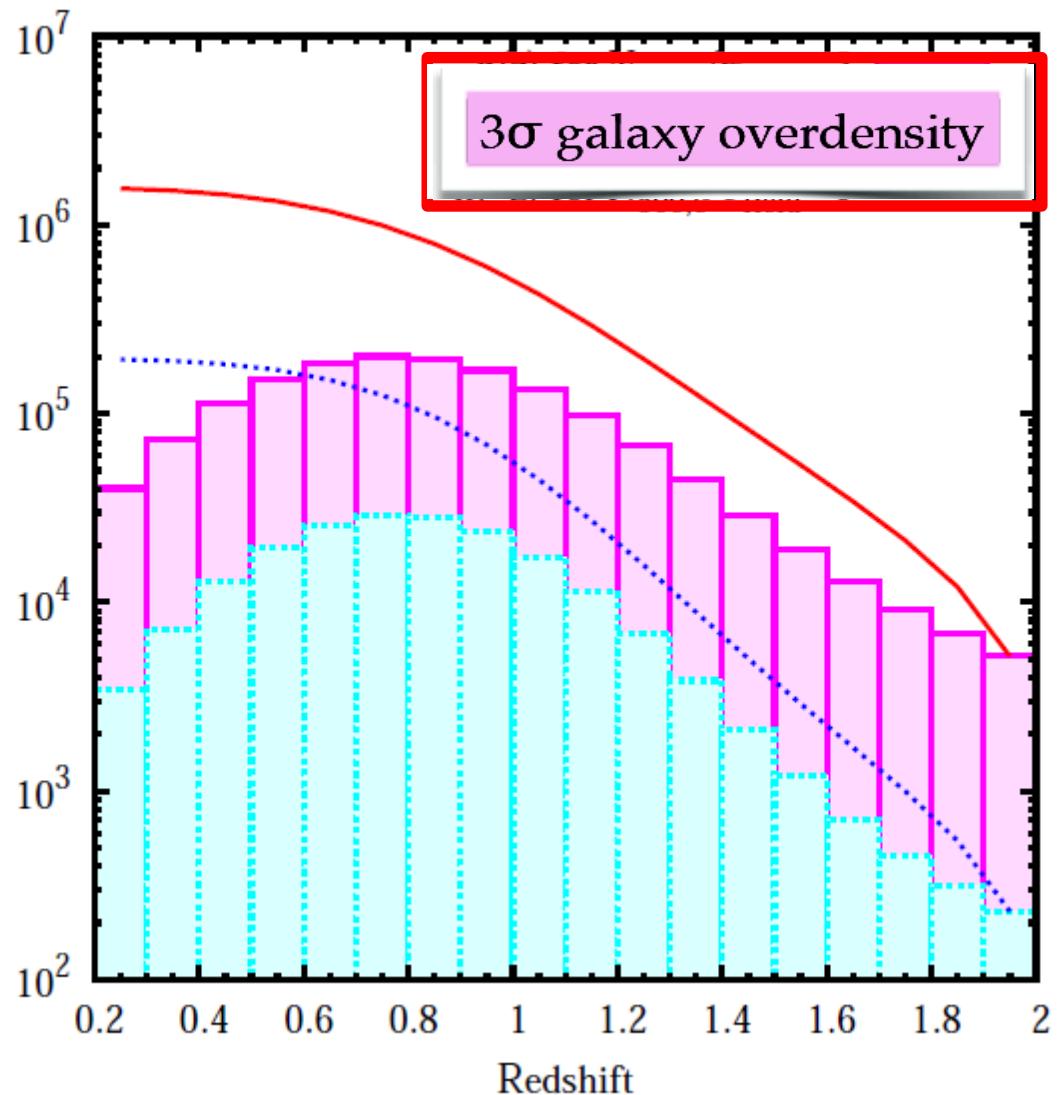
# Selection function of cluster photometric survey



These counts are calculated down to the limiting magnitude  $H_{AB} = 24$ , as a function of redshift for clusters of different masses



# Number of clusters



Euclid will detect  
~  $2 \cdot 10^5$  objects at  $0.2 \leq z \leq 2$ ,  
~  $4 \cdot 10^4$  objects at  $z > 1$   
for the  $5\sigma$  selection function.

By lowering the detection threshold  
down to  $3\sigma$ , these numbers **rise up to an  
order of magnitude**.

5 $\sigma$  galaxy overdensity

15000 sq deg

# Cluster number density

$$N_{l,m} = \Delta\Omega \int_{z_l}^{z_{l+1}} dz \frac{dV}{dz d\Omega} \int_{M_{l,m}^{ob}}^{M_{l,m+1}^{ob}} dM^{ob}$$

$$\int_0^\infty dM n(M, z) p(M^{ob} | M).$$

Self – calibration method:  
 Probability of assigning a mass  $M_{obs}$  to a cluster of  $M_{true}$  is a lognormal distribution

$$p(M^{ob}|M) = \frac{\exp[-x^2(M^{ob})]}{\sqrt{2\pi\sigma_{\ln M}^2}}$$

where:

$$x(M^{ob}) = \frac{\ln M^{ob} - \ln M_{bias} - \ln M}{\sqrt{2\sigma_{\ln M}^2}}$$

Nuisance Parameters

$$\ln M_{bias}(z) = B_{M,0} + \alpha \ln(1+z)$$

$$\sigma_{\ln M}^2(z) = \sigma_{\ln M,0}^2 - 1 + (1+z)^{2\beta}$$

$$p_{nuisance,F} = \{B_{M,0} = 0, \alpha = 0, \sigma_{\ln M,0} = 0.2, \beta = 0.125\}$$

Sartoris+10

Lima & Hu '05

# Cluster power spectrum

$$\bar{P}_{l,m,i}^{cl}(\mu, k, z_l) = \frac{\int_{z_l}^{z_{l+1}} dz \frac{dV}{dz} \tilde{n}^2(z) \tilde{P}(\mu, k, z)}{\int_{z_l}^{z_{l+1}} dz \frac{dV}{dz} \tilde{n}^2(z)}$$

Averaged cluster power spectrum

Comoving volume element

Cluster mass function convolved with the observable mass scaling relation

$$\tilde{n} = \int_0^\infty dM n(M, z) [\text{erfc}(x_m) - \text{erfc}(x_{m+1})].$$

$$\tilde{P}(k, \mu, z) = (b_{eff} + f\mu^2)^2 D^2(z) P(k)$$

Cluster power spectrum

Majumdar & Mohr '03

Sartoris+12

# Cluster power spectrum

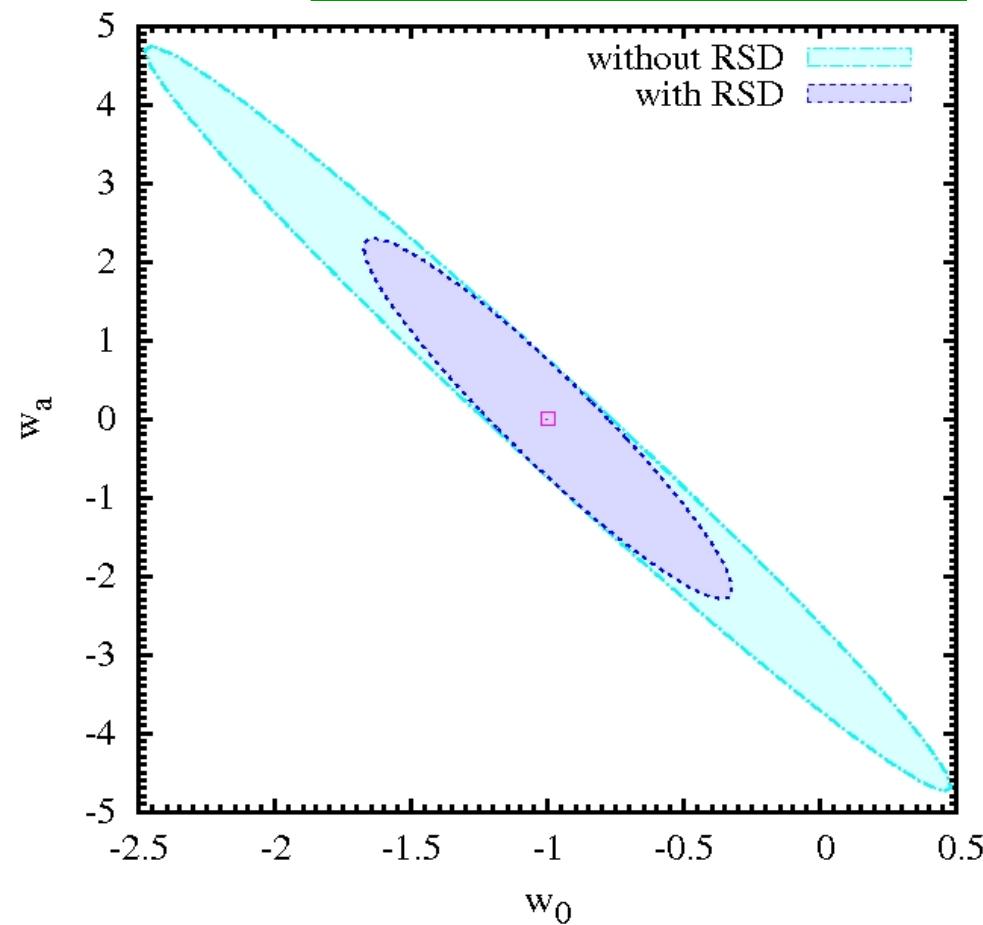
$$\bar{P}_{l,m,i}^{cl}(\mu, k, z_l) = \frac{\int_{z_l}^{z_{l+1}} dz \frac{dV}{dz} \tilde{n}^2(z) \tilde{P}(\mu, k, z)}{\int_{z_l}^{z_{l+1}} dz \frac{dV}{dz} \tilde{n}^2(z)}$$

Averaged cluster power spectrum

Cluster redshift space distortion contribution to w<sub>0</sub>-w<sub>a</sub> constraints for a wide X-ray survey (WFXT)

$$\tilde{P}(k, \mu, z) = (b_{eff} + f\mu^2)^2 D^2(z) P(k)$$

Sartoris+12



# The statistical methods and the constraints on DE

$N_{500,c}/\sigma_{\text{field}} \geq 3$  Euclid photometric cluster selection

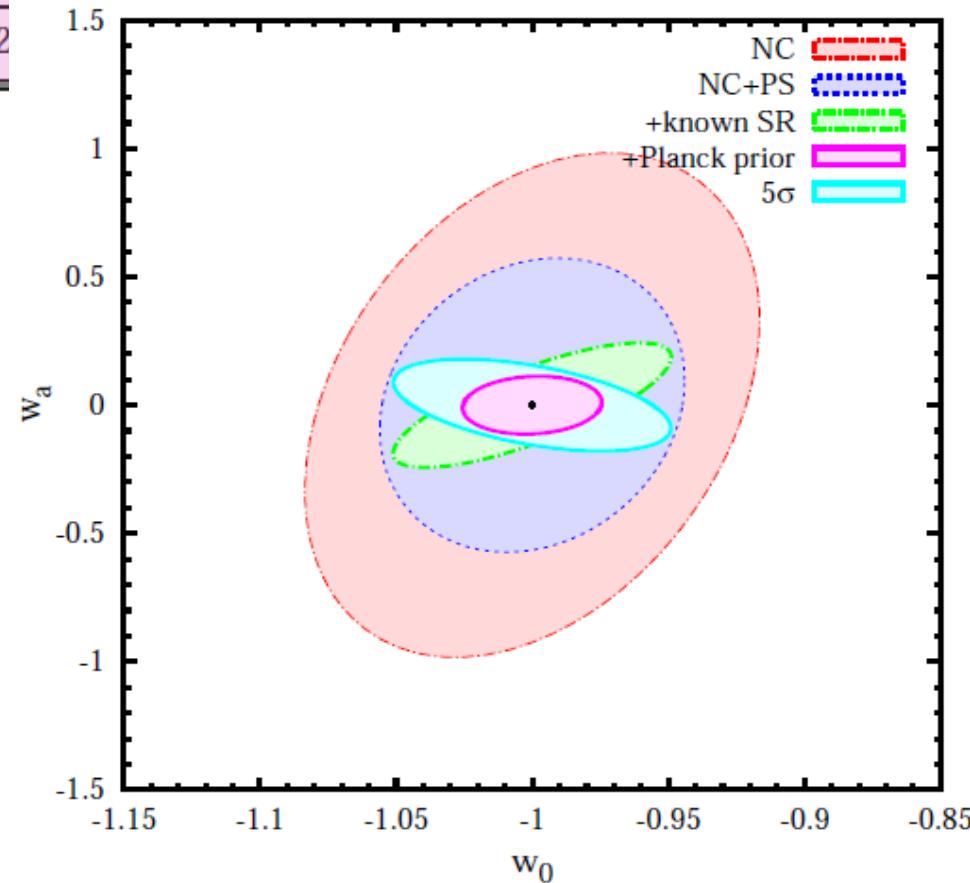
Parameter arrays: Constraints:	Eqs. 16 & 28					Eqs. 22 & 28	Eqs. 20 & 28	Eqs. 26 & 28
	FoM	$\Delta w_0$	$\Delta w_a$	$\Delta \Omega_m$	$\Delta \sigma_8$	$\Delta \gamma$	$\Delta f_{NL}$	$\Delta \Omega_\nu$
NC+PS	73	0.037	0.38	0.0019	0.0032	0.023	6.67	0.0015
NC+PS+known SR	291	0.034	0.16	0.0011	0.0014	0.020	6.58	0.0013
NC+PS+known SR+Planck	802	0.017	0.074	0.0010	0.0012	0.015	4.93	0.0012
	$N_{500,c}/\sigma_{\text{field}} \geq 5$ Euclid photometric cluster selection							
NC+PS+known SR+Planck	209	0.034	0.12	0.0022	0.002			

Fisher matrix:

$$F_{ij} \equiv - \left\langle \frac{\partial^2 \ln \mathcal{L}}{\partial p_i \partial p_j} \right\rangle$$

$$p = \{\Omega_m, \sigma_8, w_0, w_a, \Omega_k, \Omega_b, H_0, n_s\}$$

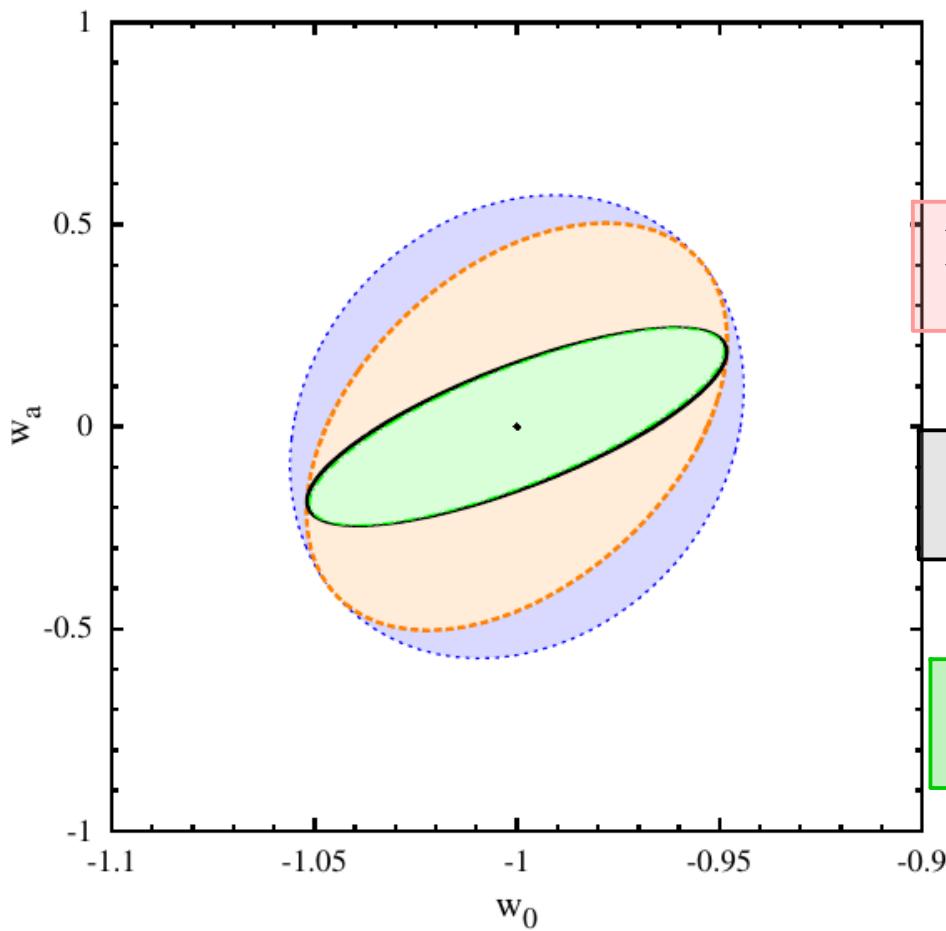
$$w(a) = w_0 + w_a(1-a)$$



# Impact of scaling relations

Knowledge of the  
observable mass  
relation

No prior



Known scatter  
evolution

Known bias  
evolution

Known scaling  
relation at  $z=0$

$$p(M^{\text{ob}}|M) = \frac{\exp[-x^2(M^{\text{ob}})]}{\sqrt{2\pi\sigma_{\ln M}^2}},$$

$$x(M^{\text{ob}}) = \frac{\ln M^{\text{ob}} - \ln M_{\text{bias}} - \ln M}{\sqrt{2\sigma_{\ln M}^2}}.$$

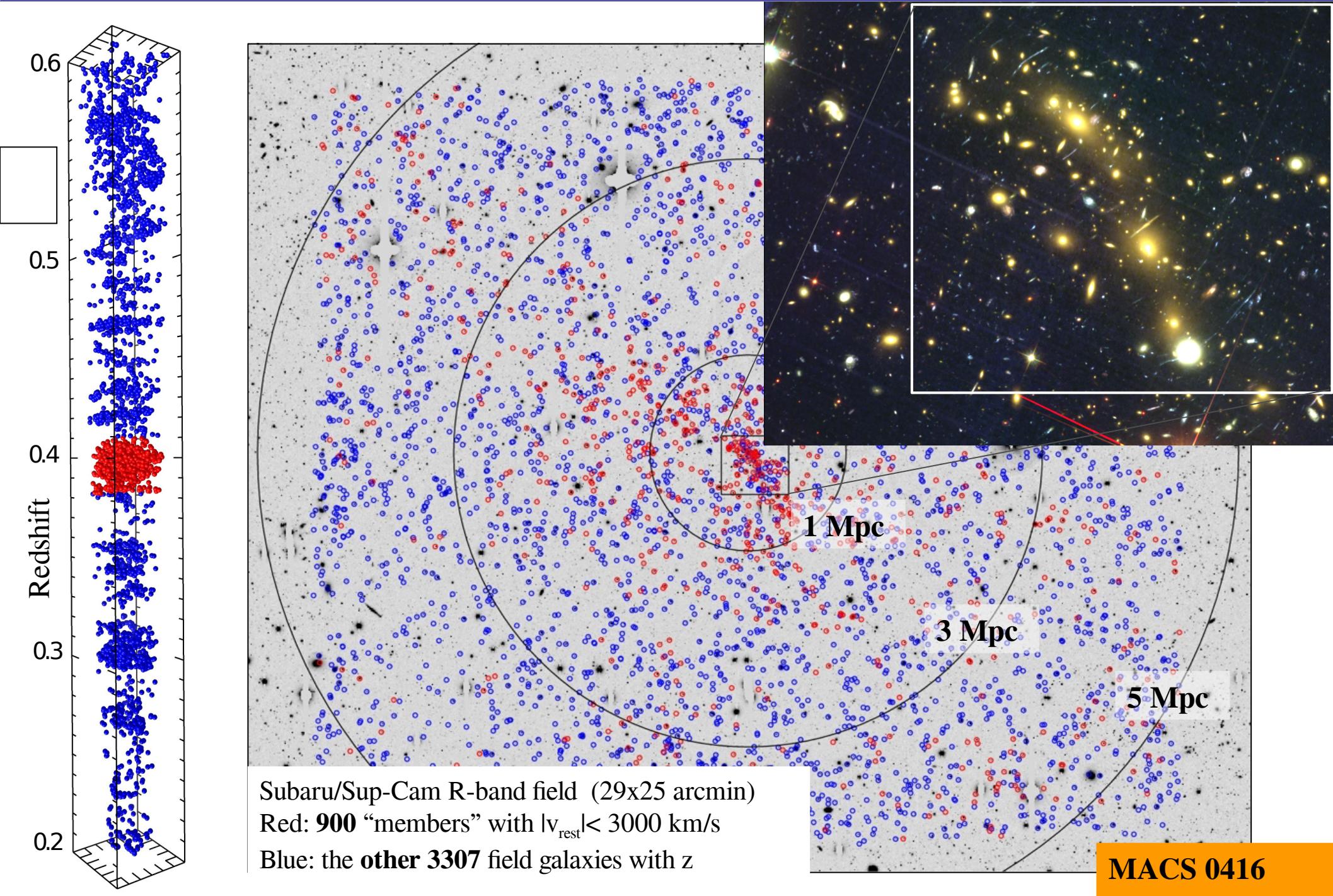
Simple parametrization of the  
nuisance parameters

$$\ln M_{\text{bias}}(z) = B_{M,0} + \alpha \ln(1+z)$$

$$\sigma_{\ln M}^2(z) = \sigma_{\ln M,0}^2 - 1 + (1+z)^{2\beta}.$$

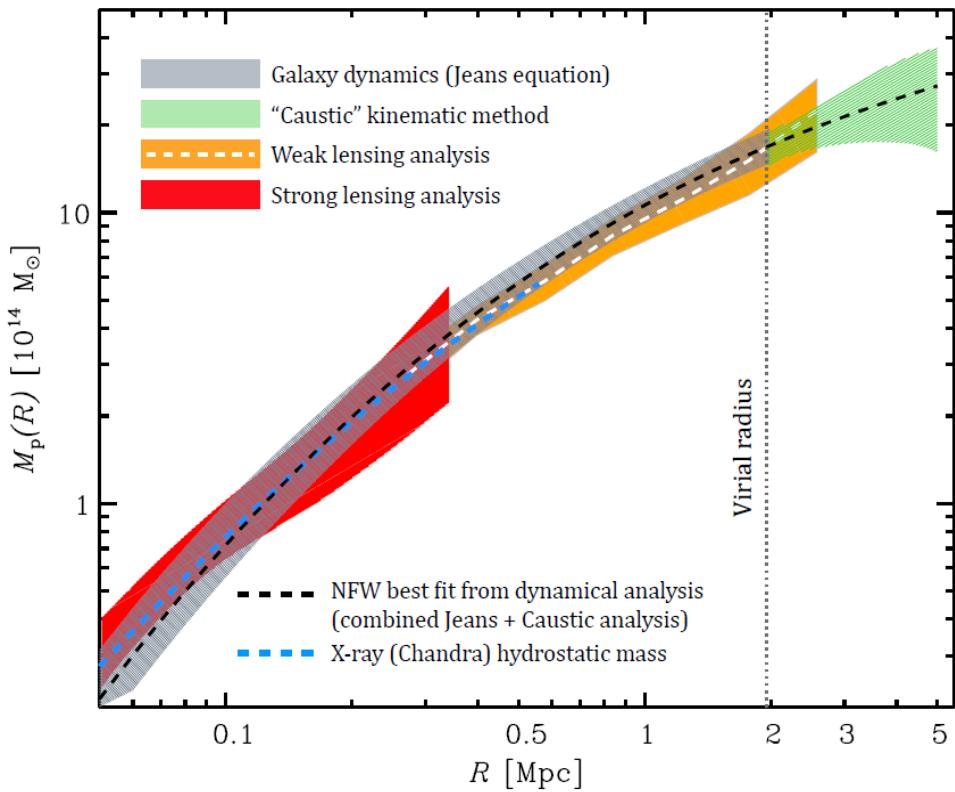
We need to know the bias evolution  
at 1% level

# CLASH + CLASH-VLT + Subaru



# Projected mass profiles from different analyses

**MACS1206**



Umetsu+12 Biviano+13

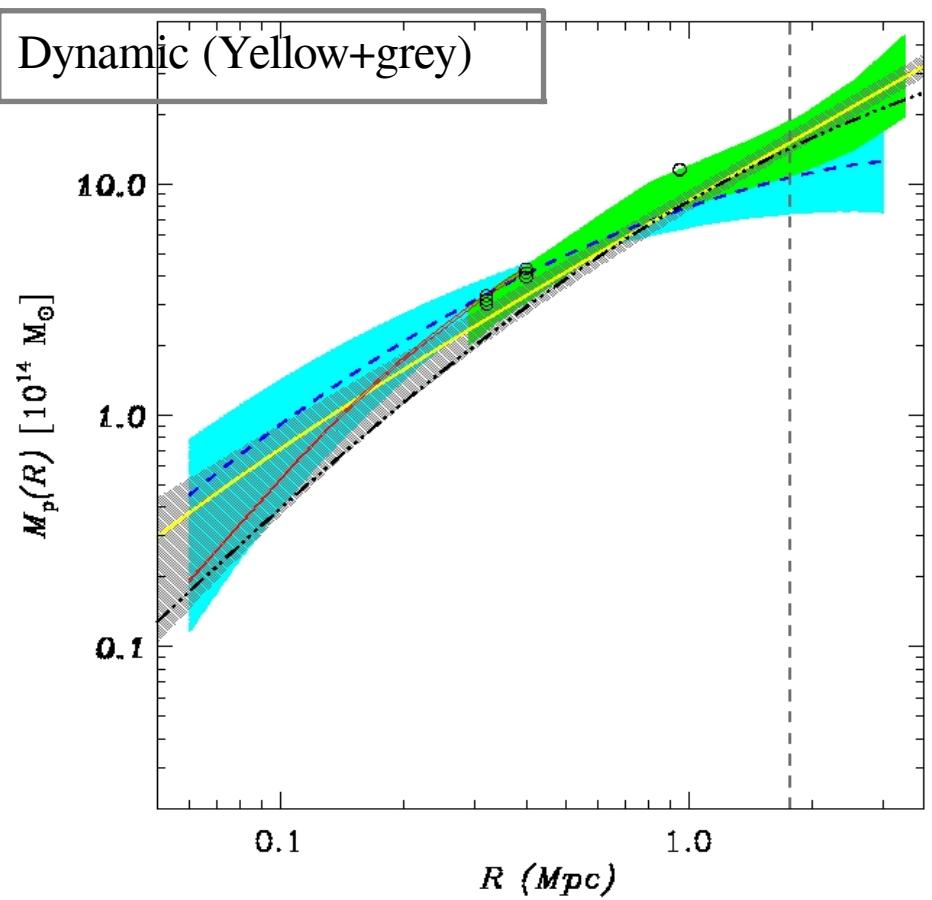
X-ray Chandra archival shallow data

Weak lensing (Umetsu+14)

**MACS 0416**

Strong lensing (Grillo+14)

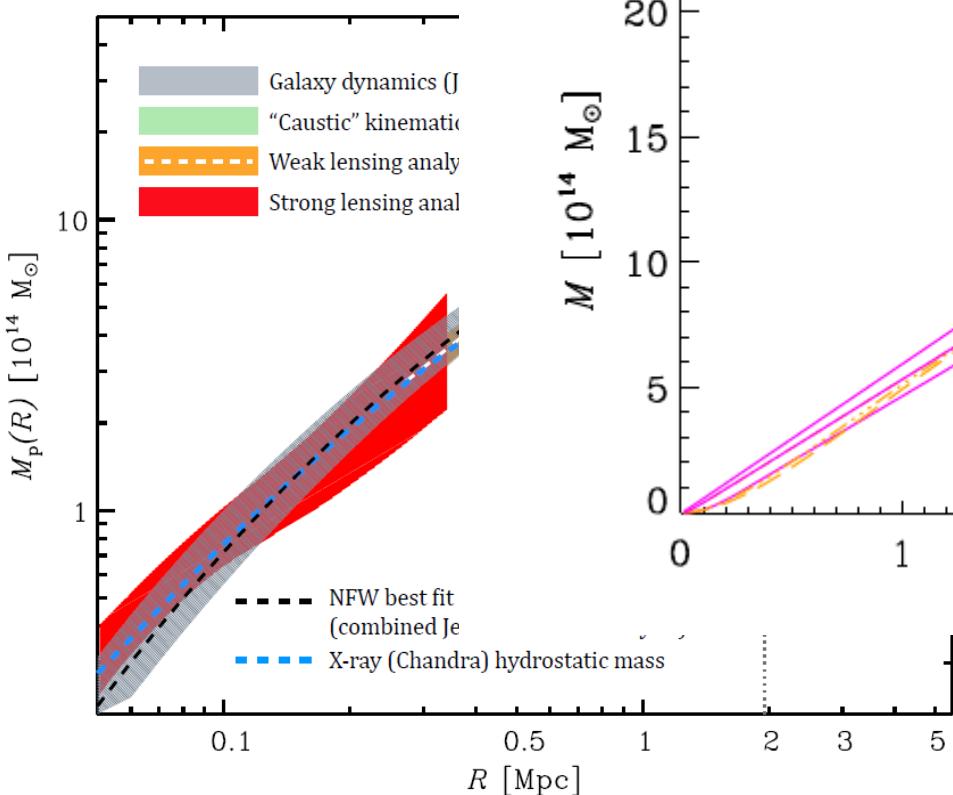
Dynamic (Yellow+grey)



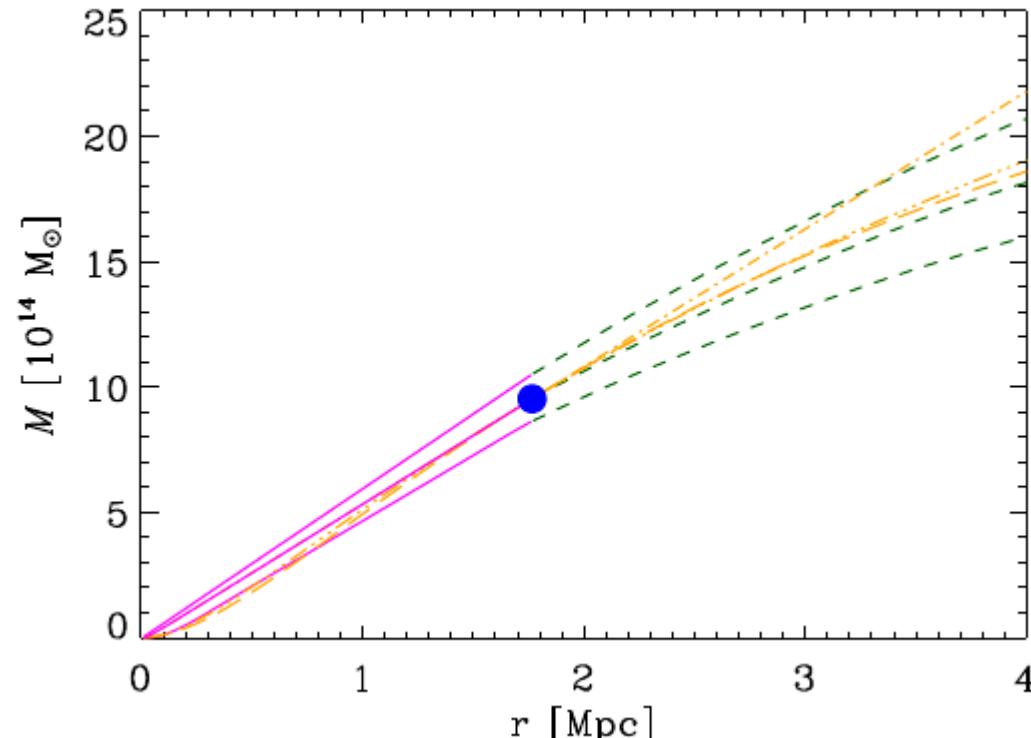
Balestra,BS+15

# Projected mass profiles from different analyses

MACS1206



MACS 0416

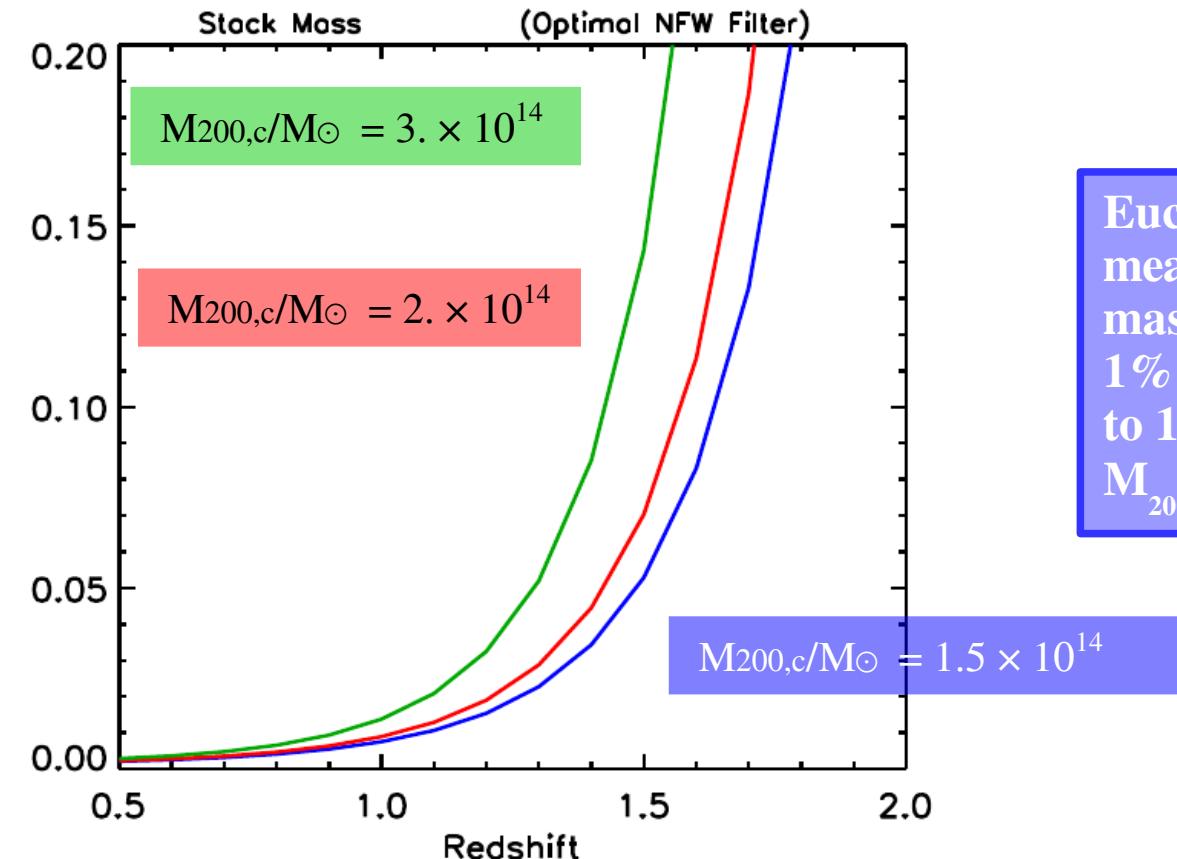


Umetsu+12 Biviano+13

Balestra,BS+15

# Observable- mass scaling relation calibration

Errors expected on the mean mass of clusters in bins of  $\Delta \log M_{200,c} = 0.2$  and  $\Delta z = 0.1$ .



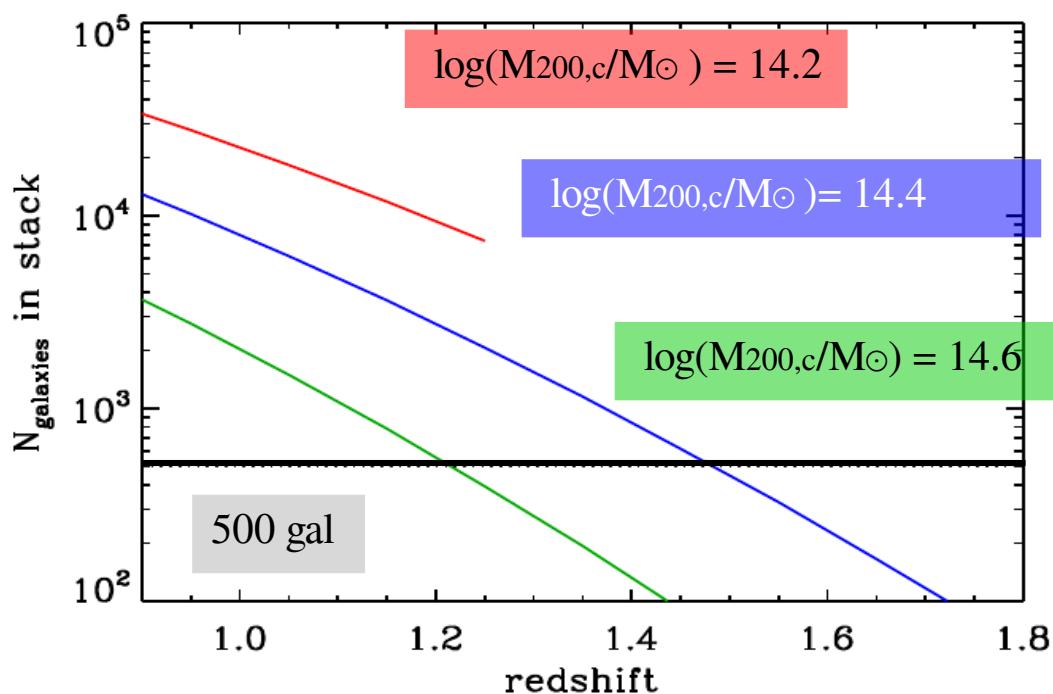
Euclid has the potential to calibrate the mean mass, and hence scaling relations bias, to 1% out to  $z=1$ , and to 10% out to  $z=1.6$  for clusters of  $M_{200,c} = 1.5 \times 10^{14} M_\odot$ .

At lower mass systems because their larger number compensates for their lower individual S/N measurements.

# Observable- mass scaling relation calibration

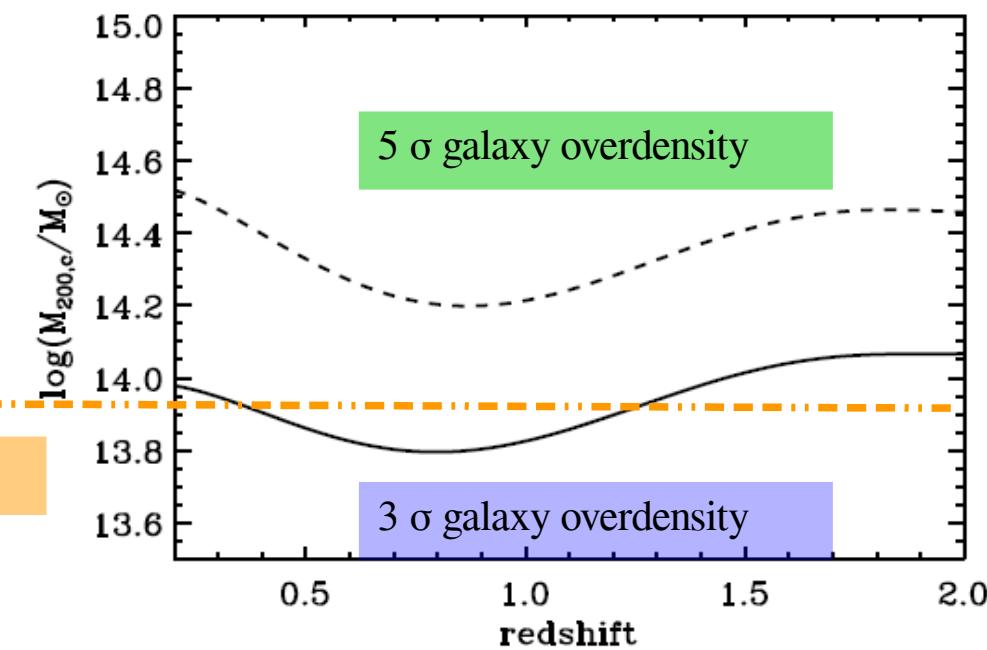
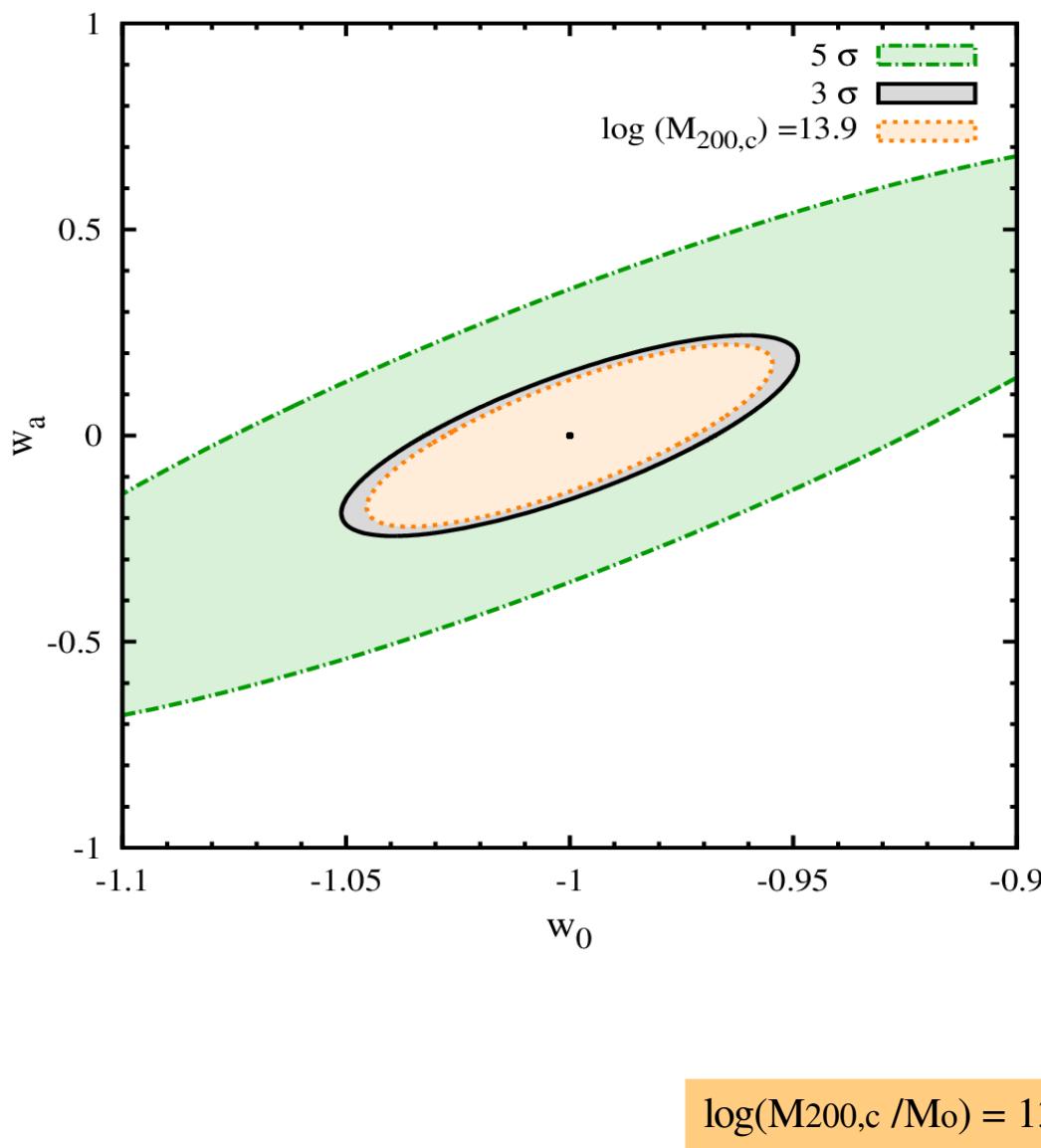
Number of cluster galaxies with spectroscopic redshifts available in stacks of clusters in bins of  $\Delta \log M = 0.2$  and  $\Delta z = 0.1$ , as a function of redshift.

The estimate is done only for clusters with a mass limit above that required for a minimum of 5 members with redshift. → This requirement stops the red curve



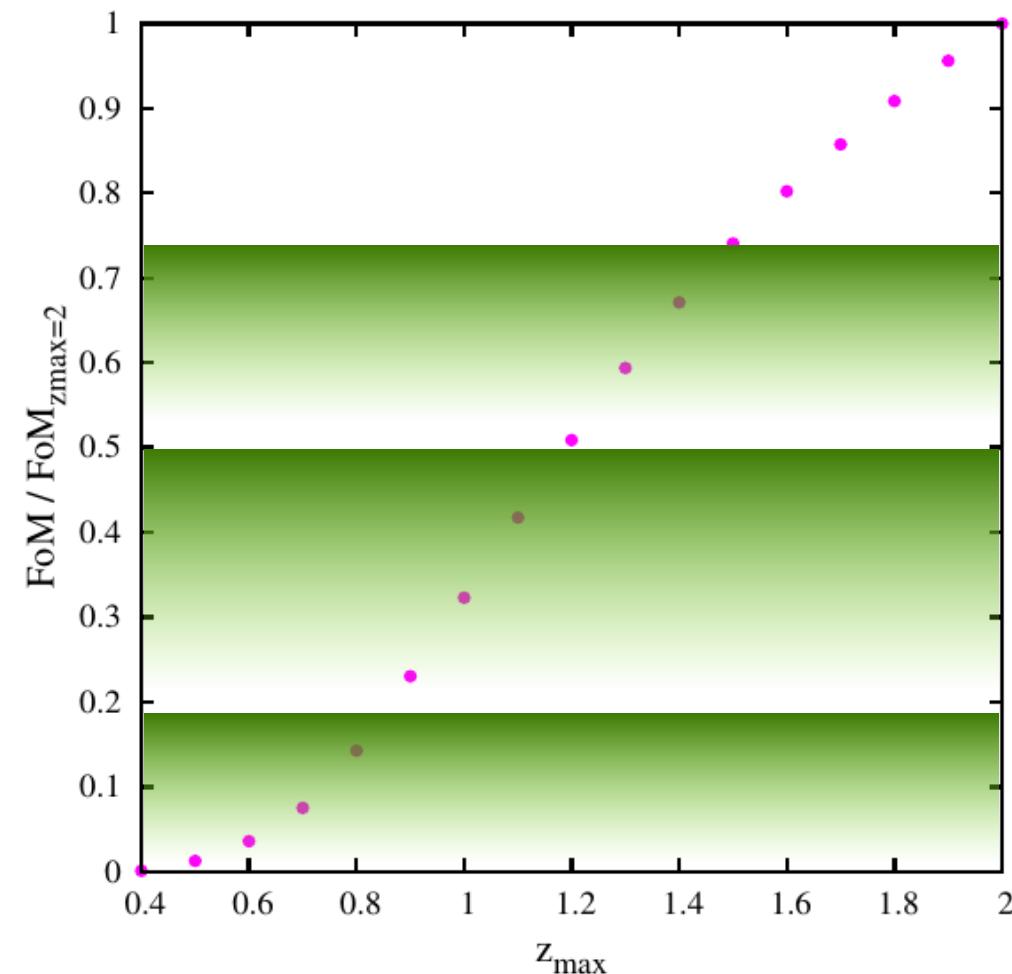
The statistical noise in the velocity dispersion estimate of a sample of  $\sim 500$  cluster members translates into a 30% statistical noise in the mass estimate.

# Impact of selection function



# Impact of high redshift clusters

Relative FoM for number counts in the  $3\sigma$  Euclid photometric cluster selection, as a function of the limiting redshift  $z_{\text{max}}$  of the survey, i.e. the ratio between the FoM evaluated over  $0.2 \leq z \leq z_{\text{max}}$  and the FoM evaluated over  $0.2 \leq z \leq 2.0$ .



$$\text{FoM} = \frac{1}{\sqrt{\det [\text{Cov}(p_i, p_j)]}}$$

# Constraints on deviation from GR

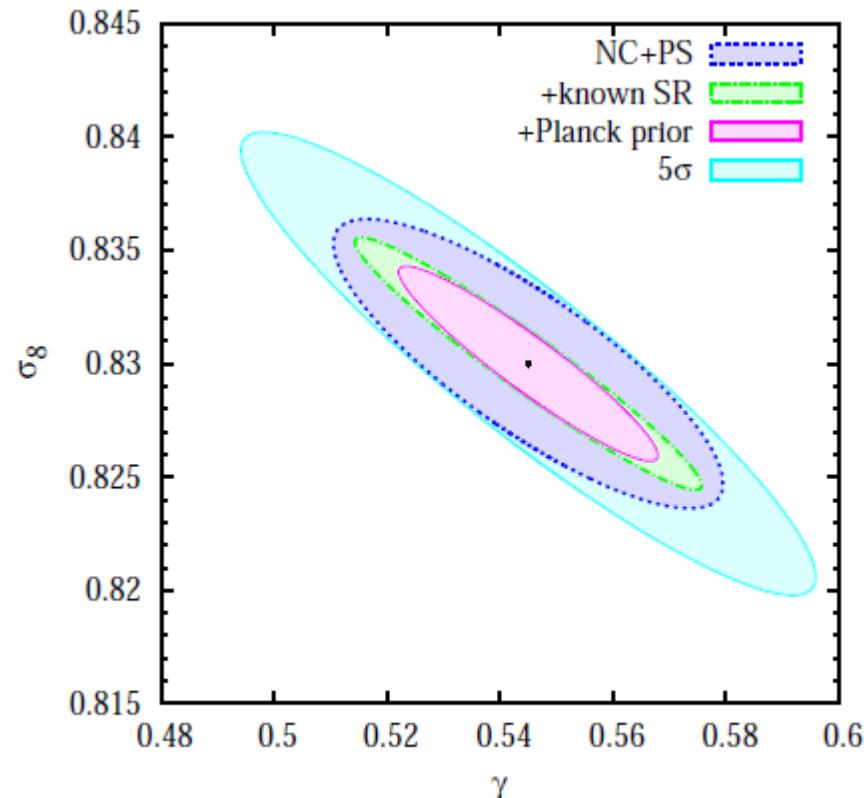
$N_{500,c}/\sigma_{\text{field}} \geq 3$  Euclid photometric cluster selection

Parameter arrays: Constraints:	Eqs. 16 & 28					Eqs. 22 & 28 $\Delta\gamma$	Eqs. 20 & 28 $\Delta f_{NL}$	Eqs. 26 & 28 $\Delta\Omega_\nu$
	FoM	$\Delta w_0$	$\Delta w_a$	$\Delta\Omega_m$	$\Delta\sigma_8$			
NC+PS	73	0.037	0.38	0.0019	0.0032	0.023	6.67	0.0015
NC+PS+known SR	291	0.034	0.16	0.0011	0.0014	0.020	6.58	0.0013
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$N_{500,c}/\sigma_{\text{field}} \geq 5$ Euclid photometric cluster selection								
NC+PS+known SR+Planck	209	0.034	0.12	0.0022	0.0026	0.034	6.74	0.0020

$$\mathbf{p} = \{\Omega_m, \sigma_8, w_0, w_a, \Omega_k, \Omega_b, H_0, n_s, \gamma\}$$

$$\frac{d \ln D(a)}{d \ln a} = \Omega_m^\gamma(a)$$

$$\mathbf{p}_{\text{nuisance, F}} = \{B_{M,0} = 0, \alpha = 0, \sigma_{\ln M,0} = 0.2, \beta = 0.125\}$$



# Constraints on deviation from GR

Parameter  
Constraints

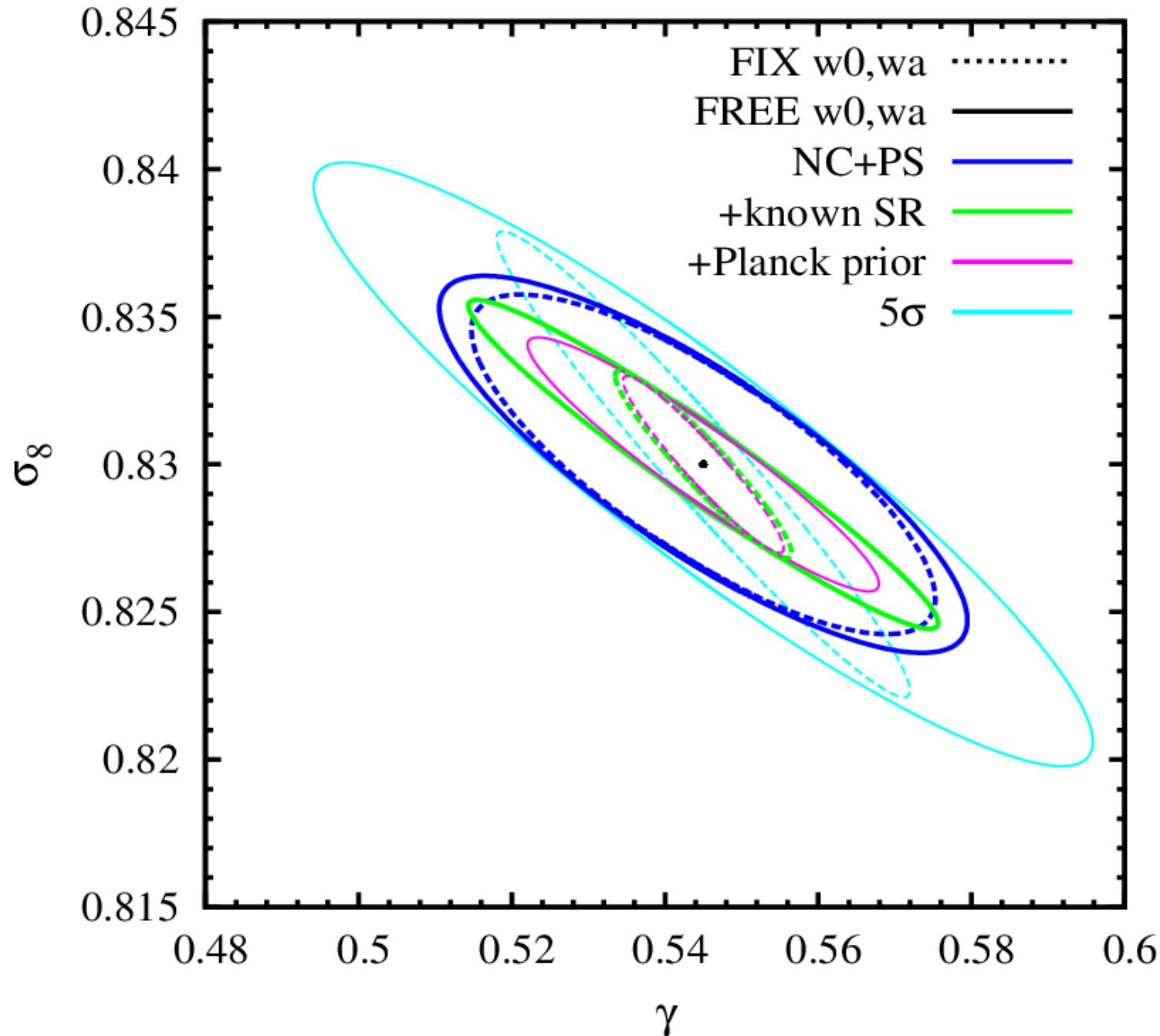
NC+PS  
NC+PS+ki  
NC+PS+ki

NC+PS+ki

$p = \{\Omega$

$\frac{d \ln L}{d \ln}$

$p_{\text{nuisance}, F}$



# Constraints on Non-Gaussianity

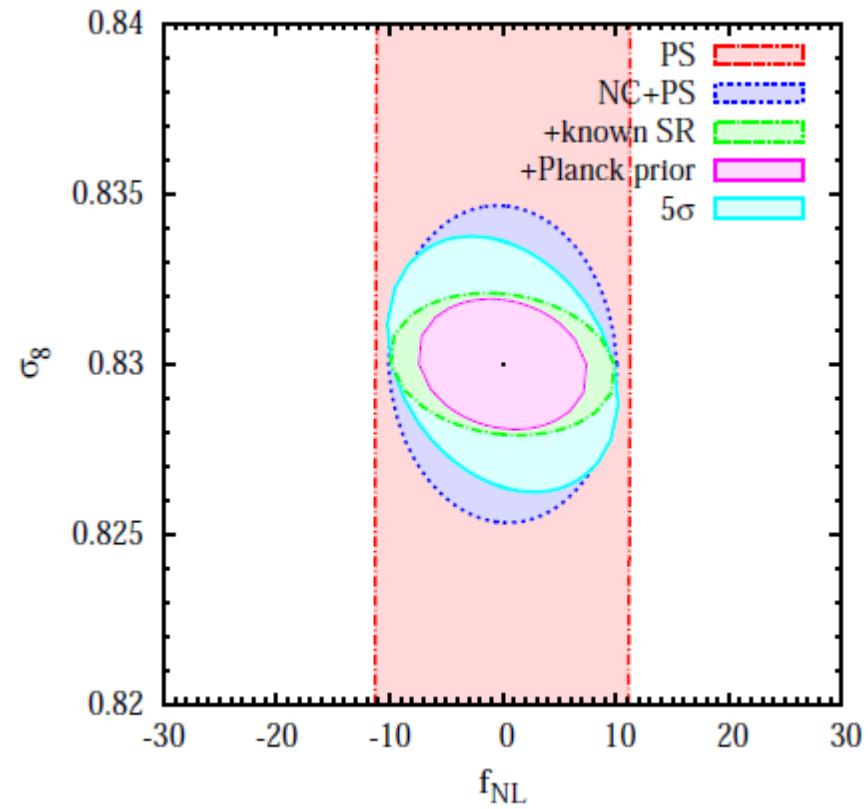
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$$\mathbf{p} = \{\Omega_m, \sigma_8, w_0, w_a, \Omega_k, \Omega_b, H_0, n_S, f_{NL}\}$$

$$\Phi = \Phi_G + f_{NL} (\Phi_G^2 - \langle \Phi_G^2 \rangle)$$

$$\mathbf{p}_{\text{nuisance},F} = \{B_{M,0} = 0, \alpha = 0, \sigma_{\ln M,0} = 0.2, \beta = 0.125\}$$

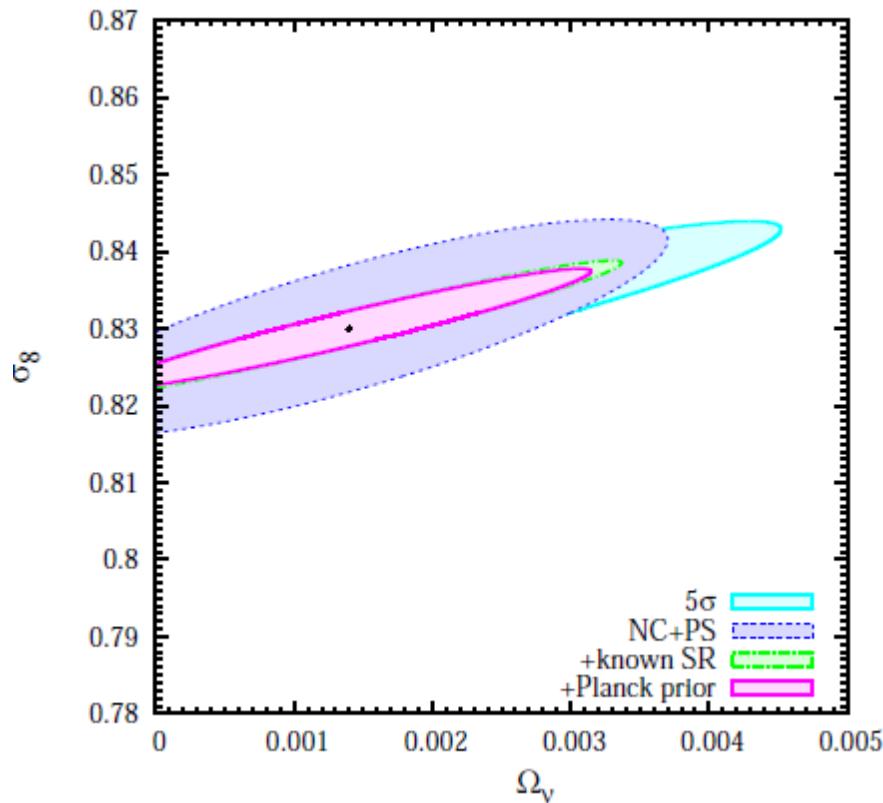


# Constraints on Neutrino mass

$N_{500,c}/\sigma_{\text{field}} \geq 3$ Euclid photometric cluster selection								
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NC+PS+known SR+Planck	209	0.034	0.12	0.0022	0.0026	0.034	6.74	0.0020



$$p = \{\Omega_m, \sigma_8, w_0, w_a, \Omega_k, \Omega_b, H_0, n_S, \Omega_\nu\}$$

$$\Omega_\nu = \frac{\rho_\nu}{\rho_c} = \frac{\sum_i^{N_\nu} m_{\nu,i}}{93.14 h^2 \text{ eV}},$$

$$\rho_m \rightarrow \rho_{CDM} = \rho_m - \rho_b$$

$$P_m \rightarrow P_{CDM}(k) = P_m(k) \left[ \frac{\Omega_{CDM} T_{CDM}(k, z) + \Omega_b T_b(k, z)}{(\Omega_b + \Omega_{CDM}) T_m(k, z)} \right]^2$$

$$p_{\text{nuisance, F}} = \{B_{M,0} = 0, \alpha = 0, \sigma_{\ln M,0} = 0.2, \beta = 0.125\}$$